

22-10-24

## Implement Iterative Deepening search algorithm.

```

function ITERATIVE-DEEPENING-SEARCH
  (problem) returns a solution, or failure
  for depth = 0 to  $\infty$  do
    result  $\leftarrow$  DEPTH-LIMITED-SEARCH
      (problem, depth)
    if result  $\neq$  cutoff then return result
  
```

1. For each child of the current node
2. If it is the target node, return
3. If the current maximum depth is reached, return
4. Set the current node to this node and go back to 1.
5. After having gone through all children, go to the next child of the parent (the next sibling)
6. After having gone through all children of the start node, increase the maximum depth and go back to 1.
- ~~7. If we have reached all left leaf (bottom) nodes, the goal node doesn't exist.~~

Initial State

Goal State

~~2 8 3~~

1 4 3

7 6

5 8 2

1 4 3

7 6 2

5 8

1	4	3
7		6
5	8	2

1	3
7	4
5	8

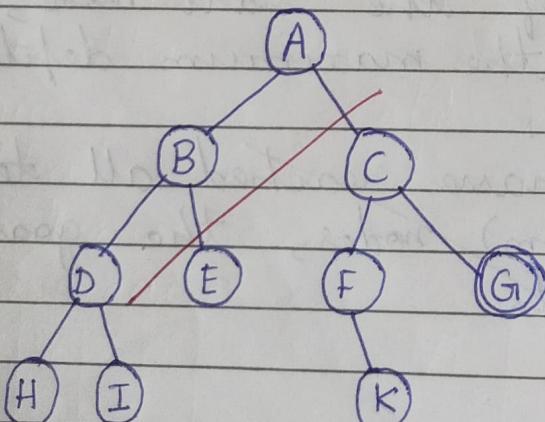
1	4	3
7	6	
5	8	2

1	4	3
7	8	6
5	2	

1	4	3
7	6	
5	8	2

1	3	1	3	1	4	1	4	3	1	4	3
7	4	6	7	4	6	7	6	3	7	8	6
5	8	2	5	8	2	5	8		5	2	5

Goal State



I Iteration A

II Iteration A, B, C

III Iteration A, B, D, E, C, F, G

Implement Hill Climbing search algorithm to solve N-Queens problem (N=4)

Hill-climbing search algorithm

function HILL-CLIMBING (problem)  
    returns a state that is a local maximum

    current  $\leftarrow$  MAKE-NODE (problem,  
                        INITIAL-STATE)

    loop do  
        neighbor  $\leftarrow$  a highest-valued  
                        successor of current  
        if neighbor.VALUE  $\leq$  current.VALUE  
            then return current.STATE  
        current  $\leftarrow$  neighbor

State: 4 queens on the board.  
One queen per column.

- Variables:  $x_0, x_1, x_2, x_3$  where  $x_i$  is the row position of the queen in column i. Assume that there is one queen per column.

- Domain for each variable:  
 $x_i \in \{0, 1, 2, 3\}$ ,  $\forall i$

- Initial state: a random state.
- Goal state: 4 queens on the board. No pair of queens are

attacking each other

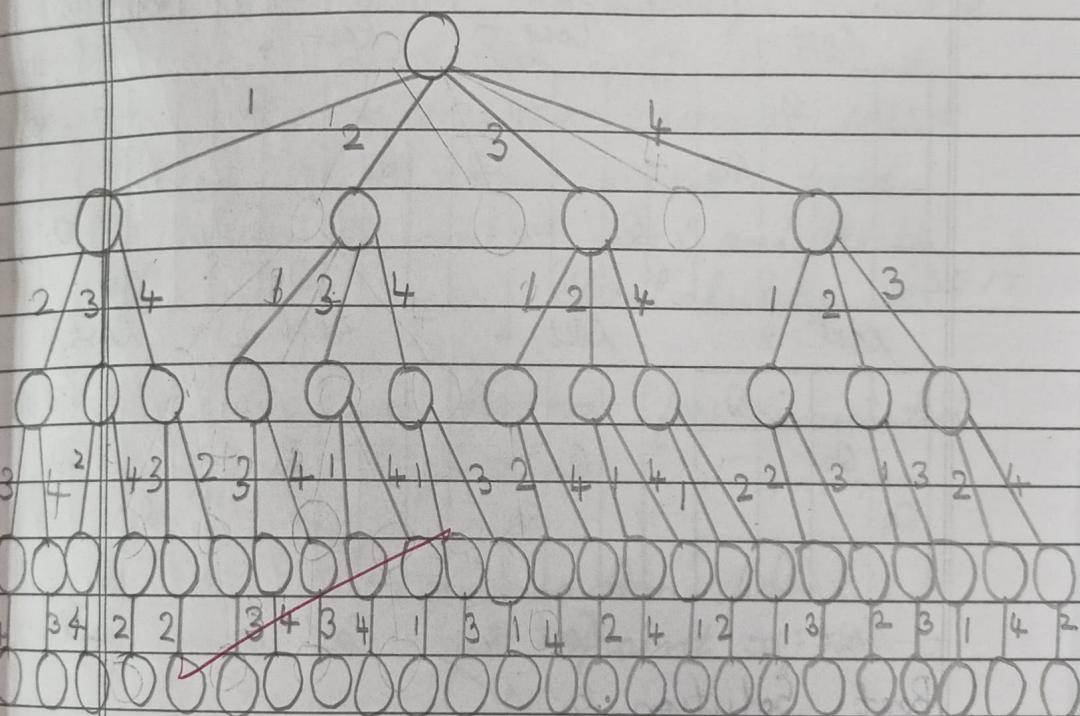
• Neighbour relation:

Swap the row positions of two queens.

