



华南理工大学

South China University of Technology

The Experiment Report of *Machine Learning*

College	Software College
Subject	Software Engineering
Student ID	201722800100
E-mail	Az.yamen@gmail.com
Tutor	Mingkui Tan
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Linear Regression, Linear Classification and Gradient Descent

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Reported By:

Ezzaddin Ahmed Othman Saeed

Purposes:

- Use data set to identify relationships among variables and use these relationships to make predictions(Regression).
- To estimate likely performance of a model on out-of-sample data.
- To realize the process of optimization and adjusting parameters and further understand of liner regression and gradient descent.

Data sets and data analysis:

In this work, I used two LIBSVM datasets which are pre-processed data originally from UCI data repository.

- *Data set 1: Housing (Boston) :*
 - (data: 506 , features: 13):

Linear Regression uses (Housing) data set in **LIBSVM Data**, including 506 samples and each sample has 13 features.

This data set contains information about the housing values in suburbs of Boston.

- *Data set 2 : Australian*
 - (classes: 2 , data: 690 of features: 14)

Linear classification uses (Australian) data set in **LIBSVM Data**, including 690 samples and each sample has 14 features.

Experimental steps:

Experiment 1 : (Linear Regression and Gradient Descent)

step 1: Load the experiment data. You can

use `load_svmlight_file` function in `sklearn` library.

step 2: Divide dataset. Here I divide dataset into training set and validation set using `train_test_split` function. Of course Test set is not required in this experiment.

step 3: Initialize linear model parameters. Here I choose normal distribution to initialize the model .

step 4: Choose loss function and derivation: Find more detail in PPT.

step 5: from all samples I calculate gradient toward loss function.

step 6: Denote the opposite direction of gradient as $G \rightarrow D$.

step 7: Update model.

step 8: Get the loss under the training set and by validating under validation set.

step 9: Repeat step 5 to 8 for several times, and drawing graph of as well as with the number of iterations.

Experiment 2 : (Linear Classification and Gradient Descent)

step 1: Load the experiment data.

step 2: Divide dataset into training set and validation set by using `train_test_split` function .

step 3: Initialize SVM model parameters with normal distribution.

step 4: I identify loss function and derivation.

step 5: Calculate gradient toward loss function from all samples.

step 6: Denote the opposite direction of gradient G as D .

step 7: Update model.

step 8: Get the loss under the train in set and by validating under validation set.

step 9: repeat step 5 to 8 for several times, and drawing graph of as well as with the number of iterations.

Code:

For linear regression :

```
1 #this code Done By:
2 #     Ezzaddin Ahmed Othman Saeed
3 #     Taliz-Yemen
4 #-----
5
6 from sklearn.externals.joblib import Memory
7
8 # STEP 1:
9
10 # load the experiment data by import load_svmlight_file function in sklearn library
11
12 from sklearn.datasets import load_svmlight_file
13 mem = Memory("./mycache")
14
15 mem.cache
16 def get_data():
17     data = load_svmlight_file("./datasets/housing_scale")
18
19     return data
20
21 X, Y = get_data()
22 X = X.data.reshape(X.shape)
23
24
25 ##### STEP 2: #####
26 # divide the dataset into training set && validation set by train_test_split function
27
28 # ==> validation set isn't requier here <==
29
30 from sklearn.model_selection import train_test_split
31 X_train, X_validation, Y_train, Y_validation = train_test_split(X, Y, test_size=0.5)
32
33 print(X_train.shape,type(X_train)) #
34
35
36
37
38 #there are several ways to implement a linear regression
39 import numpy # here I used numpy To do linear regression
40
41 n_samples_train, n_features = X_train.shape ## n_samples_train is training sample & n_features is number of features
42
43 X_train = numpy.concatenate((X_train,numpy.ones((n_samples_train,1))),axis=1)
44 Y_train = numpy.reshape(Y_train,(n_samples_train,1))
45
46 n_samples_validation, _ = X_validation.shape
47 X_validation = numpy.concatenate((X_validation,numpy.ones((n_samples_validation,1))),axis=1)
48 Y_validation = numpy.reshape(Y_validation,(n_samples_validation,1))
49
50 factor = 0.5
51 learning_rate = 0.0008
52
53
54 # # # STEP 3:
55
56 ##### Initialize linear model parameters #####
57
58 W = numpy.random.normal(0.01,0.1,size=(n_features + 1,1)) # initialize with zero normal distribution
59
60 losses_train = []
61 losses_val = []
62
63 max_loop = 200 ## total Iterations - No. Loops=200
64
65 for epoch in range(max_loop):
66     diff = numpy.dot(X_train,W) - Y_train
67     G = factor * W + numpy.dot(X_train.transpose(),diff) # calculate the gradient
68     G = -G
69     W = W + learning_rate * G # update the parameters
70
71     Y_predict = numpy.dot(X_train,W) # predict under the train set
72     loss_train = numpy.average(numpy.abs(Y_predict-Y_train)) # calculate the absolute differences
73     losses_train.append(loss_train)
```

