CE4045 CZ4045 SC4002 Natural Language Processing

N-gram Language Models

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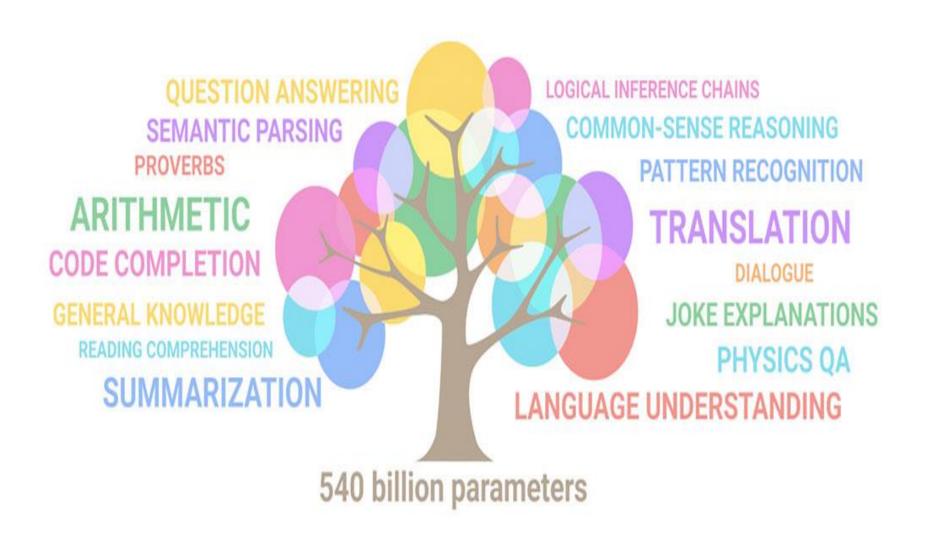
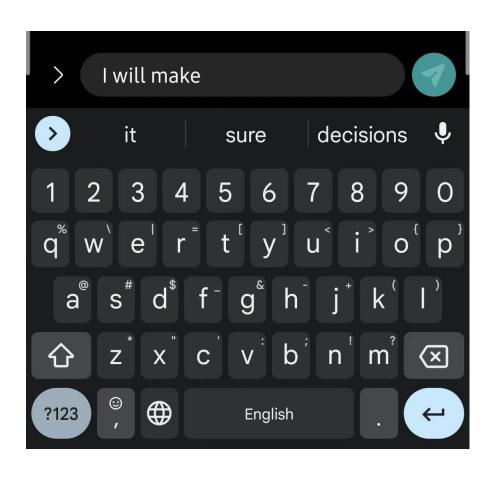


Image source: https://www.topbots.com/leading-nlp-language-models-2020/

Language Model: probabilities of sequences of words



Let's play a game

- Unlock your smart phone
- Compose a message or a note
- Start with word "I", the always select the first suggested word.
- What is the sentence you get?

> Example:

- "I will make
- Suggested next word:
 - it
 - sure
 - decisions

Why Language Model?

- ➤ Which sequence is more like a proper sentence?
 - "all of a sudden I notice three guys standing on the sidewalk"
 - "on guys all I of notice sidewalk three a sudden standing the"
- > Are such probabilities useful?
 - Speech recognition
 - "I will be back soonish" vs "I will be bassoon dish"
 - Spelling correction or grammatical error prediction
 - "Their are two midterms" vs "There are ..."
 - "Everything has improve" vs "has improved"
 - Machine translation
 - "他(he) 向(to) 记者(reporters) 介绍了(introduced) 主要(main)内容 (content)
 - "he introduced reporters to the main contents of the statement"
 - "he briefed to reporters the main contents of the statement"
 - "he briefed reporters on the main contents of the statement"

N-gram Model: The simplest language model

- Language models
 - N-gram language models
 - Neural language models
 - Pre-trained language models
 - Multimodal language models (text, vision, sound...)
- ➤ N-gram model
 - An n-gram is a sequence of n words;
 - 2-gram called bigram, 3-gram called trigram
 - Word sequence: "I like natural language processing"
 - Bigram: "I like" "like natural" "natural language" "language processing".
 - Trigram: "I like natural", "like natural language" "natural language processing"
 - An important foundational tool for understanding the fundamental concepts in LM