• Cost function: The number of pairs of queens attacking each other, directly or indirectly.

Q <sub>1</sub>	Q <sub>2</sub>
Q <sub>3</sub>	Q <sub>4</sub>

$$\text{cost} = 2 + 3 + 3 + 2 = 10$$



Q <sub>1</sub>	Q <sub>2</sub>	Q <sub>3</sub>	Q <sub>4</sub>	Q <sub>1</sub>	Q <sub>2</sub>	Q <sub>3</sub>	Q <sub>4</sub>
Q <sub>2</sub>		-Q <sub>2</sub>	Q <sub>2</sub>	Q <sub>1</sub>	Q <sub>2</sub>		Q <sub>2</sub>
Q <sub>3</sub>			Q <sub>3</sub>	Q <sub>3</sub>	Q <sub>3</sub>		Q <sub>3</sub>
Q <sub>4</sub>			Q <sub>4</sub>			Q <sub>4</sub>	-Q <sub>4</sub>

Cost = 6

Cost = 2

Cost = 9

Cost = 12

$Q_1$	$Q_1$	$Q_1$	$Q_1$	$Q_1$
$Q_2$		$Q_2$	$Q_2$	$Q_2$
$Q_3$		$Q_3$	$Q_3$	$Q_3$
$Q_4$		$Q_4$	$Q_4$	$Q_4$

Cost = 1      Cost = 4      Cost = 2      Cost = 2

$Q_1$	$Q_1$	$Q_1$	$Q_1$
$Q_2$		$Q_2$	$Q_2$
$Q_3$	$Q_3$		$Q_3$
$Q_4$		$Q_4$	$Q_4$

Cost = 4      Cost = 1      Cost = 1      Cost = 0

$Q_1$	$Q_1$	$Q_1$	$Q_1$
$Q_2$		$Q_2$	$Q_2$
$Q_3$		$Q_3$	$Q_3$
$Q_4$		$Q_4$	$Q_4$

Cost = 1      Cost = 0      Cost = 4      Cost = 1

$Q_1$	$Q_1$	$Q_1$	$Q_1$
$Q_2$		$Q_2$	$Q_2$
$Q_3$		$Q_3$	$Q_3$
$Q_4$		$Q_4$	$Q_4$

Cost = 2      Cost = 2      Cost = 4      Cost = 1

$Q_1$	$Q_1$	$Q_1$	$Q_1$
$Q_2$		$Q_2$	$Q_2$
$Q_3$		$Q_3$	$Q_3$
$Q_4$		$Q_4$	$Q_4$

Cost = 1      Cost = 2      Cost = 6      Cost = 2

Best Solution :-

$Q_1$	$Q_2$	$Q_3$	$Q_4$
		$Q_1$	$Q_2$
		$Q_3$	$Q_4$

Cost = 0      Cost = 0

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WAP to implement Simulated Annealing Algorithm

function SIMULATED-ANNEALING (problem, schedule) returns a solution state  
 inputs: problem, a problem  
 schedule, a mapping from time to "temperature"  
 $\text{current} \leftarrow \text{MAKE-NODE} (\text{problem}, \text{INITIAL STATE})$

for  $t = 1$  to  $\infty$  do  
 $T \leftarrow \text{schedule}(t)$   
 if  $T = 0$  then return current  
 next  $\leftarrow$  a randomly selected successor of current  
 $\Delta F \leftarrow \text{next.VALUE} - \text{current.VALUE}$   
 if  $\Delta F > 0$  then  $\text{current} \leftarrow \text{next}$   
 else  $\text{current} \leftarrow \text{next}$  only with probability  $e^{\Delta F / T}$

Steps to use mroose for simulated annealing Algorithm

1. Start at a random point  $x$ .
2. Choose a new point  $x_j$  on a neighbourhood  $N(x)$ .
3. Decide whether or not to move to the new point  $x_j$ . The decision will be made based on the probability function  $P(x, x_j, T)$

$$P(x, x_j, T) = \begin{cases} 1 & \text{si } F(x_j) > F(x) \\ e^{\frac{F(x_j) - F(x)}{T}} & \text{si } F(x_j) < F(x) \end{cases}$$

#### 4. Reduce T

Steps

Python Code

```
import mbrose живе as mbrose
import numpy as np

def queensmax(position):
    queennotattacking = 0
    for i in range(len(position)-1):
        noattack = 0
        for j in range(i+1, len(position)):
            if (position[j] == position[i]) or
               (position[j] == position[i] + (j-i)) or
               (position[j] == position[i] - (j-i)):
                noattack += 1
        if noattack == len(position) - 1 - i:
            queennotattacking += 1
    return queennotattacking
```

try:

```
    ui = input("Enter the initial  
    position as 8 comma-separated  
    integers (e.g., '0,1,2,3,4,5,6,7').  
    initialpos = np.array([int(x) for  
    x >= 4 for x in initialpos])
```

