
Algorithm 1: 数值微分法 (DDA)

Input: 直线 L 两端点坐标 $P_0(x_0, y_0), P_1(x_1, y_1)$, 画线颜色 $color$

```
1  $\Delta x \leftarrow x_1 - x_0, \Delta y \leftarrow y_1 - y_0;$   
2  $steps \leftarrow \max(|\Delta x|, |\Delta y|);$   
3  $dx \leftarrow \frac{\Delta x}{steps}, dy \leftarrow \frac{\Delta y}{steps};$   
4  $P \leftarrow P_0;$   
5 for  $i \leftarrow 1$  to  $steps + 1$  do  
6   |   putpixel (round( $P$ ),  $color$ );  
7   |    $P \leftarrow P + (dx, dy);$   
8 end
```

Algorithm 2: 中点画线法

Input: 直线 L 两端点坐标 $P_0(x_0, y_0), P_1(x_1, y_1)$, 画线颜色 $color$

```
1 if  $x_0 > x_1$  then
2   |   swap ( $P_0, P_1$ );
3 end
4  $a \leftarrow y_0 - y_1, b \leftarrow x_1 - x_0, c \leftarrow x_0 y_1 - x_1 y_0$ ;
5  $P_i \leftarrow P_0$ ;
6 if  $k \in [0, 1]$  then
7   |    $d \leftarrow 2a + b$ ;
8   |    $\Delta P_L \leftarrow (1, 1), \Delta d_L \leftarrow 2(a + b)$ ;
9   |    $\Delta P_G \leftarrow (1, 0), \Delta d_G \leftarrow 2a$ ;
10 else if  $k \in (1, +\infty)$  then
11   |    $d \leftarrow a + 2b$ ;
12   |    $\Delta P_L \leftarrow (0, 1), \Delta d_L \leftarrow 2b$ ;
13   |    $\Delta P_G \leftarrow (1, 1), \Delta d_G \leftarrow 2(a + b)$ ;
14 else if  $k \in [-1, 0)$  then
15   |    $d \leftarrow 2a - b$ ;
16   |    $\Delta P_L \leftarrow (1, 0), \Delta d_L \leftarrow 2a$ ;
17   |    $\Delta P_G \leftarrow (1, -1), \Delta d_G \leftarrow 2(a - b)$ ;
18 else
19   |    $d \leftarrow a - 2b$ ;
20   |    $\Delta P_L \leftarrow (1, -1), \Delta d_L \leftarrow 2(a - b)$ ;
21   |    $\Delta P_G \leftarrow (0, -1), \Delta d_G \leftarrow -2b$ ;
22 end
23 while  $P \neq P_1$  do
24   |   putpixel ( $P$ ,  $color$ );
25   |   if  $d < 0$  then
26   |     |    $P \leftarrow P + \Delta P_L, d \leftarrow d + \Delta d_L$ ;
27   |   else
28   |     |    $P \leftarrow P + \Delta P_G, d \leftarrow d + \Delta d_G$ ;
29   |   end
30 end
31 putpixel ( $P_1$ ,  $color$ );
```

