

Python code for 8-puzzle A* implementation, to calculate, $f(n)$, considering:

$g(n)$: Depth of the node, $h(n)$: Number of Misplaced tiles

```
import heapq
```

```
class PuzzleState:
```

```
    def __init__(self, state, empty_tile_pos, g, h, path, level):
```

```
        self.state = state
```

```
        self.empty_tile_pos = empty_tile_pos # (row, col)
```

```
        self.g = g # Cost from start to current state
```

```
        self.h = h # Heuristic cost to goal
```

```
        self.f = g + h # Total cost
```

```
        self.path = path # Path taken to reach this state
```

```
        self.level = level # Depth level in the state space
```

```
    def __lt__(self, other):
```

```
        return self.f < other.f # Priority queue comparison based on f value
```

```
def astar_misplaced_tiles(start_state, goal_state):
```

```
    directions = {
```

```
        (-1, 0): 'Up',
```

```
        (1, 0): 'Down',
```

```
        (0, -1): 'Left',
```

```
        (0, 1): 'Right'
```

```
    }
```

```
def calculate_heuristic(state):
```

```
    h = 0
```

```
    for i in range(3):
```

```
        for j in range(3):
```

```
            if state[i][j] != goal_state[i][j] and state[i][j] != 0:
```

```
                h += 1
```

```
    return h
```

```
def generate_moves(state, empty_tile_pos):
```

```
    moves = []
```

```
    row, col = empty_tile_pos
```

```
    for (dr, dc), direction in directions.items():
```

```
        new_row, new_col = row + dr, col + dc
```

```
        if 0 <= new_row < 3 and 0 <= new_col < 3:
```

```
            new_state = [list(r) for r in state] # Deep copy
```

```
            # Swap the empty tile with the adjacent tile
```

```
            new_state[row][col], new_state[new_row][new_col] =  
new_state[new_row][new_col], new_state[row][col]
```

```
            moves.append((new_state, (new_row, new_col), direction))
```

```
    return moves
```

```
visited = set()
```

```
start_empty_pos = next((i, j) for i in range(3) for j in range(3) if  
start_state[i][j] == 0)
```

```
start_h = calculate_heuristic(start_state)
```

```
start_node = PuzzleState(start_state, start_empty_pos, 0, start_h,  
[start_state], 0)
```

```
priority_queue = []
```

```
heapq.heappush(priority_queue, start_node)
```

```
while priority_queue:
```

```
    current_node = heapq.heappop(priority_queue)
```

```
    # Check if we reached the goal
```

```
    if current_node.state == goal_state:
```

```
        print("Goal state reached!")
```

```
        for step in current_node.path:
```

```
            for row in step:
```

```
                print(row)
```

```
            print()
```

```
        return
```

```
    visited.add(tuple(map(tuple, current_node.state))) # Add current state to  
visited
```

```
    # Generate possible moves
```

```
    for new_state, new_empty_pos, direction in  
generate_moves(current_node.state, current_node.empty_tile_pos):
```

```
        if tuple(map(tuple, new_state)) not in visited:
```

```
            g = current_node.g + 1 # Cost from start
```

```

        h = calculate_heuristic(new_state) # Heuristic
        new_path = current_node.path + [new_state]
        new_node = PuzzleState(new_state, new_empty_pos, g, h, new_path,
current_node.level + 1)

        # Print state information
        print(f"Level: {new_node.level}, Direction: {direction}, Heuristic:
{new_node.h}")
        for row in new_node.state:
            print(row)
        print()

        heapq.heappush(priority_queue, new_node)

def main():
    print("Enter initial state (3x3 grid, use 0 for empty tile):")
    start_state = [list(map(int, input().split())) for _ in range(3)]

    print("Enter goal state (3x3 grid, use 0 for empty tile):")
    goal_state = [list(map(int, input().split())) for _ in range(3)]

    astar_misplaced_tiles(start_state, goal_state)

if __name__ == "__main__":
    main()

```

Output:

Enter initial state (3x3 grid, use 0 for empty tile):

2 8 3

1 6 4

7 0 5

Enter goal state (3x3 grid, use 0 for empty tile):

1 2 3

8 0 4

7 6 5

Level: 1, Direction: Up, Heuristic: 3

[2, 8, 3]

[1, 0, 4]

[7, 6, 5]

Level: 1, Direction: Left, Heuristic: 5

[2, 8, 3]

[1, 6, 4]

[0, 7, 5]

Level: 1, Direction: Right, Heuristic: 5

[2, 8, 3]

[1, 6, 4]

[7, 5, 0]

Level: 2, Direction: Up, Heuristic: 3

[2, 0, 3]

[1, 8, 4]

[7, 6, 5]

Level: 2, Direction: Left, Heuristic: 3

[2, 8, 3]

[0, 1, 4]

[7, 6, 5]

Level: 2, Direction: Right, Heuristic: 4

[2, 8, 3]

[1, 4, 0]

[7, 6, 5]

Level: 3, Direction: Left, Heuristic: 2

[0, 2, 3]

[1, 8, 4]

[7, 6, 5]

Level: 3, Direction: Right, Heuristic: 4

[2, 3, 0]

[1, 8, 4]

[7, 6, 5]

Level: 3, Direction: Up, Heuristic: 3

[0, 8, 3]

[2, 1, 4]

[7, 6, 5]

Level: 3, Direction: Down, Heuristic: 4

[2, 8, 3]

[7, 1, 4]

[0, 6, 5]

Level: 4, Direction: Down, Heuristic: 1

[1, 2, 3]

[0, 8, 4]

[7, 6, 5]

Level: 5, Direction: Down, Heuristic: 2

[1, 2, 3]

[7, 8, 4]

[0, 6, 5]

Level: 5, Direction: Right, Heuristic: 0

[1, 2, 3]

[8, 0, 4]

[7, 6, 5]

Goal state reached!

[2, 8, 3]

[1, 6, 4]

[7, 0, 5]

[2, 8, 3]

[1, 0, 4]

[7, 6, 5]

[2, 0, 3]

[1, 8, 4]

[7, 6, 5]

[0, 2, 3]

[1, 8, 4]

[7, 6, 5]

[1, 2, 3]

[0, 8, 4]

[7, 6, 5]

[1, 2, 3]

[8, 0, 4]

[7, 6, 5]