// take input

obj = mbrose.CustomFitness(queens max)  
 prob = mbrose.DiscreteObj (length = 8,  
 fitness fn = objective, maximize  
 = True → max val = 4)  
 T = mbrose.ExpDecay()

result = mbrose.simulated annealing  
 (problem = prob, schedule = T,  
 max attempts = 500, max iter =  
 5000, init state = initial pos)

best state = result[0]  
 best fitness = result[1]

print("Best state")  
 print("Best fitness + 1")

print ("\"In Best State Diagram: ")  
 // print best state

O/P:-

Enter the initial position :

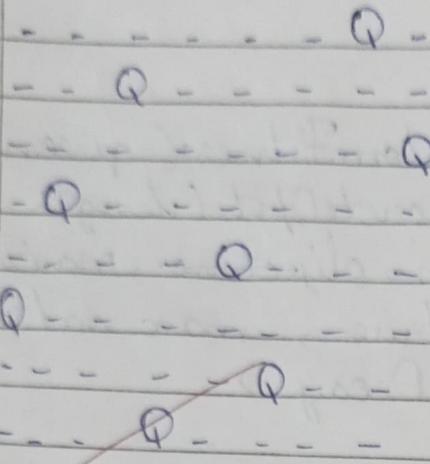
0, 1, 2, 3, 4, 5, 6, 7

The ~~best~~ position found is:

[ 5 3 1 7 4 6 0 2 ]

The number of queens that  
 are not attacking each other  
 is : 8.0

# Best State Diagram:



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Create a knowledge base using propositional logic and show that the given query entails the knowledge base or not.

### Propositional Inference: Enumeration Method

$$\text{Ex:- } \alpha = A \vee B \quad KB = (A \vee C) \wedge (B \vee \neg C)$$

A	B	C	$A \vee C$	$B \vee \neg C$	KB	$\alpha$
false	false	false	false	true	false	false
false	false	true	true	false	false	false
false	true	false	false	true	false	true
false	true	true	true	true	true	true
true	false	false	true	true	true	true
true	false	true	true	false	false	true
true	true	false	true	true	true	true
true	true	true	true	true	true	true

function TT-ENTAILS? ( $KB, \alpha$ ) returns true or false

inputs:  $KB$ , the knowledge base, a sentence in propositional logic

$\alpha$ , the query, a sentence in propositional logic

symbols  $\leftarrow$  a list of the proposition symbols in  $KB$  and  $\alpha$

return TT-CHECK-ALL ( $KB, \alpha$ , symbols, { })

function TT-CHECK-ALL ( $KB, \alpha$ , symbols, model)

returns true or false

if EMPTY? (symbols) then

if PL-TRUE? ( $KB$ , model) then return  
PL-TRUE? ( $\alpha$ , model)

else return true // when  $KB$  is

false, always returns true  
else do

$P \leftarrow \text{FIRST}(\text{symbols})$

$\text{rest} \leftarrow \text{REST}(\text{symbols})$

$\text{return}(\text{TT-CHECK-ALL}(\text{KB}, \alpha, \text{rest, model}))$

$\cup \{P = \text{true}\}$

and

$\text{TT-CHECK-ALL}(\text{KB}, \alpha, \text{rest, model})$

$\cup \{P = \text{false}\}$

O/P:-

Combinations where both KB and  $\alpha$  (AVB) are true

A    B    C

0    1    1

1    0    0

1    1    1

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Lab No. 7

# Implement Unification in First Order Logic (FOL)

Algorithm: Unify ( $\Psi_1, \Psi_2$ )

Step 1: If  $\Psi_1$  or  $\Psi_2$  is a variable or constant, then:

- If  $\Psi_1$  or  $\Psi_2$  are identical, then return NIL.
- Else if  $\Psi_1$  is a variable,
  - then if  $\Psi_1$  occurs in  $\Psi_2$ , then return FAILURE
  - else return  $\{(\Psi_2/\Psi_1)\}$
- Else if  $\Psi_2$  is a variable,
  - if  $\Psi_2$  occurs in  $\Psi_1$ , then return FAILURE
  - else return  $\{(\Psi_1/\Psi_2)\}$
- Else return FAILURE

Step 2: If the initial Predicate symbol in  $\Psi_1$  and  $\Psi_2$  are not same, then return FAILURE.

Step 3: If  $\Psi_1$  and  $\Psi_2$  have a different number of arguments, then return FAILURE.

~~Step 4: Set Substitution set (SUBST) to NIL~~

Step 5: For  $i=1$  to the number of elements in  $\Psi_2$ .

- a) Call Unify function with the ith element of  $\Psi_1$  and ith element of  $\Psi_2$ , and put the result into  $S$ .
- b) If  $S = \text{failure}$  then return Failure.
- c) If  $S \neq \text{NIL}$  then do,
- Apply  $S$  to the remainder of both  $L_1$  and  $L_2$
  - $\text{SUBST} = \text{APPEND}(S, \text{SUBST})$ .