Algorithm 3: Bresenham 画线法

Input: 直线 L 两端点坐标 $P_0(x_0, y_0), P_1(x_1, y_1)$, 画线颜色 $color$

```
1 if  $x_0 > x_1$  then
2   | swap ( $P_0, P_1$ );
3 end
4  $\Delta x = x_1 - x_0, \Delta y = y_1 - y_0$ ;
5  $P_i \leftarrow P_0$ ;
6 if  $k \in [0, 1]$  then
7   |  $d \leftarrow 2\Delta y - \Delta x$ ;
8   |  $\Delta P_L \leftarrow (1, 0), \Delta d_L \leftarrow 2\Delta y$ ;
9   |  $\Delta P_G \leftarrow (1, 1), \Delta d_G \leftarrow 2(\Delta y - \Delta x)$ ;
10 else if  $k \in (1, +\infty)$  then
11   |  $d \leftarrow 2\Delta x - \Delta y$ ;
12   |  $\Delta P_L \leftarrow (0, 1), \Delta d_L \leftarrow 2\Delta x$ ;
13   |  $\Delta P_G \leftarrow (1, 1), \Delta d_G \leftarrow 2(\Delta x - \Delta y)$ ;
14 else if  $k \in [-1, 0)$  then
15   |  $d \leftarrow -2\Delta y - \Delta x$ ;
16   |  $\Delta P_L \leftarrow (1, 0), \Delta d_L \leftarrow -2\Delta y$ ;
17   |  $\Delta P_G \leftarrow (1, -1), \Delta d_G \leftarrow -2(\Delta y + \Delta x)$ ;
18 else
19   |  $d \leftarrow 2\Delta x + \Delta y$ ;
20   |  $\Delta P_L \leftarrow (0, -1), \Delta d_L \leftarrow 2\Delta x$ ;
21   |  $\Delta P_G \leftarrow (1, -1), \Delta d_G \leftarrow 2(\Delta x + \Delta y)$ ;
22 end
23 while  $P \neq P_1$  do
24   | putpixel ( $P$ ,  $color$ );
25   | if  $d < 0$  then
26     |  $P \leftarrow P + \Delta P_L, d \leftarrow d + \Delta d_L$ ;
27   | else
28     |  $P \leftarrow P + \Delta P_G, d \leftarrow d + \Delta d_G$ ;
29   | end
30 end
31 putpixel ( $P_1$ ,  $color$ );
```

Algorithm 4: 中点画圆法

Input: 圆 C 圆心 $C(x, y)$, 半径 R , 画线颜色 $color$

```
1  $P_1 \leftarrow (0, R)$ ;  
2  $d_1 \leftarrow 1 - R$ ;  
3  $i \leftarrow 1$ ;  
4 while  $P_i \neq (\frac{R}{\sqrt{2}}, \frac{R}{\sqrt{2}})$  do  
5   DrawCirclePoints ( $P_i$ , color);  
6   if  $d < 0$  then  
7      $P_{i+1} \leftarrow (x_i + 1, y_i), d_{i+1} \leftarrow d_i + 2x_i + 3$ ;  
8   else  
9      $P_{i+1} \leftarrow (x_i + 1, y_i - 1), d_{i+1} \leftarrow d_i + 2(x_i - y_i) + 5$ ;  
10  end  
11   $i \leftarrow i + 1$ ;  
12 end  
13 DrawCirclePoints ( $P_i$ , color);
```

Algorithm 5: Bresenham 画圆法

Input: 圆 C 圆心 $C(x, y)$, 半径 R , 画线颜色 $color$

```
1  $P_1 \leftarrow (0, R)$ ;  
2  $d_1 \leftarrow 2(1 - R)$ ;  
3  $i \leftarrow 1$ ;  
4 while  $P_i \neq (\frac{R}{\sqrt{2}}, \frac{R}{\sqrt{2}})$  do  
5   DrawCirclePoints ( $P_i$ , color);  
6   if  $d < 0 \ \& \ 2(d + y) - 1 \leq 0$  then  
7      $P_{i+1} \leftarrow (x_i + 1, y_i), d_{i+1} \leftarrow d_i + 2x_i + 3$ ;  
8   else  
9      $P_{i+1} \leftarrow (x_i + 1, y_i - 1), d_{i+1} \leftarrow d_i + 2(x_i - y_i + 3)$ ;  
10  end  
11   $i \leftarrow i + 1$ ;  
12 end  
13 DrawCirclePoints ( $P_i$ , color);
```