Our task: computing P(w|h)

- P(w|h): the probability of word w given some history h
 - Example: h is "I will make", and the word w is "it"
 - $P(w|h) = P(it|I \ will \ make)$
 - Estimate the probability P(w|h) from a large text collection
 - Count number of times "I will make" appears
 - Count number of times "I will make it" appears

$$P(w|h) = \frac{C(I \text{ will make } it)}{C(I \text{ will make})}$$



What if the history h is a long sequence like: "all of a sudden I notice three guys standing on the sidewalk"

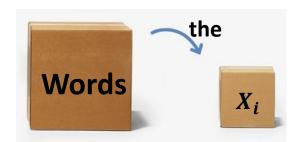
h w

Language is creative!

Chain rule of probability: a better way to compute P(w|h)

➤ Notations:

- The probability of a particular random variable X_i taking on the value "the" is $P(X_i = "the")$, or simply P(the)
- A sequence of N words either as $w_1, w_2, ..., w_n$ or $w_{1:n}$



- The joint probability of each word in a sequence having a particular value $P(X_1 = w_1; X_2 = w_2; X_3 = w_3; ...; X_n = w_n)$ is $P(w_1, w_2, ..., w_n)$ or $P(w_{1:n})$
- ➤ Chain rule of probability

$$P(X_1, ..., X_n) = P(X_1)P(X_2|X_1)P(X_3|X_1X_2) ... P(X_n|X_{1:n-1})$$

- Applying the chain rule to words
- $P(w_{1:n}) = P(w_1)P(w_2|w_1)P(w_3|w_1w_2) \dots P(w_n|w_{1:n-1}) = \prod_{k=1}^n P(w_k|w_{1:k-1})$
- We could estimate the joint probability of an entire sequence of words by multiplying together a number of conditional probabilities

N-gram: an approximation

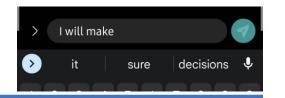
- \triangleright We now have: $P(w_{1:n}) = \prod_{k=1}^{n} P(w_k | w_{1:k-1})$
 - We could estimate the joint probability of an entire sequence of words by multiplying together a number of conditional probabilities
 - Question is: how to compute $P(w_n|w_{1:n-1})$?
 - In fact, we are at the starting point, to compute P(w|h): the probability of word w given some history h and $h = w_{1:n-1}$
- ➤ Bigram model
 - Approximates the probability of a word given all the previous words $P(w_n|w_{1:n-1})$ by using only the conditional probability of the preceding word $P(w_n|w_{n-1})$.
 - $P(w_n|w_{1:n-1}) \approx P(w_n|w_{n-1})$

This is called Markov assumption

Figure Generalize to N-gram model ($N \ge 2$):

$$P(w_n|w_{1:n-1}) \approx P(w_n|w_{n-N+1:n-1})$$

Bigram example



- Approximates the probability of a word given all the previous words $P(w_n|w_{1:n-1})$ by using only the conditional probability of the preceding word $P(w_n|w_{n-1})$.
- ➤ Before using bigram:

$$P(I \text{ will make it}) = P(I) \times P(\text{will}|I) \times P(\text{make}|I \text{ will}) \times P(\text{it}|I \text{ will make})$$

➤ With bigram

$$P(I \ will \ make \ it) = P(I) \times P(will | I) \times P(make | will) \times P(it | make)$$

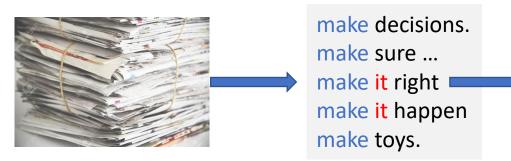
Bigram model

- \triangleright With bigram model $P(w_n|w_{1:n-1}) \approx P(w_n|w_{n-1})$
 - Our example

$$P(w|h) = P(it|I \ will \ make) \approx P(it|make)$$

$$P(w_{1:n}) = \prod_{k=1}^{n} P(w_k | w_{1:k-1}) \approx \prod_{k=1}^{n} P(w_k | w_{k-1})$$