Step 6 :- Return  $\text{SUBST}$ .

Ex 1:-

$$P(x, f(y)) - \textcircled{1}$$

$$P(a, f(g(x))) - \textcircled{2}$$

$\textcircled{1}$  and  $\textcircled{2}$  are identical if  $x$  is replaced with  $a$  in  $\textcircled{1}$

$$P(a, f(y))$$

if  $y$  is replaced with  $g(x)$

$$P(a, f(g(x)))$$

Unification is achieved

Ex 2:-

$$Q(a, g(x), a) , f(y)) - \textcircled{1}$$

$$Q(a, g(f(b)), a) , f(y)) - \textcircled{2}$$

Replace  $x$  with  $f(b)$  in  $\textcircled{1}$

~~$$Q(a, g(f(b)), a) , f(y)) - \textcircled{1}$$~~

Replace  $f(y)$  with  $f(f(b))$  in  $\textcircled{2}$

$Q(a, g(f(b), a), x)$

$Q(a, g(f(b), a), f(y))$

They are not unified

Ex 3:-

$\Psi_1 = P(b, x, f(g(z)))$  -①

$\Psi_2 = P(z, f(y), f(y))$  -②

Replace  $z$  in ② as  $b$

$\Psi_2 = P(b, f(y), f(y))$

Replace  $x$  in ① as  $f(y)$

$\Psi_1 = P(b, f(y), f(g(z)))$

Replace  $y$  in ② as  $g(z)$

$\Psi_2 = P(b, f(y), f(g(z)))$

Unification is achieved.

Ex 4:-

$\Psi_1 = P(f(a), g(y))$

$\Psi_2 = P(x, x)$

~~Failure as  $x$  cannot be replaced by  $f(a), g(y)$~~

O/P:-

i) Enter the first term: [ $'P'$ ,  $'b'$ ,  $'?x'$ ,  
 $[f, [g, ?z]]]$ ]

Enter the second term: [ $'P'$ ,  $?z$ ,  
 $[f, ?y], [f, ?y]]$ ]

~~Unification successful!~~

~~Substitution:  $?z : b, ?x : f(y)$~~

~~$[f, ?y], ?y : [g, ?z]$~~

2. Enter the first term:  
['P', ['f', ['a']], ['g', ['?y']]]  
Enter the second term: ['P', '?x', ['g', ['?y']]]  
Unification failed: Predicate symbols  
don't match: g != f

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8. Create a knowledge base consisting of FOL statements and prove the given query using forward reasoning

Algorithm

function FOL-FC-ASK(KB,  $\alpha$ ) returns a substitution or false  
 inputs: KB, the knowledge base,  
 a set of first-order definite clauses  
 $\alpha$ , the query, an atomic sentence

local variables: new, the new sentences inferred on each iteration.

repeat until new is empty

new  $\leftarrow \{\}$

for each rule in KB do

$(P_1 \wedge \dots \wedge P_n \Rightarrow q) \leftarrow \text{STANDARDIZE}$   
 - VARIABLES (rule)

for some  $p'_1 \dots p'_n$  in KB

$q' \leftarrow \text{SUBST}(q, p')$

if  $q'$  does not unify with some sentence already in KB or  
 new then add  $q'$  to new

$\phi \leftarrow \text{UNIFY}(q', \alpha)$

if  $\phi$  is not fail then return

add new to KB

return false.

It is a crime for an American to sell weapons to hostile nations

American ( $p$ )  $\wedge$  Weapon ( $q$ )  $\wedge$  Sells ( $p, q, r$ )  $\wedge$  Hostile ( $r$ )  $\Rightarrow$  Criminal ( $r$ )

Country A has some missiles.

$\exists x \text{ Owns}(A, x) \wedge \text{Missile}(x)$

Owes ( $A, T_1$ )

Missile ( $T_1$ )

All of the missiles were sold to country A by Robert

$\forall x \text{ Missile}(x) \wedge \text{Owes}(A, x) \Rightarrow \text{Sells}(\text{Robert}, x, A)$

Missiles are weapons

Missile ( $x$ )  $\Rightarrow$  Weapon ( $x$ )