Algorithm 6: 多边形逼近画圆法

Input: 圆 C 圆心 $C(x, y)$, 半径 R , 画线颜色 $color$

```
1  $n \leftarrow 3\sqrt{R}$ ;  
2  $\theta \leftarrow \frac{2\pi}{n}$ ;  
3  $P_1 \leftarrow (0, R)$ ;  
4  $i \leftarrow 2$ ;  
5 while  $i \leq n$  do  
6    $P_i = (x_{i-1} \cos \theta - y_{i-1} \sin \theta, y_{i-1} \cos \theta + x_{i-1} \sin \theta)$ ;  
7   DrawLine ( $P_{i-1}, P_i$ , color);  
8    $i \leftarrow i + 1$ ;  
9 end  
10 DrawLine ( $P_n, P_1$ , color);
```

Algorithm 7: 任意角度画弧法

Input: 圆弧 \widehat{SE} 所属圆的圆心 $C(x_c, y_c)$, 圆弧起点 $S(x_s, y_s)$, 圆弧终点方位点 $E_{pos}(x_{epos}, y_{epos})$, 画线颜色 $color$

// 求得平移到原点的圆其对应圆心、起点、终点方位点和实际终点

```
1  $C' \leftarrow (0, 0), S' \leftarrow (x_s - x_c, y_s - y_c);$ 
2  $E'_{pos} \leftarrow (x_{epos} - x_c, y_{epos} - y_c), E' \leftarrow C'E'_{pos} \cap \odot C';$ 
   // 确定起点和终点所属区域或界点
3  $region_s = \text{GetRegion}(S), region_e = \text{GetRegion}(E);$ 
   // 划分完全绘制区域、部分绘制区域和非绘制区域
4 Fill (state, 0);
5 if  $region_s = K_i$  &  $region_e = K_j$  then
6   for  $R = R_i \rightarrow R_{j-1}$  do
7     state[R]  $\leftarrow$  1;
8   end
9 else if  $region_s = K_i$  &  $region_e = R_j$  then
10  for  $R = R_i \rightarrow R_{j-1}$  do
11    state[R] = 1;
12  end
13   $MN \leftarrow (\min(x_{K_j}, x_E), \min(y_{K_j}, y_E)), MX \leftarrow (\max(x_{K_j}, x_E), \max(y_{K_j}, y_E));$ 
14   $Rect \leftarrow (MN, MX), \text{state}[region_e] \leftarrow -1;$ 
15 else if  $region_s = R_i$  &  $region_e = K_j$  then
16  for  $R = R_{i+1} \rightarrow R_j$  do
17    state[R] = 1;
18  end
19   $MN \leftarrow (\min(x_{K_{i+1}}, x_S), \min(y_{K_{i+1}}, y_S)), MX \leftarrow (\max(x_{K_{i+1}}, x_S), \max(y_{K_{i+1}}, y_S));$ 
20   $Rect \leftarrow (MN, MX), \text{state}[region_s] \leftarrow -1;$ 
21 else
22  for  $R = R_{i+1} \rightarrow R_{j-1}$  do
23    state[R] = 1;
24  end
25  if  $S, E$  属于同一象限 &  $S$  在  $E$  顺时针侧 then
26     $MN \leftarrow (\min(x_S, x_E), \min(y_S, y_E)), MX \leftarrow (\max(x_S, x_E), \max(y_S, y_E));$ 
27     $Rect \leftarrow (MN, MX);$ 
28  else
29     $MN_1 \leftarrow (\min(x_{K_j}, x_E), \min(y_{K_j}, y_E)), MX_1 \leftarrow (\max(x_{K_j}, x_E), \max(y_{K_j}, y_E));$ 
30     $MN_2 \leftarrow (\min(x_{K_{i+1}}, x_S), \min(y_{K_{i+1}}, y_S)), MX_2 \leftarrow (\max(x_{K_{i+1}}, x_S), \max(y_{K_{i+1}}, y_S));$ 
31     $Rect \leftarrow (MN_1, MX_2) \cup (MN_2, MX_2);$ 
32  end
33  state[region_s]  $\leftarrow$  -1, state[region_e]  $\leftarrow$  -1;
34 end
   // 八方对称遍历圆像素点, 每次生成的像素点需要判断是否在绘制区域内
35 DrawCircleOfArc( $C, R, color, state, Rect$ );
```