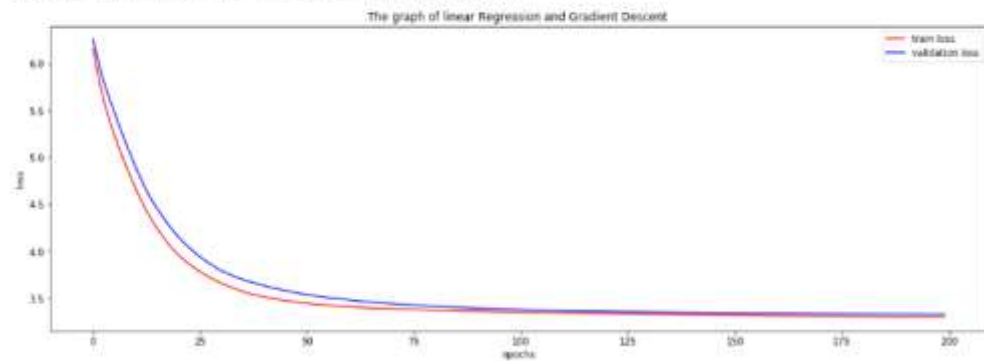
```

81 %matplotlib inline
82 import matplotlib.pyplot as plt
83
84 epoches = range(len(losses_train))
85
86 plt.figure(figsize=(18,8))
87 plt.plot(epoches,losses_train,"-",color="r",label="train loss")
88 plt.plot(epoches,losses_val,"-",color="b",label="validation loss")
89 plt.xlabel("epoches")
90 plt.ylabel("loss")
91 plt.legend()
92 plt.title("The graph of linear Regression and Gradient Descent ")
93
94

```

(253, 13) <class 'numpy.ndarray'>

Out[9]: Text(0.5,1,'The graph of linear Regression and Gradient Descent ')



For linear classification

```

1 #This code Done By:
2 #   Ezzaddin Ahmed Othman Saeed
3 #   Taiz-Yemen
4 #-----
5
6 from sklearn.externals.joblib import Memory
7
8 # STEP 1:
9
10 # Load the experiment data.
11 from sklearn.datasets import load_svmlight_file
12
13 mem = Memory("./nycache")
14
15 mem.cache
16 def get_data():
17     data = load_svmlight_file("./datasets/australian_scale")
18
19     return data
20
21 X, y = get_data()
22 X = X.toarray()
23
24
25 from sklearn.model_selection import train_test_split
26 X_train, X_val, y_train, y_val = train_test_split(X, y, test_size=0.25, random_state=42)

```

```

1 import numpy
2 n_samples_train, n_features_train = X_train.shape
3
4
5 def svm(X_train, y_train, W):
6     g = numpy.ones([n_features_train, 1])
7     for i in range(n_samples_train):
8         X = X_train[i].reshape(1, n_features_train)
9         y = y_train[i].reshape(1, 1)
10        h = 1 - numpy.multiply(y, numpy.dot(X, W))
11        if (h >= 0):
12            g += W * numpy.dot(X.T, y)
13        else:
14            g += W
15
16    W = W - lr * g / n_samples_train
17    return W
18

```

```

1 def svm_loss(X_train, y_train, f, W):
2     n_samples_train, n_features_train = X_train.shape
3     loss = 0
4     for i in range(n_samples_train):
5         X = X_train[i]
6         y = y_train[i]
7         h = 1 - numpy.multiply(y, numpy.dot(W.T, X))
8         if (h >= 0):
9             loss += f * h
10    return loss / n_samples_train + numpy.dot(W.T, W) / 2

```

```

1 f = 0.5
2 #learning rate
3 lr = 0.01
4 losses_train = []
5 losses_val = []
6 total_loop = 100
7 n_samples_train, n_features_train = X_train.shape
8 W = numpy.ones((n_features_train, 1))
9
10 for i in range(total_loop):
11
12     W = svm(X_train, y_train, W)
13     loss = svm_loss(X_train, y_train, f, W)
14     losses_train.append(loss[0][0])
15     loss_val = svm_loss(X_val, y_val, f, W)
16     losses_val.append(loss[0][0])
17

```

```

1 import matplotlib.pyplot as plt
2
3 plt.figure(figsize=(16, 9))
4 plt.plot(losses_train, color="r", label="train loss")
5 plt.plot(losses_val, color="b", label="validation loss")
6 plt.legend()
7 plt.xlabel("epoch")
8 plt.ylabel("loss")
9 plt.title("Linear Classification & Gradient Descent")
10 plt.show()

```


The initialization method of model parameters:

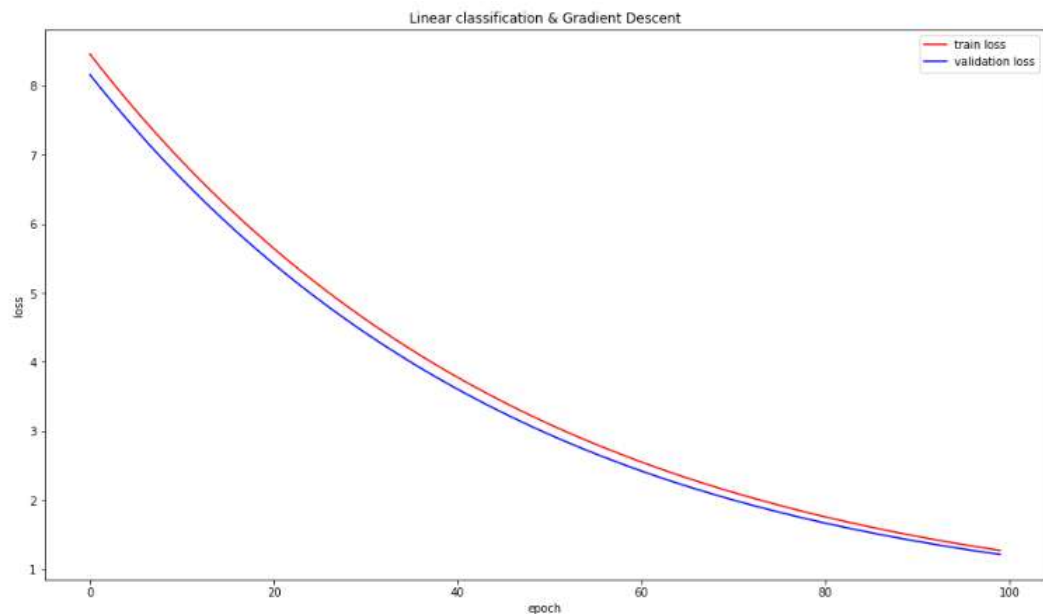
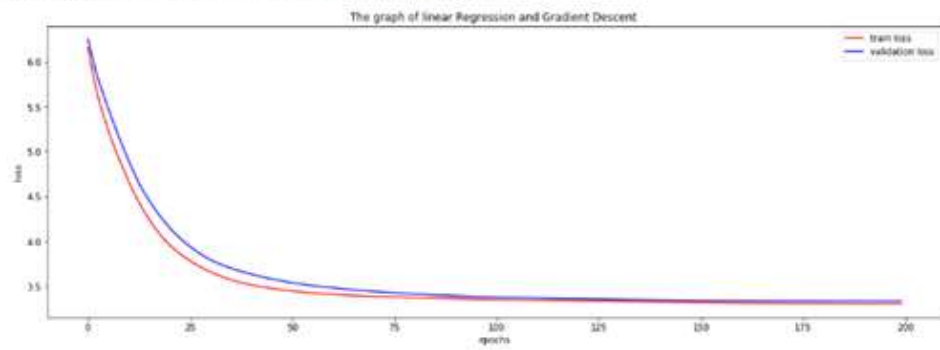
```
50 factor = 0.5
51 learning_rate = 0.0008
52
53
54 ## # STEP 3:
55
56 ##### Initialize linear model parameters #####
57
58 W = numpy.random.normal(0.01,0.1,size=(n_features + 1,1)) # initialize with zero normal distribution
59
60 losses_train = []
61 losses_val = []
62
63 max_loop = 200 ## total iterations - No. Loops=200
64
65 for epoch in range(max_loop):
66     diff = numpy.dot(X_train,W) - Y_train
67     G = factor * W + numpy.dot(X_train.transpose(),diff) # calculate the gradient
68     G = -G
69     W = W + learning_rate * G # update the parameters
70
71     Y_predict = numpy.dot(X_train,W) # predict under the train set
72     loss_train = numpy.average(numpy.abs(Y_predict-Y_train)) # calculate the absolute differences
73     losses_train.append(loss_train)
74
75     Y_predict = numpy.dot(X_validation,W) # predict under the validation set
76     loss_val = numpy.average(numpy.abs(Y_predict-Y_validation)) # calculate the absolute differences
77     losses_val.append(loss_val)
78
79 #####
80
81 %matplotlib inline
82 import matplotlib.pyplot as plt
83
84 epoches = range(len(losses_train))
```

Experimental results and curve:

Hyper-parameter selection (η , epoch, etc.): $\eta = 0.0008$ and 0.01 ,
epoch=200 and 100

Assessment Results (based on selected validation):

Out[9]: Text(0.9,1,"The graph of Linear Regression and Gradient Descent ")



Results analysis:

From the graph its easily understandable that the train curve and the test curve are almost same.

Similarities and differences between linear regression and linear classification:

Type	linear regression	linear classification
type of output	Continuous	discrete
Category	supervised	supervised

Regression is used to predict **continuous values**. Classification is used to predict which class a data point is part of (**discrete value**).

Both regression and classification problems belong to the supervised category of machine learning. In Supervised machine learning, a model or a function is learnt from the data to predict the future data. In simple terms, $y=f(x)$ is a predictive model learnt from the data set $D = \{(X_1, y_1), \dots (X_n, y_2)\}$ where X is the input vector and y is the output.

Based on the type of output y , the learning problems are classified into regression and classification. In case of classification, the output variable is discrete and in regression, the output variable is continuous.

Summary:

In this Report, after apply Experiment, we understand similarity and differences between linear regression and gradient descent through conduct some experiments under small scale dataset. In Experiment 1 we use regression for predicting housing prices in the boston dataset present in the sklearn datasets .