#

Enemy of America is known as hostile

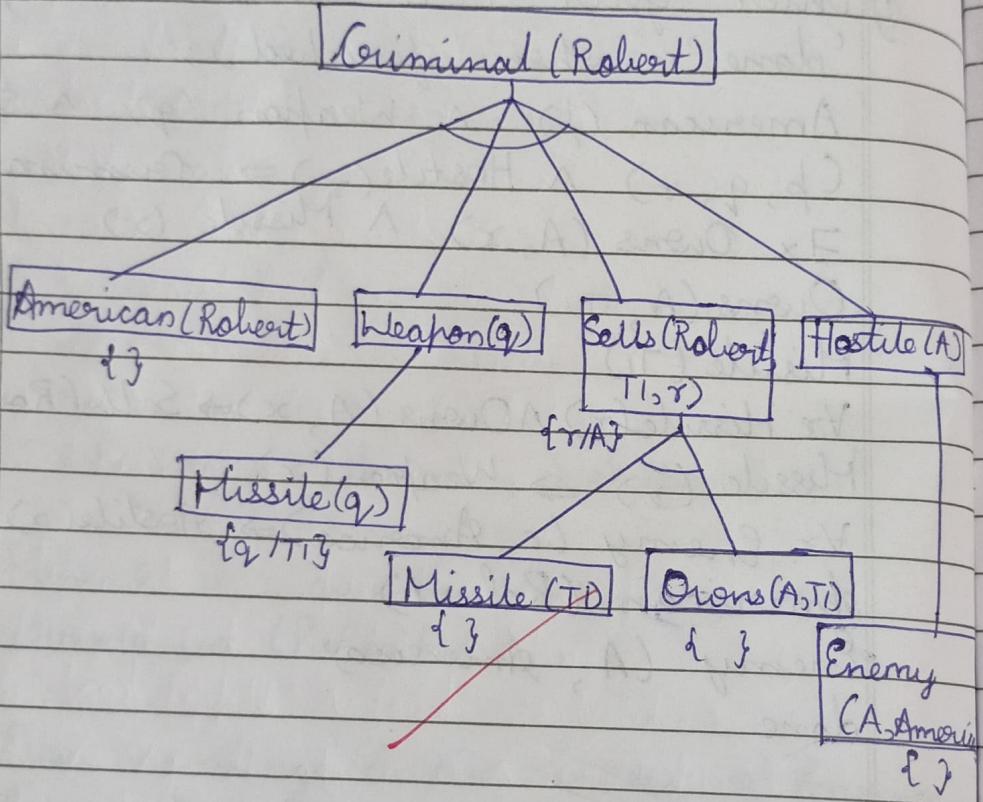
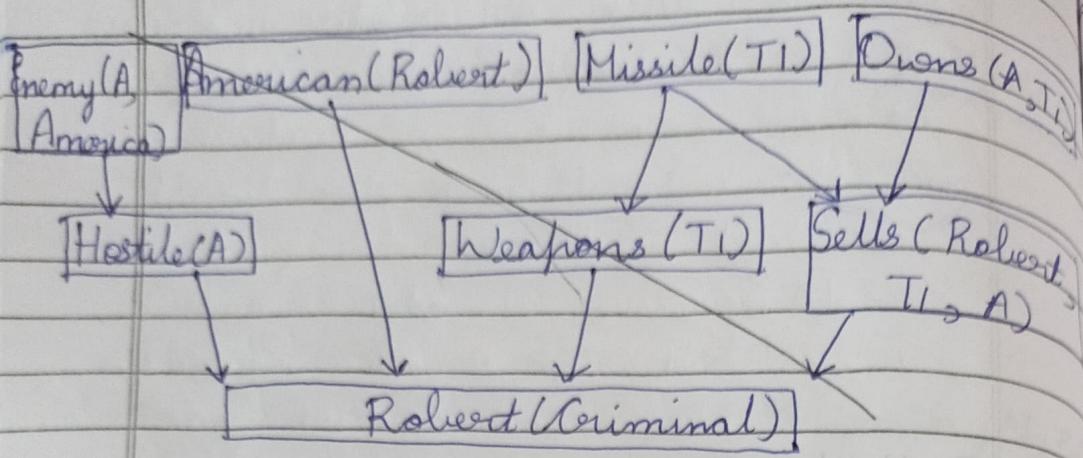
$\forall x \text{ Enemy}(x, \text{America}) \Rightarrow \text{Hostile}(x)$

Robert is an American

American (Robert)

The country A is an enemy of America

Enemy (A, America)



Output:-

- i) Enter your FOL statements ( type 'done' when finished ):

American ( $p$ )  $\wedge$  Weapon ( $q$ )  $\wedge$  Sells

( $p, q, r$ )  $\wedge$  Hostile ( $r$ )  $\Rightarrow$  Criminal ( $p$ )

$\exists x$  Owns ( $A, x$ )  $\wedge$  Missile ( $x$ )

Owes ( $A, T_1$ )

Missile ( $T_1$ )

$\forall x$  Missile ( $x$ )  $\wedge$  Owns ( $A, x$ )  $\Rightarrow$  Sells (Robert,  $x$ )

Missile ( $x$ )  $\rightarrow$  Weapon ( $x$ )

$\forall x$  Enemy ( $x, America$ )  $\Rightarrow$  Hostile ( $x$ )

American (Robert)

Enemy ( $A, America$ )

done

~~Enter the query to prove:~~

~~Criminal (Robert)~~

Proven : Criminal (Robert)

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9. Convert a given first order logic statement into Conjunctive Normal Form (CNF) to Resolution

Basic steps for proving a conclusion S given premises

Premise<sub>1</sub>, ..., Premise<sub>n</sub>

(all expressed in FOL).

