



Football VII

Produced by Dr. Mario | UNC STOR 538





NFL Overtime

- Occurs in the Situation of a Tied Game
- Coin Toss Winner Has Two Choices
- Choice 1: Kickoff
- Choice 2: Receive
- Overtime is Sudden Death
- If No Team Wins in Overtime, Game Results in a Tie
- Receiving Team Wins 60% of the Time (1994-2006)
- Proposed Moving Kickoff to Make it Harder for Receiving Team

It is better to receive, than to give.

- Mahatma Mario







- *Mathematical Model of Sudden Death Overtime
 - \clubsuit Let p = Probability Average NFL Team Scores in a Possession
 - Assumption: Each Team Has Identical Probability of Scoring
 - Ties Happen Less Than 5% of the Time
 - Assumption: Game Will Endure Forever
 - \clubsuit Let K = Probability Team Receiving Wins the Game
- Two Ways Receiving Team Wins
 - *Receiving Team Scores on First Possessions

 $P(Win \ on \ First \ Possession) = p$

Receiving Team Fails to Score But Scores on Later Possession

 $P(Win \ on \ Second \ Possession) = (1-p)(1-p)K$

Assume Independence







Based on Previous Statements

$$K = p + (1 - p)(1 - p)K$$
 Is This Nonsense?

$$K = \frac{p}{1 - (1 - p)(1 - p)} = \frac{p}{2p - p^2} = \frac{p}{p(-p + 2)} = \frac{1}{2 - p}$$









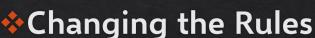


- Checking Mathematics Empirically
 - Using NFL Data (2003-2006)

$$p = 31\%$$

Therefore, the Probability Receiving Team Wins in Overtime

$$K = \frac{1}{2 - 0.31} = 0.59 \approx 60\%$$



- ♦ In 2012, NFL Modified Overtime Rules
- Receiving Team Needs a Touchdown to Win the Game
- Since then 52.7% of Coin Toss Winners, Win the Game







Modified Mathematics

- \clubsuit Let p = Probability Average NFL Team Scores in a Possession
- \clubsuit Let q = Probability Average NFL Team Scores a Touchdown in a Possession
- Probability Receiving Team Wins on First Possession

$$P(Win \ on \ First \ Possession) = q$$

Probability Receiving Team Wins on Second Possession

$$P(Win \ on \ Second \ Possession) = (1-q)(1-p)K$$

Now, Based on Mathematics

$$K = q + (1 - q)(1 - p)K$$
 $K = \frac{q}{1 - (1 - q)(1 - p)}$

• Based on 2019, q = 22.4% and p = 36.4%

$$K = \frac{0.224}{1 - (1 - 0.224)(1 - 0.364)} = 44.23\%$$
 — Math is Dope





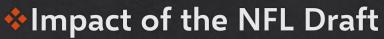












- NFL is Considered to Be the Fairest League in the Land
- Teams Draft in Inverse Order From Browns to Best
- There are 8 Rounds in the NFL Draft
- 6.1 Million People Watch on Average
- 100,000 People Attend on Average
- Early Draft Picks are Believed to Be More Valuable Than Late Draft Picks

Research by Cade Massey and Richard Thaler

- Article Called The Loser's Curse
- Collected Data on All Draft Day Trades From Recent Years
- ***** Define v(n) = Value of the nth Pick
- Not About the Player But About the Position
- Suppose Team Traded 12th and 28th Pick for 4th Pick

$$v(12) + v(28) = v(4)$$





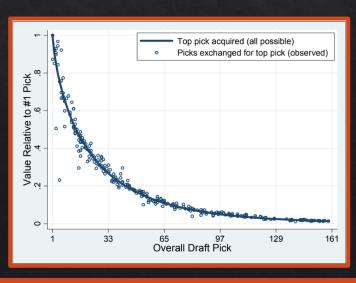


- Model for Value
 - Used Exponential Function

$$v(n) = e^{-a(n-1)^b}$$

- Based on Weibull Distribution
- Estimated Parameters a and b Based on Data From Trades
- Trades Can Be Used to Identify the Perceived Value of the Picks
- **♦** Final Estimates: *a = -0.148* & *b=0.7*









- Determining Value of Player According to On-Field Impact
 - **♦** Not on Roster
 - **♦** No Starts
 - 1-8 Starts
 - **♦**9-16 Starts
 - Pro-Baller



Mean Salary	Performance Level
\$ —	not on roster
\$ 1,039,870	no starts
\$ 1,129,260	1 to 8 starts
\$ 4,525,227	>8 starts
\$ 9,208,248	Pro Bowl

Salary of Quarterbacks

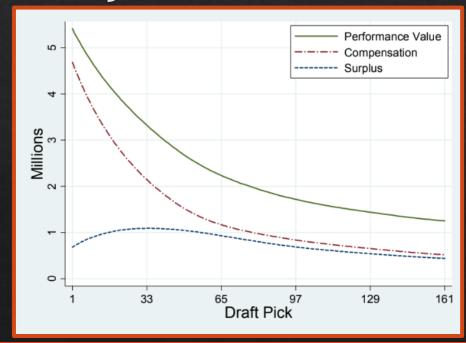






- Examination of Surplus
 - Drafted NFL Players are Paid According to Draft Position
 - Determined By Player Value Minus Average Player Salary
 - Discovered Average Surplus By Draft Position Increased
 - Meaning Later Picks Contributed More Value









- Critique's by Phil Birnbaum
 - Well-known in Sabermetrics
 - Major Flaw: Assumption Players Who Play the Same Position and Are in the Same Performance Category are Equally Valuable
 - Example: Quarterback with 1 Game Equivalent to QB with 8 Games
 - Need Better Measure of Player Performance Than Usage in Starts
- Using Combine 40-YD Dash to Predict Running Back Performance
 - Important to Identify Good Draft Picks
 - Analysis Done by Bill Barnwell
 - 40-YD Dash Time Negatively Correlated With YDs Gained and Carries (-0.36)
 - When Would a Slower Runner Be Better Than Faster Runner?







- Adjustment for Weight
 - Thanks Bill Barnwell

weight-adjusted 40-yard dash score =
$$\frac{200 \times \text{weight in pounds}}{(40 \text{ yard time in seconds})^4}$$



- New Measure Has a 0.45 Correlation with Yards and Carries
- Accounts for Data from 1999 to 2008
- Calibrated to Average Out to 100 Across All Running Backs
- Any Other Criticism's of Value Model by Massey and Thaler?





The Winner's Curse

- Look for Reasons of the Draft's Inefficiency
- Winner's of Auctions Pay More Than the Object is Worth
- Surplus Analysis Shows Picks Below #43 are at a Disadvantage
- Because of Trades, Teams are Bidding on Picks
- In What Other Ways are Winner's Cursed?





Final Inspiration

If you're not first, be last.

- Mahatma Mario