## Assignment # 1 Solutions

due Friday, August 21st, 2020

1 Set  $c_f = $18,000$ ,  $c_v = $0.9$ /piece, p = \$3.2/piece

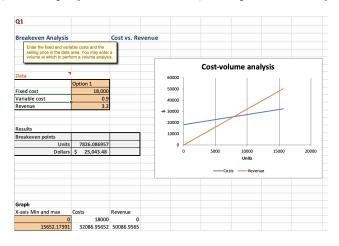
(a) Given x = 12,000

$$TC = c_f + c_v x$$
  
= 18,000 + (0.9)(12,000) = \$28,800  
 $TR = px$   
= (3.2)(12,000) = \$38,400  
 $Profit = TR - TC$   
= 38,400 - 28,800 = \$9,600

(b) To break even, solve  $px - (c_f + c_v x) = 0$  for x.

$$x = \frac{c_f}{p - c_v} = \frac{18,000}{3.2 - 0.9} \approx 7,827$$
 cupcakes.

To break even, the company should sell about 7,827 cupcakes annually.



- (c) The break-even volume as a percentage of capacity is  $\frac{7827}{12000} \approx 0.6522 = 65.23\%$
- **2** Set  $c_f = \$4,000, c_v = \$0.21/\text{pound}.$

Case 1:  $p_1 = \$0.75/\text{pound}, x_1 = 9,000.$ 

$$TC_1 = c_f + c_v x_1$$

$$= 4,000 + (0.21)(9000) = \$5,890$$

$$TR_1 = p_1 x_1$$

$$= (0.75)(9000) = \$6,750$$

$$Profit_1 = TR_1 - TC_1$$

$$= 6,750 - 5,890 = \$860$$

Case 2:  $p_2 = \$0.95/\text{pound}, x_2 = 5,700.$ 

$$TC_2 = c_f + c_v x_2$$

$$= 4,000 + (0.21)(5700) = \$5,197$$

$$TR_2 = p_1 x_1$$

$$= (0.95)(5700) = \$5,415$$

$$Profit_2 = TR_2 - TC_2$$

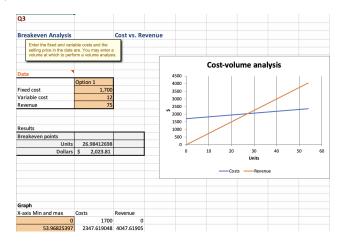
$$= 5,415 - 5,197 = \$218$$

Since  $Profit_2 < Profit_1$ , the dairy should not raise the price.

- **3** Set  $c_f = \$1,700, c_v = 7 + 5 = \$12/\text{student}, p = \$75/\text{student}$
- (a) To break even, solve  $px (c_f + c_v x) = 0$  for x.

$$x = \frac{c_f}{p - c_v} = \frac{1,700}{75 - 12} \approx 27$$
 students.

To break even, 27 students need to enroll in Hannah and Kathleen's class.



(b) Given  $c_f = \$1,700$ ,  $c_v = 7 + 5 = \$12/\text{student}$ , p = \$75/student, solve  $5,000 = px - (c_f + c_v x)$  for x.

$$x = \frac{5000 + c_f}{p - c_v} = \frac{6,700}{75 - 12} \approx 107$$
 students.

(c) If x = 60,  $c_f = \$1,700$ ,  $c_v = 7 + 5 = \$12/\text{student}$ , solve  $5,000 = px - (c_f + c_v x)$  for p.

$$p = \frac{5000 + c_f + c_v x}{x} = \frac{7,420}{60} \approx \$123.67$$

They need to charge \$123.67/student.

4

Let

 $x_1 =$  amount of oats include in each cereal box

 $x_2 = \text{amount of rice include in each cereal box}$ 

The model is as follows:

$$\min z = 0.05x_1 + 0.03x_2$$
s.t.  $8x_1 + 6x_2 \ge 48$ 

$$x_1 + 2x_2 \ge 12$$

$$x_i > 0, \quad \forall i = 1, 2.$$

## 5 Let

 $x_1$  = number of chairs produced each day.

 $x_2$  = number of tables produced each day.

The model is as follows:

$$\max z = 400x_1 + 100x_2$$
s.t.  $8x_1 + 10x_2 \le 80$ 
 $2x_1 + 6x_2 \le 36$ 
 $x_1 \le 6$ 
 $x_i \ge 0, \quad \forall i = 1, 2.$