1. Convert all sentences to CNF
2. Negate conclusion S & convert result to CNF
3. Add negated conclusion S to the premise clauses.
4. Repeat until contradiction or no progress is made:
  - a. Select 2 clauses (call them parent clauses)
  - b. Resolve them together, performing all required unifications
  - c. If resolvent is the empty clause, a contradiction has been found (i.e., S follows from the premises)
  - d. If not, add resolvent to the premises.

If we succeed in Step 4, we have proved the conclusion.

Given the KB or Premises:

- John likes all kind of food.
- Apple and vegetables are food.
- Anything anyone eats and not killed if food.
- Anil eats peanuts and still alive.
- Harry eats everything that Anil eats.
- Anyone who is alive implies not killed.
- Anyone who is not killed implies alive.

Prove by resolution that:

- John likes peanuts.

Representation in FOL

- $\forall x : \text{food}(x) \rightarrow \text{likes}(\text{John}, x)$
- $\text{food}(\text{Apple}) \wedge \text{food}(\text{vegetables})$
- $\forall y \forall z : \text{eats}(x, y) \wedge \neg \text{killed}(x) \rightarrow \text{food}(y)$
- $\text{eats}(\text{Anil}, \text{Peanuts}) \wedge \text{alive}(\text{Anil})$
- $\forall x : \text{eats}(\text{Anil}, x) \rightarrow \text{eats}(\text{Harry}, x)$
- $\forall z : \neg \text{killed}(z) \rightarrow \text{alive}(z)$
- $\forall x : \text{alive}(x) \rightarrow \neg \text{killed}(x)$
- likes(John, Peanuts)

Eliminate implication  $\alpha \Rightarrow \beta$  with  $\neg \alpha \vee \beta$

- $\forall x : \neg \text{food}(x) \vee \text{likes}(\text{John}, x)$
- $\text{food}(\text{Apple}) \wedge \text{food}(\text{vegetables})$
- $\forall x \forall y : \neg [\text{eats}(x, y) \wedge \neg \text{killed}(x)] \vee \text{food}(y)$
- $\text{eats}(\text{Anil}, \text{Peanuts}) \wedge \text{alive}(\text{Anil})$
- $\forall x : \neg \text{eats}(\text{Anil}, x) \vee \text{alive}(x) \text{ eats}(\text{Harry}, x)$
- $\forall x : \neg [\neg \text{killed}(x)] \vee \text{alive}(x)$
- $\forall x : \neg \text{alive}(x) \vee \neg \text{killed}(x)$
- likes(John, Peanuts)

Move negation ( $\neg$ ) inwards and rewrite

- $\forall x : \neg \text{food}(x) \vee \text{likes}(\text{John}, x)$
- $\text{food}(\text{Apple}) \wedge \text{food}(\text{vegetables})$
- $\forall x \forall y : \neg \text{eats}(x, y) \vee \neg \text{killed}(x) \vee \text{food}(y)$
- $\text{eats}(\text{Anil}, \text{Peanuts}) \wedge \text{alive}(\text{Anil})$
- $\forall x : \neg \text{eats}(\text{Anil}, x) \vee \text{eats}(\text{Harry}, x)$
- $\forall z : \neg \text{killed}(z) \vee \text{alive}(z)$
- $\forall z : \neg \text{alive}(z) \vee \neg \text{killed}(z)$
- likes(John, Peanuts).