- \triangleright Now, how to compute $P(w_n|w_{n-1})$, like P(it|make)?
 - Estimate bigram probabilities by maximum likelihood estimation or MLE
 - We estimate $P(w_n|w_{n-1}) = \frac{C(w_{n-1}w_n)}{C(w_{n-1})}$ where $C(\cdot)$ is the count, or frequency



$$C(make) = 5$$

 $C(make it) = 2$

P(it|make) = 0.4

An example with a mini-corpus of three sentences

$$<$$
s $>$ Sam I am $<$ /s $>$

<s> I do not like green eggs and ham </s>

- <s> is a special symbol at the beginning of the sentence to give us the bigram context of the first word.
- </s> is the end-symbol to make the bigram grammar a true probability distribution.
- Some of bigram probabilities from this corpus

$$P(I| < s >) = \frac{2}{3} = 0.67$$

•
$$P(Sam | < s >) = \frac{1}{3} = 0.33$$

•
$$P(am|I) = \frac{2}{3} = 0.67$$

•
$$P(|Sam) = \frac{1}{2} = 0.5$$

•
$$P(Sam|am) = \frac{1}{2} = 0.5$$

•
$$P(do|I) = \frac{1}{3} = 0.33$$

The chance a sentence starts with I is 67%
The chance a sentence starts with Sam is 33%
The chance word am follows I is 67%

- In practice, trigram is more commonly used.
- If trigram is used, then we need to add extra context,
 e.g., P(The | < s >< s >)

Let's take a larger example: Berkeley Restaurant Project

- A dialogue system from the last century that answered questions about a database of restaurants in Berkeley, California.
- A sample of 9332 sentences is on the website http://www1.icsi.berkeley.edu/Speech/berp.html
- ➤ Some sample sentences:
 - can you tell me about any good cantonese restaurants close by
 - mid priced thai food is what i'm looking for
 - tell me about chez panisse
 - can you give me a listing of the kinds of food that are available
 - i'm looking for a good place to eat breakfast
 - when is caffe venezia open during the day

Unigram counts and bigram counts for example words

- ➤ Number of sentences: 9332
- ➤ Number of unique words (vocabulary): 1446
- > A sample of 7 words with unigram counts and bigram counts

| i | want | to | eat | chinese | food | lunch | spend |
|------|------|------|-----|---------|------|-------|-------|
| 2533 | 927 | 2417 | 746 | 158 | 1093 | 341 | 278 |

(I want) occurred 827 times

(Chinese food) occurred 82 times

 W_n

| | i | want | to | eat | chinese | food | lunch | spend |
|---------|----|------|-----|-----|---------|------|-------|-------|
| i | 5 | 827 | 0 | 9 | 0 | 0 | 0 | 2 |
| want | 2 | 0 | 608 | 1 | 6 | 6 | 5 | 1 |
| to | 2 | 0 | 4 | 686 | 2 | 0 | 6 | 211 |
| eat | 0 | 0 | 2 | 0 | 16 | 2 | 42 | 0 |
| chinese | 1 | 0 | 0 | 0 | 0 | 82 | 1 | 0 |
| food | 15 | 0 | 15 | 0 | 1 | 4 | 0 | 0 |
| lunch | 2 | 0 | 0 | 0 | 0 | 1 | 0 | 0 |
| spend | 1 | 0 | 1 | 0 | 0 | 0 | 0 | 0 |

 w_{n-1}

Bigram probabilities

- > Based on the unigram counts and bigram counts
- > We have the following sample bigram probabilities
- > We can estimate other bigram probabilities as well

| i | want | to | eat | chinese | food | lunch | spend |
|------|------|------|-----|---------|------|-------|-------|
| 2533 | 927 | 2417 | 746 | 158 | 1093 | 341 | 278 |

| | i | want | to | eat | chinese | food | lunch | spend |
|---------|----|------|-----|-----|---------|------|-------|-------|
| i | 5 | 827 | 0 | 9 | 0 | 0 | 0 | 2 |
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| food | 15 | 0 | 15 | 0 | 1 | 4 | 0 | 0 |
| lunch | 2 | 0 | 0 | 0 | 0 | 1 | 0 | 0 |
| spend | 1 | 0 | 1 | 0 | 0 | 0 | 0 | 0 |

