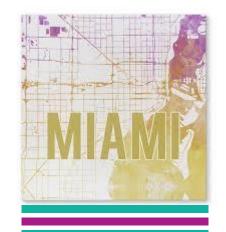


Operations Research (OR)



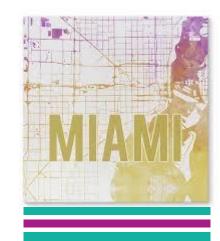
- Many different names (Management Science, Business Analytics, etc.)
- Discipline dealing with the application of advanced analytical methods to help make better decisions
- Typically, there is a quantity that needs to be optimized
- The objective function is a mathematical expression describing the quantity that we want to analyze in terms of key variables
- Goal is to find best value of variables that either maximizes or minimizes the objective function



Models in OR



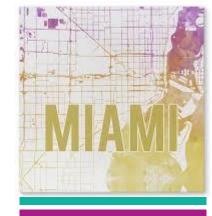
- A model is a mathematical representation of a problem using mathematical relationships involving key variables, the objective function, and constraints
- Two types of OR models
 - Deterministic models assume the relationships of a problem are fully known
 - Stochastic models allow some relationships to contain randomness
- First part of course is focused on deterministic models



Ex: Production of Steel



- Crysteel is a company that makes and sells steel products
- Cost of \$5 to produce one unit and each unit sells for \$20
- Each unit requires 4lbs. of steel and the Crysteel has 100lbs. of steel
- Q: How many units should be produced to maximize the profit?
- Define variables
 - Z = Profit
 - x = Number of units to produce



Ex: Production of Steel



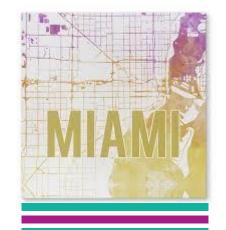


$$Z = \$20x - \$5x$$
Objective Function

Company is limited on production due to finite amount of steel

$$4x \le 100$$
Constraint

• The objective function with the constraint is our OR model



Ex: Production of Steel

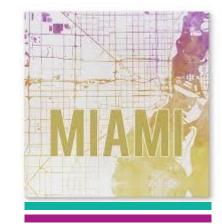




Maximize
$$Z = \$20x - \$5x$$

subject to $4x \le 100$

- We say that 20, 5, and 4 are model parameters
- Remember we are trying to find the "best" value for x
- Graphically, objective function is a straight line that always increases
- Why not just make 100 units? Constraint $4x \le 100 \longrightarrow x \le 25$
- A: Set x=25 (Large as Possible) to maximize profit $Z = \$20 \times 25 \$5 \times 25 = \$375$



Break-Even Analysis

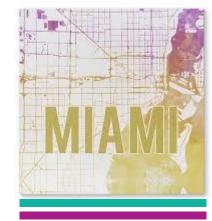


- Q: How many items need to be sold to make \$0 in profit (break even)?
- Typical production involves fixed cost and variable cost
 - Fixed cost (c_f) independent on number of units (x)
 - Variable cost (c_v) dependent of x
- Formula for total cost C

$$C = c_f + c_v x$$

• Updated representation for profit with selling price per unit p

$$Z = px - (c_f + c_v x) = px - c_f - c_v x$$



Break-Even Analysis





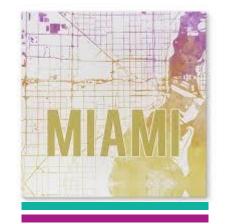
$$0 = px^* - c_f - c_v x^*$$

$$0 = (p - c_v)x^* - c_f$$

$$c_f = (p - c_v)x^* -$$

$$x^* = \frac{c_f}{p - c_v}$$

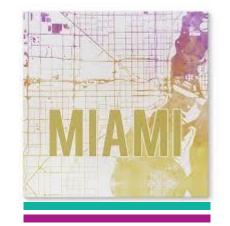
• A: If we sell x^* items, we will make \$0 in profit





