

READING:	1.1
EXERCISES:	CH.1: 1,5-8, 15, 17, 19
ASSIGNED:	HW 1
PRODUCER:	DR. MARIO

[illegible]

# Prerequisites for the Model

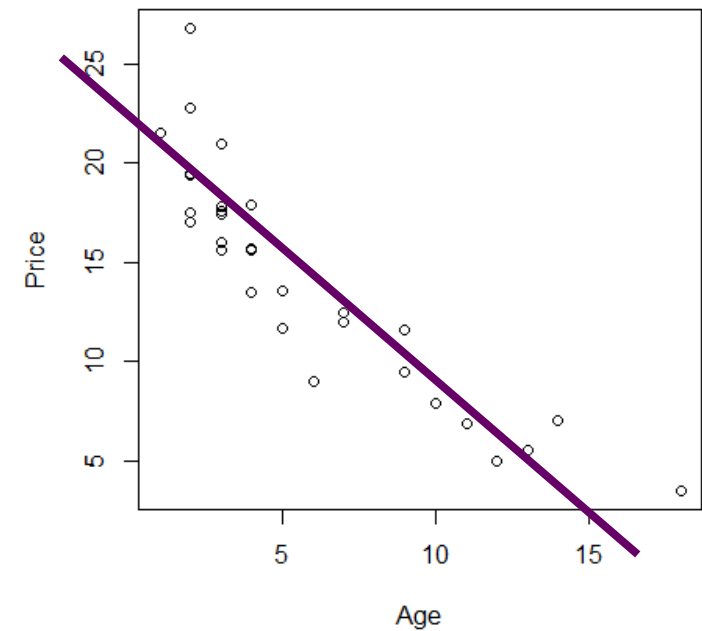
1. Single Quantitative Response Variable  $Y$
2. Single Quantitative Predictor Variable  $X$
3. Scatterplot of  $Y$  versus  $X$  (Book Does Side-by-Side Boxplots)
4. Evidence that a **Straight Line** is Reasonable for Modeling the Relationship between  $Y$  and  $X$

# Example: Honda Accords

- Question: *Is there a linear relationship between the **age** of an Accord and the **price** of an Accord?*
- Both Variables are Quantitative
- Which One is Response?
- Scatter Plot of *price versus age* or *price on age* Shows Evidence of a **Linear** Relationship

# Example: Honda Accord Price

```
library(Stat2Data) #Package for Textbook  
library(mosaic)  
  
data("AccordPrice") #Puts dataset into Global Environment  
  
plot(Price~Age,data=AccordPrice)
```



# Simple Linear Regression Model

- General Form

$$Y = f(X) + \epsilon$$

$$= \boxed{\mu_Y} + \epsilon$$

Mean of Y Given X or  $E[Y|X]$

- Simple Linear Regression

$$Y = \boxed{\beta_0 + \beta_1 X} + \epsilon$$

- Shape Depends on y-Intercept  $\beta_0$  and Slope  $\beta_1$

# Fitting Model to Data

- Fitted (Estimated) Model

$$\hat{Y} = \hat{\beta}_0 + \hat{\beta}_1 X$$

- Residual for  $i^{\text{th}}$  Car

$$\hat{\epsilon}_i = Y_i - \hat{Y}_i = Y_i - (\hat{\beta}_0 + \hat{\beta}_1 X)$$

- Sum of Squared Errors (SSE)

$$\sum \hat{\epsilon}_i^2 = \sum (\hat{Y}_i - Y_i)^2$$

# Fitting Model to Data

- Least Squares Regression: *Choose Estimates  $\hat{\beta}_0$  and  $\hat{\beta}_1$  such that SSE is as small as possible*

$$\hat{Y} = \hat{\beta}_0 + \hat{\beta}_1 X$$

- Interpretation of  $\hat{Y}$ : **Expected** value or **predicted** value of  $Y$  given a known value for  $X$
- Interpretation of  $\hat{\beta}_0$ : *The predicted value of  $Y$  given that  $X=0$*
- Interpretation of  $\hat{\beta}_1$ : *The amount by which our expected value of  $Y$  would **change** if we **increase**  $X$  by **1 unit***

# Centering Data

- Suppose we replace our Predictor  $X$  with  $X - \bar{x}$

- Notice

$$\begin{aligned} Y &= \beta_0 + \beta_1(X - \bar{x}) + \epsilon \\ &= \beta_0 + \beta_1 X - \beta_1 \bar{x} + \epsilon \\ &= (\beta_0 - \beta_1 \bar{x}) + \beta_1 X + \epsilon \\ &= \beta_0^* + \beta_1 X + \epsilon \end{aligned}$$

Slope Is Unaffected

Y-intercept Will Change



## *Make Reasonable Decisions*