$$P(want|i) = 0.33$$
 $P(to|want) = 0.66$

| | i | want | to | eat | chinese | food | lunch | spend |
|---------|---------|------|--------|--------|---------|--------|--------|---------|
| i | 0.002 | 0.33 | 0 | 0.0036 | 0 | 0 | 0 | 0.00079 |
| want | 0.0022 | 0 | 0.66 | 0.0011 | 0.0065 | 0.0065 | 0.0054 | 0.0011 |
| to | 0.00083 | 0 | 0.0017 | 0.28 | 0.00083 | 0 | 0.0025 | 0.087 |
| eat | 0 | 0 | 0.0027 | 0 | 0.021 | 0.0027 | 0.056 | 0 |
| chinese | 0.0063 | 0 | 0 | 0 | 0 | 0.52 | 0.0063 | 0 |
| food | 0.014 | 0 | 0.014 | 0 | 0.00092 | 0.0037 | 0 | 0 |
| lunch | 0.0059 | 0 | 0 | 0 | 0 | 0.0029 | 0 | 0 |
| spend | 0.0036 | 0 | 0.0036 | 0 | 0 | 0 | 0 | 0 |

Now you can compute a probability of a sentence

| | i | want | to | eat | chinese | food | lunch | spend |
|---------|---------|------|--------|--------|---------|--------|--------|----------|
| i | 0.002 | 0.33 | 0 | 0.0036 | 0 | 0 | 0 | 0.00079 |
| want | 0.0022 | 0 | 0.66 | 0.0011 | 0.0065 | 0.0065 | 0.0054 | 0.0011 |
| to | 0.00083 | 0 | 0.0017 | 0.28 | 0.00083 | 0 | 0.0025 | 0.087 |
| eat | 0 | 0 | 0.0027 | 0 | 0.021 | 0.0027 | 0.056 | 0 |
| chinese | 0.0063 | 0 | 0 | 0 | 0 | 0.52 | 0.0063 | 0 |
| food | 0.014 | 0 | 0.014 | 0 | 0.00092 | 0.0037 | 0 | 0 |
| lunch | 0.0059 | 0 | 0 | 0 | 0 | 0.0029 | 0 | Addition |
| spend | 0.0036 | 0 | 0.0036 | 0 | 0 | 0 | 0 | P(i < s |

> Probability of sentence: "I want English food"

P(<s> I want English food </s>)

- = =P(i|<s>) P(want|i) P(English|want) P(food|English) P(</s>|food)
- $= 0.25 \times 0.33 \times 0.0011 \times 0.5 \times 0.68$
- = 0.000031

Practical issues: Probability of a sentence is typically very small. To avoid numerical underflow, we use log probabilities. $p_1 \times p_2 \times p_3 \times p_4 = \exp(\log p_1 + \log p_2 + \log p_3 + \log p_4)$

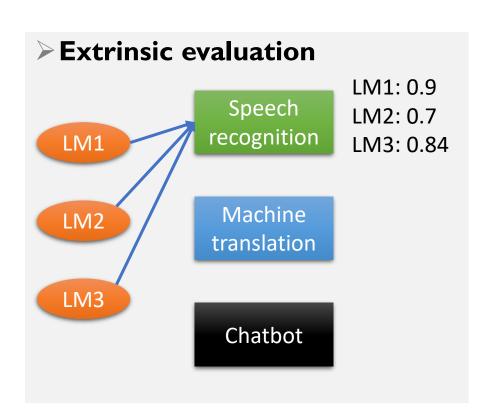
P(english|want) = 0.0011

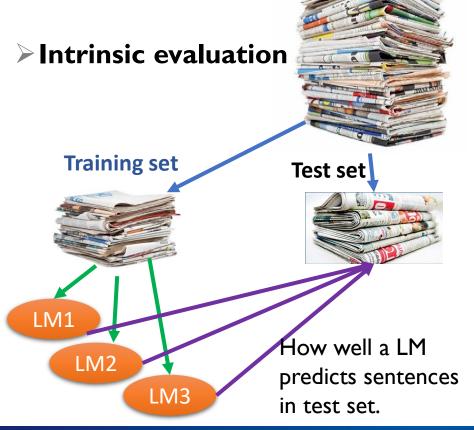
P(food|English) = 0.5P(</s > |food) = 0.68

Evaluating Language Model

> We may learn a bigram model, a trigram model, or other types of LMs

How do we know any model is good?



