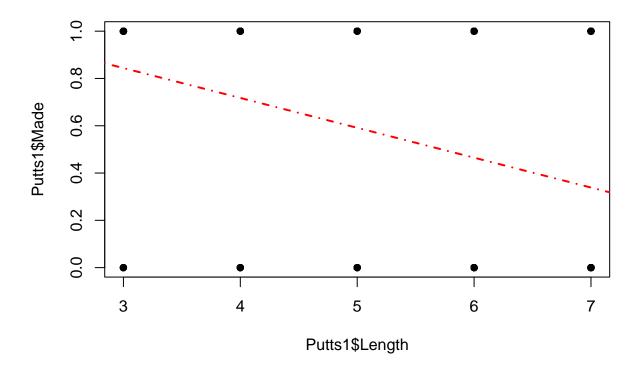
# Supplement for Lecture 27: Logistic Regression

#### Load Data

```
#Load and Preview Data
data(Putts1)
head(Putts1)
    Length Made
## 1
         3
## 2
         3
              1
## 3
         3 1
         3 1
## 5
         3
              1
## 6
#Inspect Data
nrow(Putts1)
## [1] 587
table(Putts1$Made,Putts1$Length)
##
##
       3 4 5 6 7
    0 17 31 47 64 90
##
  1 84 88 61 61 44
```

### Plot of Raw Data

```
plot(Putts1$Length,Putts1$Made,pch=16)
abline(lm(Made~Length,data=Putts1),lty=4,lwd=2,col="red")
```



#### Plot of Summarized Data

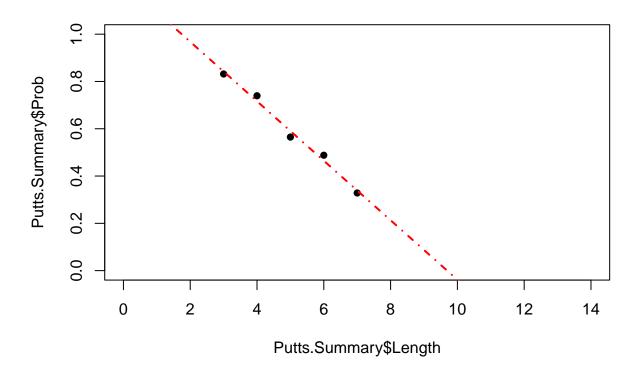
```
tapply(Putts1$Made,Putts1$Length,FUN=mean)

## 3 4 5 6 7

## 0.8316832 0.7394958 0.5648148 0.4880000 0.3283582

Putts.Summary=data.frame(Length=3:7,Prob=tapply(Putts1$Made,Putts1$Length,FUN=mean))

plot(Putts.Summary$Length,Putts.Summary$Prob,pch=16,ylim=c(0,1),xlim=c(0,14))
abline(lm(Prob~Length,data=Putts.Summary),lty=4,lwd=2,col="red")
```



## Logistic Regression Model

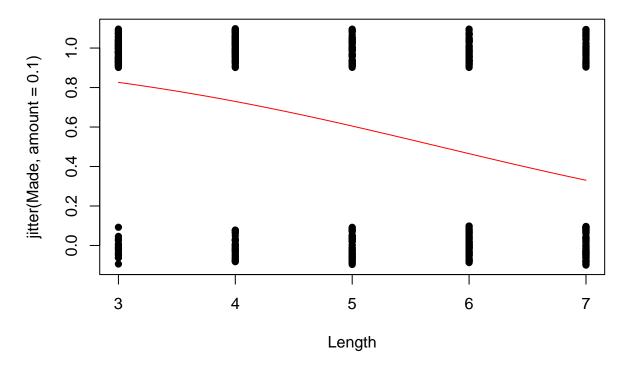
```
putt.mod = glm(Made~Length, family=binomial, data=Putts1)
summary(putt.mod)
##
## Call:
## glm(formula = Made ~ Length, family = binomial, data = Putts1)
##
## Deviance Residuals:
##
       Min
                 10
                      Median
                                   3Q
                                           Max
##
  -1.8705 -1.1186
                      0.6181
                               1.0026
                                        1.4882
##
## Coefficients:
##
               Estimate Std. Error z value
                                                      Pr(>|z|)
                           0.36893
                                     8.828 < 0.0000000000000000 ***
## (Intercept) 3.25684
## Length
               -0.56614
                           0.06747 -8.391 <0.0000000000000000 ***
##
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
  (Dispersion parameter for binomial family taken to be 1)
##
##
##
       Null deviance: 800.21 on 586 degrees of freedom
## Residual deviance: 719.89 on 585 degrees of freedom
## AIC: 723.89
```

```
##
## Number of Fisher Scoring iterations: 4
```

