

3. Ann. $\text{app}(\text{rev } l_1) l_2 = \text{app_rev } l_1 l_2$ gilt für alle Listen l_1, l_2 .

Wir zeigen dies über die Länge der Liste l_1 .

3. Anf. $\text{app}(\text{rev } []) l_2 \stackrel{\text{Def.}}{=} \text{app } [] l_2 \stackrel{\text{Def.}}{=} l_2 \stackrel{\text{Def.}}{=} \text{app_rev } [] l_2$

3. Schritt: $l_1 = xS \Rightarrow l_1 = x :: xS$

3. Schluss: $\text{app}(\text{rev } (x :: xS)) l_2 \stackrel{\text{Def.}}{=} \text{app}(\text{app } (\text{rev } xS) [x]) l_2$

$\stackrel{(1)}{=} \text{app } (\text{rev } xS) (\text{app } [x] l_2) \stackrel{\text{Def.}}{=} \text{app } (\text{rev } xS) (x :: \text{app } [] l_2)$

$\stackrel{\text{Def.}}{=} \text{app } (\text{rev } xS) (x :: l_2) \stackrel{3. \text{ Ann.}}{=} \text{app_rev } xS (x :: l_2)$

$\stackrel{\text{Def.}}{=} \text{app_rev } (x :: xS) l_2$

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