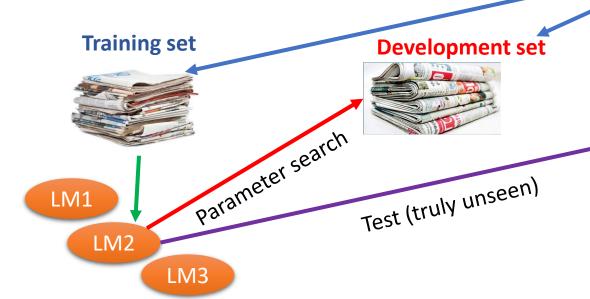


Intrinsic evaluation

If a **test set** is very frequently used, we may learn some of its characteristics. There is a risk that we tune some parameters to make the model perform better on test set.

> A development set is often used to learn parameters.

A typical split ratio is 8:1:1



Test set



How well a LM predicts sentences in test set.

What measure to use?

Perplexity

Perplexity (PP) is the probability of the test set (assigned by the language model), normalized by the number of words. N denotes number of words in a test data, $w1, ..., w_N$ is the test data.

$$PP(W) = P(w_1 w_2 \dots w_N)^{-\frac{1}{N}} = \sqrt[N]{\frac{1}{P(w_1 w_2 \dots w_N)}}$$

> Chain rule:
$$PP(W) = \sqrt[N]{\prod_{i=1}^{N} \frac{1}{P(w_i|w_1...w_{i-1})}}$$

For bigrams:
$$PP(W) = \sqrt[N]{\prod_{i=1}^{N} \frac{1}{P(w_i|w_{i-1})}}$$

A good model gives high probability on test data, hence a **low perplexity** value.

An (intrinsic) improvement in perplexity does not guarantee an (extrinsic) improvement in the performance on a real task.

Let's take a closer look at testing

Training set (Straits Times, Jan – Sept)

Test set (Straits Times, Oct – Dec)



"Coronavirus disease COVID-19 is"

- The word "COVID-19" never appears in training data
- \triangleright The model has no knowledge about this word, P(COVID-19|any_word) = 0
- Then the perplexity is undefined

$$PP(W) = \sqrt[N]{\prod_{i=1}^{N} \frac{1}{P(w_i|w_{i-1})}}$$

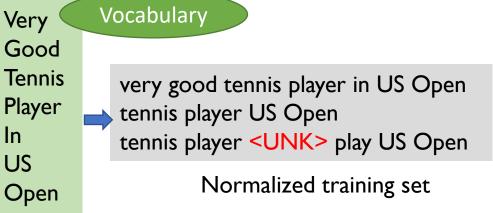
> Happens to all unknown words, a.k.a out of vocabulary (OOV) words

Need to handle potentially unknown words in training

- In training, we add a pseudo-word called <UNK>.
 - Any potential unknown word in the test set is considered as an instance of <UNK>
- ➤ But where are the instances of <UNK> in training data?
- ➤ Modeling <UNK>
 - Choose a vocabulary (word list) that is fixed in advance, before training.
 - Convert in the training set any word that is not in this vocabulary to the unknown word token <UNK>, in a text normalization step.
 - Estimate the probabilities for <UNK> from its counts, just like any other regular word in the training set.
- > Example:

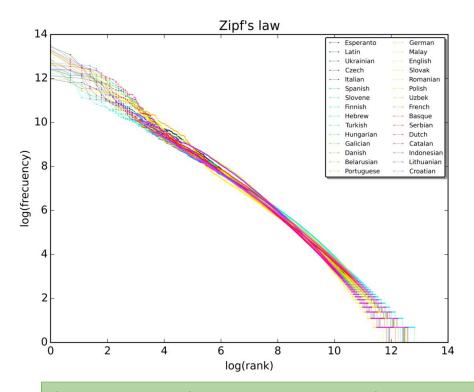
very good tennis player in US Open tennis player US Open tennis player qualify play US Open