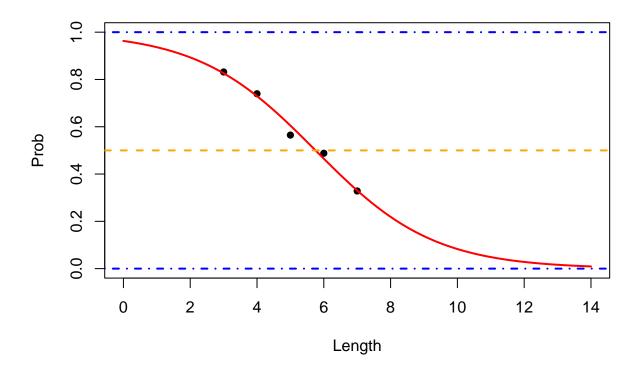
# Visualization of Logistic Regression Model

```
b0 = as.numeric(coef(putt.mod)[1])
b1 = as.numeric(coef(putt.mod)[2])

plot(jitter(Made,amount=0.1)~Length,data=Putts1,pch=16)
curve(exp(b0+b1*x)/(1+exp(b0+b1*x)),col="red",add=TRUE)
```



```
plot(Prob~Length,data=Putts.Summary,pch=16,ylim=c(0,1),xlim=c(0,14))
curve(exp(b0+b1*x)/(1+exp(b0+b1*x)),col="red",lwd=2,add=TRUE)
abline(h=c(0,1),lwd=2,col="blue",lty=4)
abline(h=0.5,lwd=2, col="orange",lty=2)
```



### Comparing Sample Proportions to Estimated Probabilities

```
prop=as.numeric(tapply(Putts1$Made,Putts1$Length,FUN=mean))
prob=as.numeric(predict(putt.mod,type="response",newdata=data.frame(Length=3:7)))
OUT = data.frame(Length=3:7,Proportion = prop, Probability=prob)
OUT
     Length Proportion Probability
##
          3 0.8316832
                         0.8261256
## 1
## 2
          4 0.7394958
                         0.7295364
## 3
          5 0.5648148
                         0.6049492
          6 0.4880000
## 4
                         0.4650541
## 5
          7 0.3283582
                         0.3304493
```

#### Odds

```
#Calculate using Formula

OUT$Odds = OUT$Probability/(1-OUT$Probability)

OUT

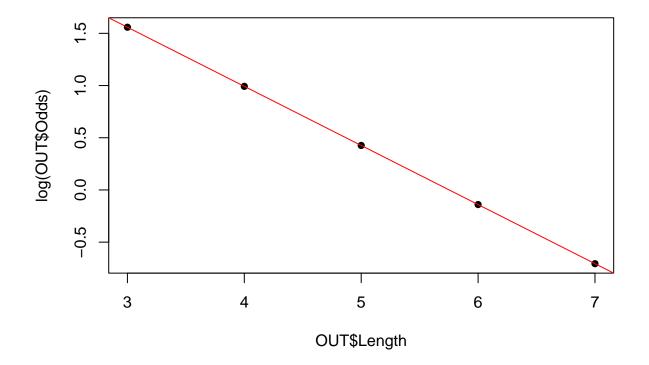
## Length Proportion Probability Odds

## 1 3 0.8316832 0.8261256 4.751277

## 2 4 0.7394958 0.7295364 2.697355

## 3 5 0.5648148 0.6049492 1.531320
```

```
## 4
           0.4880000
                         0.4650541 0.869348
## 5
         7
            0.3283582
                         0.3304493 0.493539
#Calculate using Predict Function
exp(predict(putt.mod, newdata=data.frame(Length=3:7)))
##
                   2
                            3
## 4.751277 2.697355 1.531320 0.869348 0.493539
#Plot log(odds) vs Length
plot(x=0UT$Length,y=log(OUT$0dds),pch=16)
abline(a=b0,b=b1,col="red")
```



#### **Odds Ratios**

```
#Compare 3ft Putts to 7ft Putts
exp(b0+b1*3)/exp(b0+b1*7)

## [1] 9.626953
#Compare 7ft Putts to 3ft Putts (Reciprocal)
exp(b0+b1*7)/exp(b0+b1*3)
```

## [1] 0.103875

Interpretation: The odds of making a 3ft putt is 9.63 times the odds of making a 7ft putt. This is equivalent to saying the odds of making a 7ft putt is 0.10 times the odds of making a 3ft putt. Typically, statisticians prefer interpreting odds >1 which requires putting the group with the higher chance of success in the numerator.

### Relationship to Slope of Line

```
\# Compare\ 4ft\ Putts\ to\ 3ft\ Putts
\exp(b0+b1*4)/\exp(b0+b1*3)
## [1] 0.5677116
#Compare 7ft Putts to 6ft Putts
\exp(b0+b1*7)/\exp(b0+b1*6)
## [1] 0.5677116
#Calculate Slope From Odds Ratio
log(0.5677116)
## [1] -0.5661417
b1
## [1] -0.5661417
#Notice the difference here
exp(b0+b1*7)
## [1] 0.493539
\exp(b0+b1*6)*\exp(b1)
## [1] 0.493539
Notice: For every one unit increase in X, the odds of success increases by a factor of e^b1
\# Empirical\ Logit\ Plot
OUT$EmpiricalLogit = log(OUT$Proportion/(1-OUT$Proportion))
plot(x=0UT$Length,y=0UT$EmpiricalLogit,pch=16)
```