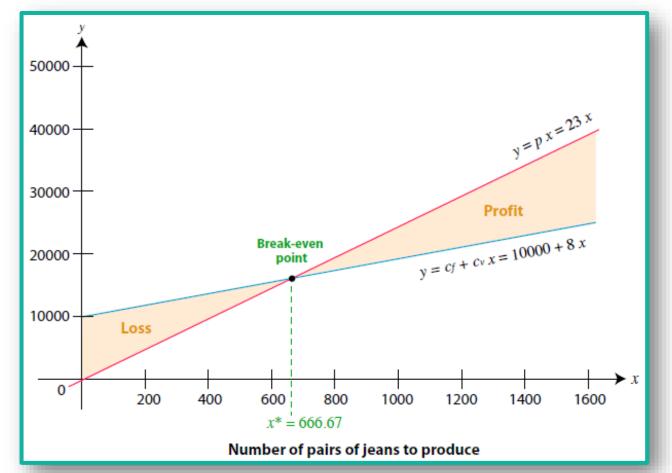
- Jeanealogy creates dope jeans
- They pay \$10,000 to run their factory
- Each pair of jeans costs \$8 to make and sold at \$23
- Q: What is the break-even point in their production?
- Key Variables $x = Number\ of\ Jeans\ Produced$ $c_v = \$8$ $c_f = \$10,000$ p = \$23
- A: Break-even point

$$x^* = \frac{c_f}{p - c_v} = \frac{10,000}{23 - 8} = 666.67 \approx 667$$





Finding the break-even point graphically

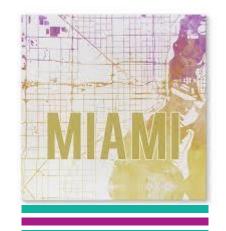


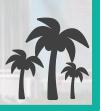




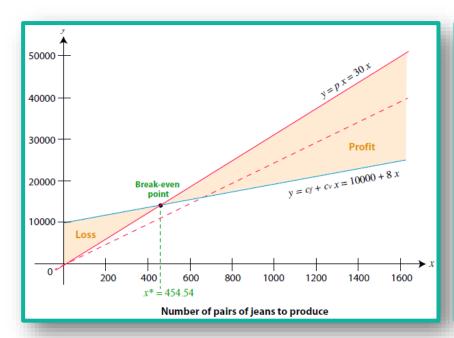
- Sensitivity analysis is seeing how x^* is influenced by parameters c_f , c_v , and p
- Suppose Jeanology improves quality of jeans which now cost \$12 per jeans to produce but can be sold at the insane price of \$30
- Q: How does the break-even point change?

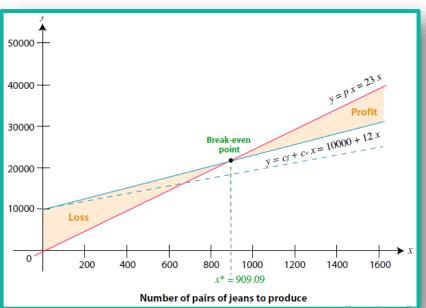
• A:
$$x^* = \frac{c_f}{p - c_v} = \frac{10,000}{30 - 8} = 454.54$$
$$x^* = \frac{c_f}{p - c_v} = \frac{10,000}{23 - 12} = 909.09$$
$$x^* = \frac{c_f}{p - c_v} = \frac{10,000}{30 - 12} = 555.56$$

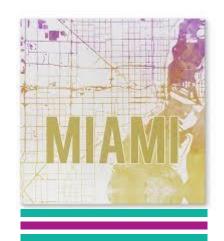




• Graphical sensitivity analysis

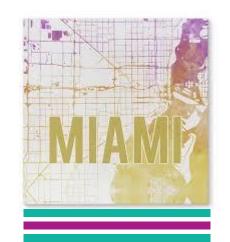






Sensitivity Analysis Motivation

- Business environment is dynamic, and parameters will change over time.
- We need to see where small changes have big effects
- Parameters are often estimated, and the break-even solution is inexact
- Businesses want to know how reliable the solution is and what is the impact of deviations from expectation









The End