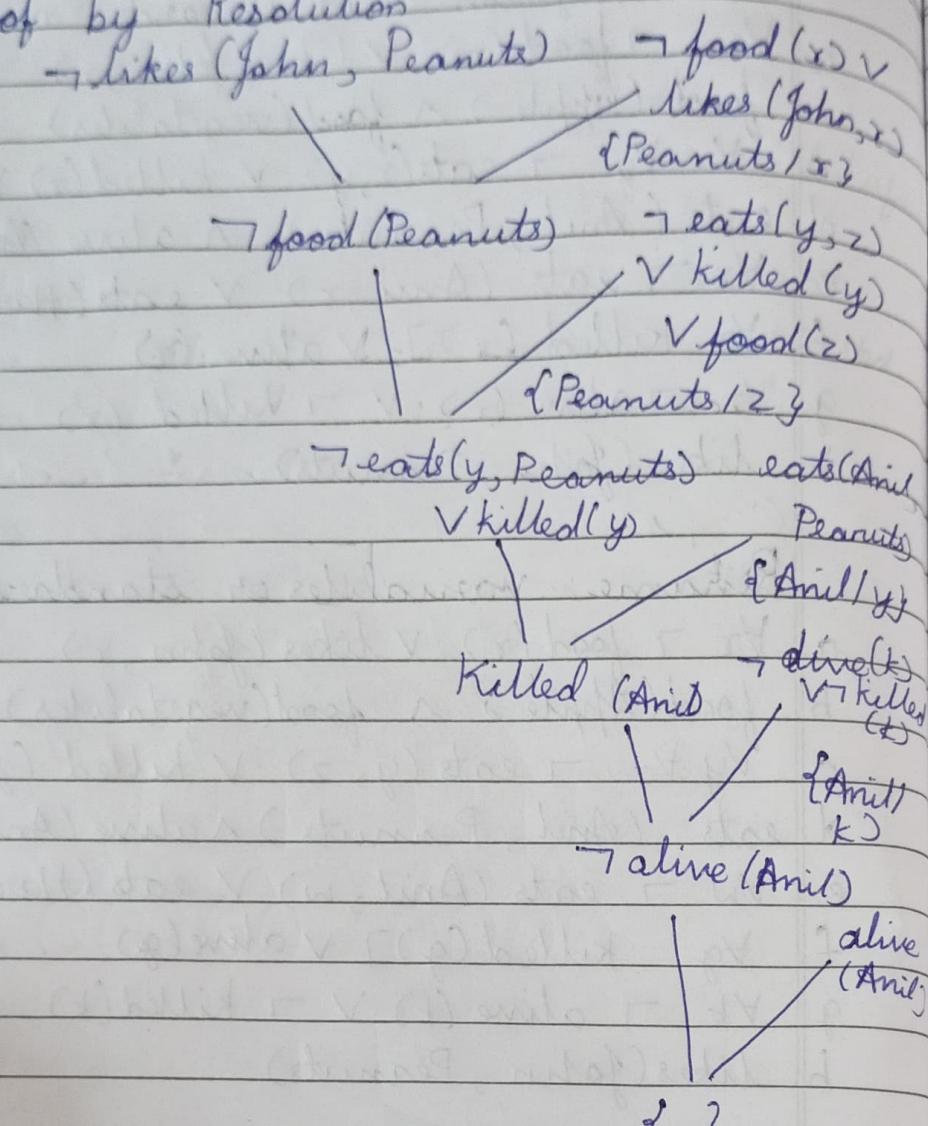
Rename variables or standardize view

- $\forall x : \neg \text{food}(x) \vee \text{likes}(\text{John}, x)$
- $\text{food}(\text{Apple}) \wedge \text{food}(\text{vegetables})$
- $\forall y \forall z : \neg \text{eats}(y, z) \vee \neg \text{killed}(y) \vee \text{food}(z)$
- $\text{eats}(\text{Anil}, \text{Peanuts}) \wedge \text{alive}(\text{Anil})$
- $\forall w : \neg \text{eats}(\text{Anil}, w) \vee \text{eats}(\text{Harry}, w)$
- $\forall g : \neg \text{killed}(g) \vee \text{alive}(g)$
- $\forall k : \neg \text{alive}(k) \vee \neg \text{killed}(k)$
- likes(John, Peanuts)

Drop Universal Quantifiers

- $\neg \text{food}(x) \vee \text{likes}(\text{John}, x)$
- $\text{food}(\text{Apple})$
- $\text{food}(\text{vegetables})$
- $\neg \text{eats}(y, z) \vee \neg \text{killed}(y) \vee \text{food}(z)$
- $\text{eats}(\text{Anil}, \text{Peanuts})$
- $\text{alive}(\text{Anil})$
- $\neg \text{eats}(\text{Anil}, w) \vee \text{eats}(\text{Harry}, w)$
- $\neg \text{killed}(g) \vee \text{alive}(g)$
- $\neg \text{alive}(k) \vee \neg \text{killed}(k)$
- likes(John, Peanuts).

Proof by Resolution



Output:-

Derived Fact: ~~Food(Peanuts)~~

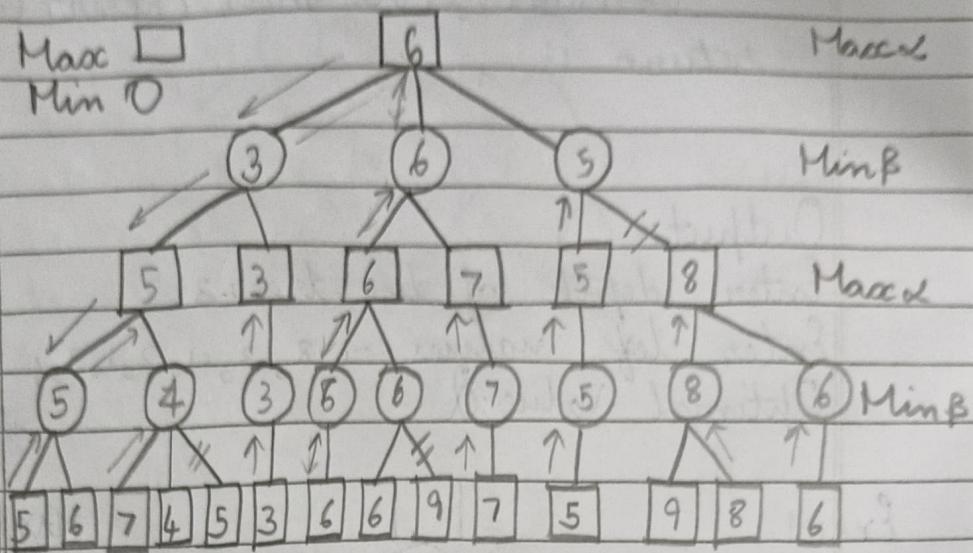
Derived Fact: ~~Likes(John, Peanuts)~~

Proven: ~~Likes(John, Peanuts)~~

Hence Proven

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## 10. Alpha Beta Pruning Algorithm