Original training set



Modeling <UNK>

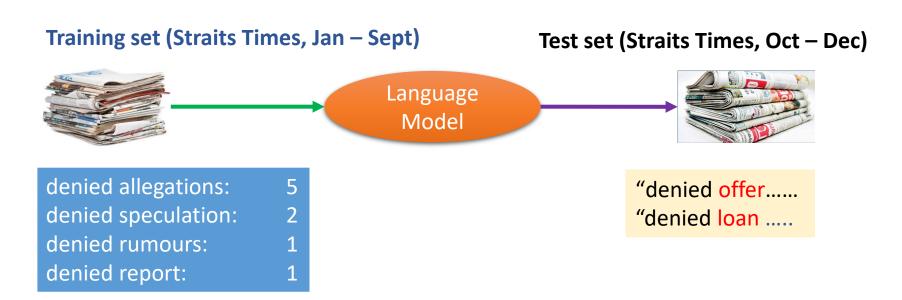
- ➤ How to create a vocabulary
 - Approach I: Based on some existing knowledge about the dataset, and fix a vocabulary in advance,
 - Approach II: Implicitly define a vocabulary based on word distribution
- > Example for Approach II.
 - Count the frequency of every words in training data
 - All words that appear fewer than K times are considered as <UNK>,
 e.g., K = 3



A small number of events occur with high frequency A large number of events occur with low frequency

https://en.wikipedia.org/wiki/Zipf%27s_law

Let's re-look at testing



- ➤ Both words "offer" and "loan" are common words (there is no unknown words)
- > But, the model does not see "denied offer" or "denied loan" in training
 - P(offer|denied) = 0? P(loan|denied) = 0?

The training data is never large enough to cover *all* possible word combinations!

Smoothing: avoid assigning zero probabilities to unseen events

- There are many smoothing techniques available
 - Laplace (add-one) smoothing
 - Add-k smoothing
 - Stupid backoff
 - Kneser-Ney smoothing
- The simplest way to do smoothing: Laplace Smoothing
 - Assuming every possible n-gram appears once which we do not explicitly observe.
 - Add one to all the n-gram counts, before we normalize them into probabilities.
 - Laplace smoothing does not perform well enough to be used smoothing in modern n-gram models
 - But it usefully introduces many of the concepts in other smoothing algorithms,
 - Is a practical smoothing algorithm for other tasks like text classification

Laplace Smoothing Example

| i | want | to | eat | chinese | food | lunch | spend |
|------|------|------|-----|---------|------|-------|-------|
| 2533 | 927 | 2417 | 746 | 158 | 1093 | 341 | 278 |

Raw counting

| | | O | | | | | | |
|---------|----|------|-----|-----|---------|------|-------|-------|
| | i | want | to | eat | chinese | food | lunch | spend |
| i | 5 | 827 | 0 | 9 | 0 | 0 | 0 | 2 |
| want | 2 | 0 | 608 | 1 | 6 | 6 | 5 | 1 |
| to | 2 | 0 | 4 | 686 | 2 | 0 | 6 | 211 |
| eat | 0 | 0 | 2 | 0 | 16 | 2 | 42 | 0 |
| chinese | 1 | 0 | 0 | 0 | 0 | 82 | 1 | 0 |
| food | 15 | 0 | 15 | 0 | 1 | 4 | 0 | 0 |
| lunch | 2 | 0 | 0 | 0 | 0 | 1 | 0 | 0 |
| spend | 1 | 0 | 1 | 0 | 0 | 0 | 0 | 0 |

$$P(want|I) = \frac{C(I want)}{C(I)} = \frac{827}{2533}$$

Laplace smoothing (add-one)

| | i | want | to | eat | chinese | food | lunch | spend |
|---------|----|------|-----|-----|---------|------|-------|-------|
| i | 6 | 828 | 1 | 10 | 1 | 1 | 1 | 3 |
| want | 3 | 1 | 609 | 2 | 7 | 7 | 6 | 2 |
| to | 3 | 1 | 5 | 687 | 3 | 1 | 7 | 212 |
| eat | 1 | 1 | 3 | 1 | 17 | 3 | 43 | 1 |
| chinese | 2 | 1 | 1 | 1 | 1 | 83 | 2 | 1 |
| food | 16 | 1 | 16 | 1 | 2 | 5 | 1 | 1 |
| lunch | 3 | 1 | 1 | 1 | 1 | 2 | 1 | 1 |
| spend | 2 | 1 | 2 | 1 | 1 | 1 | 1 | 1 |