$$\alpha \geq \beta$$

Algorithm:

function MINIMAX-DECISION(state) returns  
an action

return arg max  $a \in \text{ACTIONS}(s)$

MIN-VALUE(RESULT(state, a))

function MAX-VALUE(state) returns a  
utility value

if TERMINAL-TEST(state) then return  
UTILITY(state)

$$v \leftarrow -\infty$$

for each  $a$  in ACTIONS(state) do

~~$v \leftarrow \max(v, \text{MIN-VALUE}(\text{RESULT}(s, a)))$~~

returns  $v$

function MIN-VALUE(state) returns a  
utility value

if TERMINAL-TEST(state) then return  
UTILITY(state)

$$v \leftarrow \infty$$

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for each  $a$  in ACTIONS( $s_t$ ) do  
 $v \leftarrow \min(v, \text{MAX-VALUE}(\text{RESULT}(s_t, a)))$   
return  $v$

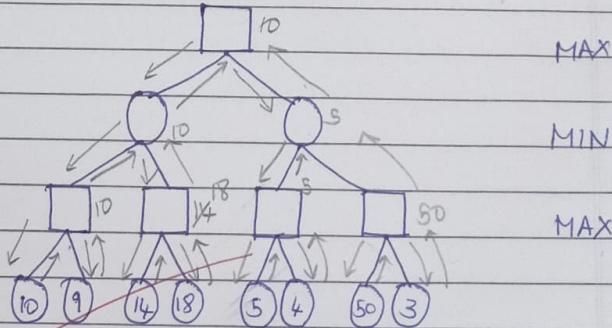
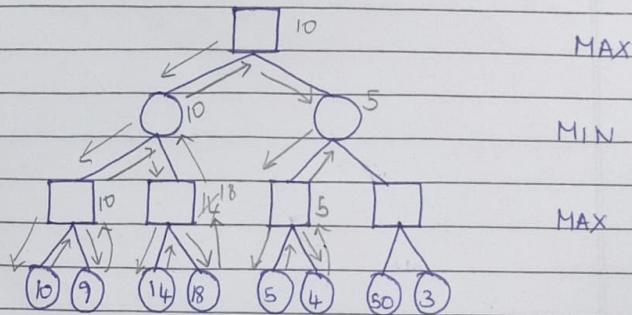
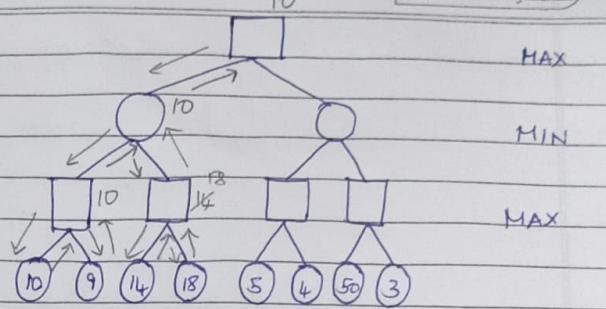
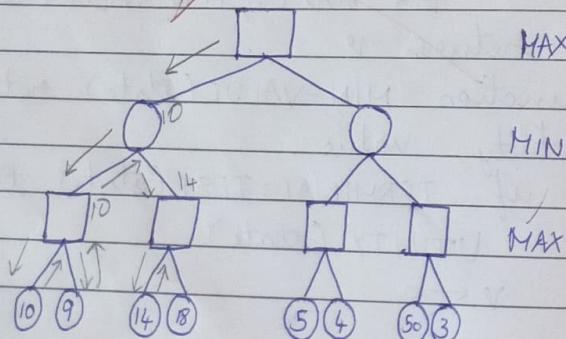
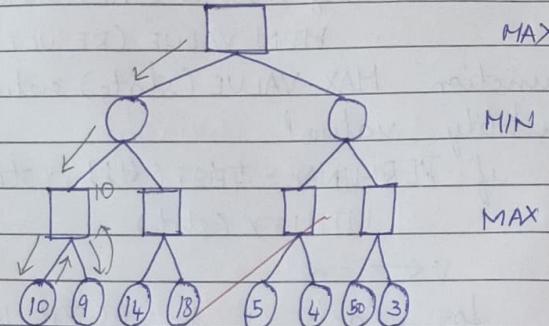
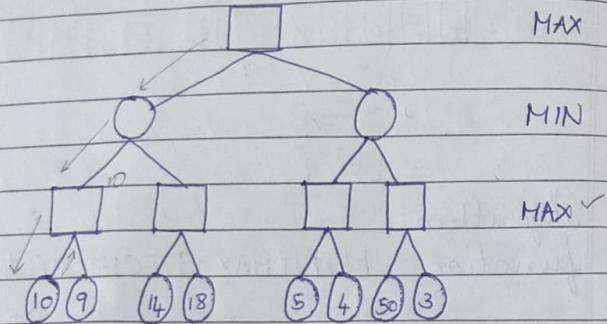
Output:-

Enter depth of the tree: 3

Enter leaf values: -1, 8, -3, -1, 2, 1, 3, 4

Optimal Value: 0

Ex:-



SB  
31/07/2024