$$P(want|I) = \frac{C(I \ want) + 1}{C(I) + ?} = \frac{828}{2533 + ?}$$

Laplace Smoothing Example

| | i | want | to | eat | chinese | food | lunch | spend |
|---------|----|------|-----|-----|---------|------|-------|-------|
| i | 6 | 828 | 1 | 10 | 1 | 1 | 1 | 3 |
| want | 3 | 1 | 609 | 2 | 7 | 7 | 6 | 2 |
| to | 3 | 1 | 5 | 687 | 3 | 1 | 7 | 212 |
| eat | 1 | 1 | 3 | 1 | 17 | 3 | 43 | 1 |
| chinese | 2 | 1 | 1 | 1 | 1 | 83 | 2 | 1 |
| food | 16 | 1 | 16 | 1 | 2 | 5 | 1 | 1 |
| lunch | 3 | 1 | 1 | 1 | 1 | 2 | 1 | 1 |
| spend | 2 | 1 | 2 | 1 | 1 | 1 | 1 | 1 |

- ➤ What are added to the training text?
 - For each word, we have added |V| number of additional appearance.
 - |V| is the size of vocabulary.

| (I I) (I want) (I to) (I Chinese) | (want I) (to I) (Chinese I) |
|--|-----------------------------------|
| (I food) (I lunch) (I spend) (I) | (food I) (lunch I) (spend I) (I) |
| | •••• |

(I, every word in vocabulary)

$$P_{laplace}(want|I) = \frac{C(I \ want) + 1}{C(I) + V} = \frac{828}{2533 + 1446}$$

In this example dataset: Number of unique words (vocabulary): I 446

Laplace Smoothing

➤ Before smoothing

$$P(w_n|w_{n-1}) = \frac{C(w_{n-1}w_n)}{C(w_{n-1})}$$

With Laplace smoothing

•
$$P_{laplace}(w_n|w_{n-1}) = \frac{C(w_{n-1}w_n)+1}{C(w_{n-1})+V}$$

| | i | want | to | eat | chinese | food | lunch | spend |
|---------|---------|------|--------|--------|---------|--------|--------|---------|
| i | 0.002 | 0.33 | 0 | 0.0036 | 0 | 0 | 0 | 0.00079 |
| want | 0.0022 | 0 | 0.66 | 0.0011 | 0.0065 | 0.0065 | 0.0054 | 0.0011 |
| to | 0.00083 | 0 | 0.0017 | 0.28 | 0.00083 | 0 | 0.0025 | 0.087 |
| eat | 0 | 0 | 0.0027 | 0 | 0.021 | 0.0027 | 0.056 | 0 |
| chinese | 0.0063 | 0 | 0 | 0 | 0 | 0.52 | 0.0063 | 0 |
| food | 0.014 | 0 | 0.014 | 0 | 0.00092 | 0.0037 | 0 | 0 |
| lunch | 0.0059 | 0 | 0 | 0 | 0 | 0.0029 | 0 | 0 |
| spend | 0.0036 | 0 | 0.0036 | 0 | 0 | 0 | 0 | 0 |

P(to|want) changed from 0.66 to 0.26!

→ too much probability mass is moved to all the zeros.

| | i | want | to | eat | chinese | food | lunch | spend |
|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| i | 0.0015 | 0.21 | 0.00025 | 0.0025 | 0.00025 | 0.00025 | 0.00025 | 0.00075 |
| want | 0.0013 | 0.00042 | 0.26 | 0.00084 | 0.0029 | 0.0029 | 0.0025 | 0.00084 |
| to | 0.00078 | 0.00026 | 0.0013 | 0.18 | 0.00078 | 0.00026 | 0.0018 | 0.055 |
| eat | 0.00046 | 0.00046 | 0.0014 | 0.00046 | 0.0078 | 0.0014 | 0.02 | 0.00046 |
| chinese | 0.0012 | 0.00062 | 0.00062 | 0.00062 | 0.00062 | 0.052 | 0.0012 | 0.00062 |
| food | 0.0063 | 0.00039 | 0.0063 | 0.00039 | 0.00079 | 0.002 | 0.00039 | 0.00039 |
| lunch | 0.0017 | 0.00056 | 0.00056 | 0.00056 | 0.00056 | 0.0011 | 0.00056 | 0.00056 |
| spend | 0.0012 | 0.00058 | 0.0012 | 0.00058 | 0.00058 | 0.00058 | 0.00058 | 0.00058 |

Add-k Smoothing

- > Move a bit less of the probability mass from the seen to the unseen events.
- Instead of adding I to each count, we add a fractional count k (0 < k < 1)

$$P_{Add-k}(w_n|w_{n-1}) = \frac{C(w_{n-1}w_n) + k}{C(w_{n-1}) + kV}$$

- The value of k can be 0.1, 0.05, 0.5 or other values, determined on a development set.
- Add-k is useful for some tasks like text classification, but in general does not do well for language modeling

Backoff and Interpolation

➤ Backoff: use less context

- We use the trigram if the evidence is sufficient, otherwise we use the bigram, otherwise the unigram.
- We only "back off" to a lower-order n-gram if we have zero evidence for a higher-order n-gram.

➤ Interpolation

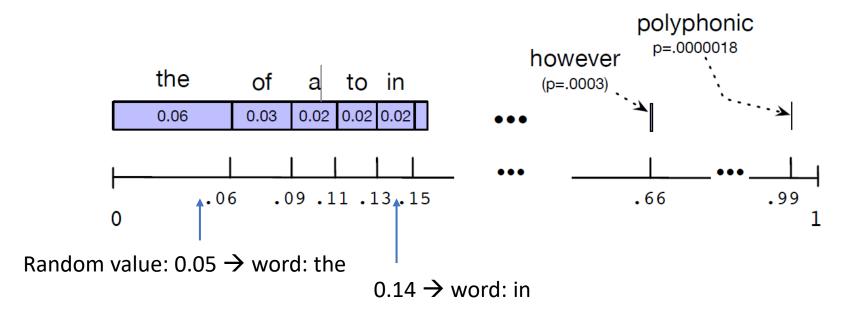
- We always mix the probability estimates from all the n-gram estimators, weighting and combining the trigram, bigram, and unigram counts.
- $\hat{P}(w_n|w_{n-2}w_{n-1}) = \lambda_1 P(w_n) + \lambda_2 P(w_n|w_{n-1}) + \lambda_3 P(w_n|w_{n-2}w_{n-1})$
- $\lambda_1 + \lambda_2 + \lambda_3 = I$

Language Generation

- Sampling sentences from a language model
 - Sampling from a distribution: choose random points according to their likelihood.
 - Sampling from a language model, which represents a distribution over sentences, means to generate some sentences: choose each sentence according to its likelihood
- > Visualize how sentence generation works for the unigram case.
 - A unigram language model is a collection of unigram probabilities, e.g., $P(the), P(of), P(a) \dots$
 - We place these unigram probabilities on a line, ordered by their probabilities
 - Then we generate a random value between 0 and 1, find the point on the probability line, and print the word whose interval includes this random value

Language Generation (for unigram case)

- Visualize how sentence generation works for the unigram case.
 - A unigram language model is a collection of unigram probabilities, e.g., $P(the), P(of), P(a) \dots$
 - We place these unigram probabilities on a line, ordered by their probabilities
 - Then we generate a random value between 0 and 1, find the point on the probability line, and print the word whose interval includes this random value



Language Generation (for bigram case)

- For bigram cases:
 - Generate the first word by sampling $P(word_1 \mid < S >)$
 - Generate the second word by sampling $P(word_2|word_1)$
 - Generate the rest of the words.
 - Generation stops when $P(</s>|word_n)$ is generated.

```
For bigram cases:

P(word_1 | < S >)
enerate the first word by sampling P(word_1 | < S >)
enerate the second word by sampling P(word_2 | word_1)
enerate the rest of the words.

• Generation stops when P(</s > | word_n) is generated.
```

Random value: 0.05 → word: the

 $0.14 \rightarrow$ word: in

N-gram Language Model

- Word prediction
 - Probability of a sequence of words $P(w_1w_2 w_n)$, or probability of a word given some history P(w|h)
- ➤ N-grams
 - Counting and basic concepts
- ➤ N-gram Language Model
 - Modeling unknown words
 - Smoothing to avoid assigning zero probabilities to unseen sequences
 - Evaluation
- ➤ Reference: https://web.stanford.edu/~jurafsky/slp3/
 - Chapter 3, N-gram Language Models

What can we do?

- > Given a collection of documents, we are able to train a language model
- Given a language model, we are able to compute the probability of sentences
- Given a language model, we can also generate sentences