

Implementation of 8 Puzzle Problem using non heuristic approach

Using BFS

```
from collections import deque
```

```
# Class representing the state of the board
```

```
class BoardNode:
```

```
def __init__(self, board, parent=None, move=None):
```

```
self.board = board # The current state of the board
```

```
self.parent = parent # The parent node (previous state)
```

```
self.move = move # The move taken to reach this state
```

```
def is_goal(self, goal_state):
```

```
return self.board == goal_state # Check if the current state matches the goal state
```

```
def __hash__(self):
```

```
return hash(str(self.board)) # Unique identifier for the state
```

```
def __eq__(self, other):
```

```
return self.board == other.board # Equality check for two BoardNodes
```

```
def __repr__(self):
```

```
return '\n'.join([' '.join(map(str, row)) for row in self.board]) # Display the board state
```

```
# BFS class implementing the search algorithm
```

```
class BFS:
```

```
def __init__(self, initial_board, goal_state):
```

```
self.initial_node = BoardNode(initial_board) # Initialize with the starting state
```

```

self.goal_state = goal_state # Goal state for the puzzle

def search(self):
    visited = set() # Set to keep track of visited states
    queue = deque([self.initial_node]) # Initialize the queue for BFS
    solutions = [] # List to store all solutions

    while queue:
        node = queue.popleft() # Remove the first node from the queue

        if node.is_goal(self.goal_state): # Check if the current node is a goal state
            path = self.get_solution_path(node) # Get the solution path
            solutions.append(path) # Store the solution path
            continue # Continue to search for other solutions

        visited.add(node) # Mark the current node as visited

        # Generate successors and add them to the queue
        for neighbor in self.get_successors(node):
            if neighbor not in visited and neighbor not in queue:
                queue.append(neighbor) # Add the new state to the queue

    # Display all solutions found
    for idx, solution in enumerate(solutions):
        print(f"Solution {idx + 1}: Moves: {solution}")

    print(f"Total number of optimal solutions: {len(solutions)}") # Print total solutions

```

```

def get_successors(self, node):

    board = node.board

    x, y = self.find_zero(board) # Find the position of the empty tile (0)

    successors = []

    # Define possible moves (direction, new x, new y)
    moves = [('UP', -1, 0), ('DOWN', 1, 0), ('LEFT', 0, -1), ('RIGHT', 0, 1)]

    # Generate new board states for each possible move
    for move_name, dx, dy in moves:

        new_x, new_y = x + dx, y + dy

        if 0 <= new_x < 3 and 0 <= new_y < 3: # Check if the new position is within bounds

            new_board = [row[:] for row in board] # Copy the current board state

            new_board[x][y], new_board[new_x][new_y] = new_board[new_x][new_y],
            new_board[x][y] # Swap

            successors.append(BoardNode(new_board, node, move_name)) # Create a new BoardNode

    return successors


def find_zero(self, board):

    # Locate the empty space (0) in the board

    for i in range(len(board)):

        for j in range(len(board[i])):

            if board[i][j] == 0:

                return i, j

    return None

```

```

def get_solution_path(self, node):
    # Reconstruct the path to the solution by following parent nodes
    path = []
    while node.parent is not None:
        path.append(node.move) # Add the move taken to the path
        node = node.parent # Move to the parent node
    return path[::-1] # Reverse the path to get the correct order


# Function to get user input for the board configuration
def get_user_input(board_type):
    print(f"Enter the {board_type} 8-puzzle board configuration (3x3) row by row (use 0 for the empty tile):")
    board = []
    for _ in range(3):
        row = list(map(int, input().split())) # Input a row
        board.append(row) # Add row to the board
    return board


# Main function to run the program
if __name__ == "__main__":
    initial_board = get_user_input("initial") # Get the initial board configuration from the user
    goal_state = get_user_input("goal") # Get the goal board configuration from the user


# Create a BFS instance and start the search
bfs_solver = BFS(initial_board, goal_state)
bfs_solver.search() # Perform the search for solutions

```

Output:

Enter the initial 8-puzzle board configuration (3x3) row by row (use 0 for the empty tile):

1 2 3

0 4 6

7 5 8

Enter the goal 8-puzzle board configuration (3x3) row by row (use 0 for the empty tile):

1 2 3

4 5 6

7 8 0

Solution 1:

Moves: ['RIGHT', 'DOWN', 'RIGHT']

Final Board State:

1 2 3

4 5 6

7 8 0

Number of moves: 3

Solution 2:

Moves: ['RIGHT', 'RIGHT', 'DOWN', 'LEFT', 'UP', 'RIGHT', 'DOWN', 'LEFT', 'UP', 'RIGHT', 'DOWN']

Final Board State:

1 2 3

4 5 6

7 8 0

Number of moves: 11

Using DFS

```
class BoardNode:
```

```
def __init__(self, board, parent=None, move=None):
```

```
    self.board = board
```

```
    self.parent = parent
```

```
    self.move = move
```

```
def is_goal(self, goal_state):
```

```
    return self.board == goal_state
```

```
def __hash__(self):
```

```
    return hash(str(self.board))
```

```
def __eq__(self, other):
```

```
    return self.board == other.board
```

```
def __repr__(self):
```

```
    return '\n'.join([' '.join(map(str, row)) for row in self.board])
```

```
class DFS:
```

```
def __init__(self, initial_board, goal_state):
```

```
    self.initial_node = BoardNode(initial_board)
```

```
    self.goal_state = goal_state
```

```
    self.found_solutions = []
```

```
    self.unique_states = set() # Set to track unique states
```

```
    self.permutation_count = 0 # Counter for permutations
```

```

def search(self):
    visited = set()
    self._dfs(self.initial_node, visited)

    # Print solutions and states
    if self.found_solutions:
        for solution in self.found_solutions:
            self.print_solution(solution)
        else:
            print("No solution found.")

    # Print unique states encountered
    print(f"Total unique states encountered: {len(self.unique_states)}")
    print(f"Total permutations encountered: {self.permutation_count}")

def _dfs(self, node, visited):
    if node.is_goal(self.goal_state):
        self.found_solutions.append(self.get_solution_path(node))
        return True

    visited.add(node) # Add the current node to visited set

    # Add current state as a hashable tuple
    self.unique_states.add(tuple(map(tuple, node.board))) # Add current state to unique states
    self.permutation_count += 1 # Increment permutation count

    for neighbor in self.get_successors(node):
        if neighbor not in visited:
            if self._dfs(neighbor, visited):

```

```
return True
```

```
return False
```

```
def get_successors(self, node):
```

```
    board = node.board
```

```
    x, y = self.find_zero(board)
```

```
    successors = []
```

```
    moves = [('UP', -1, 0), ('DOWN', 1, 0), ('LEFT', 0, -1), ('RIGHT', 0, 1)]
```

```
    for move_name, dx, dy in moves:
```

```
        new_x, new_y = x + dx, y + dy
```

```
        if 0 <= new_x < 3 and 0 <= new_y < 3: # Check bounds
```

```
            new_board = [row[:] for row in board] # Make a copy
```

```
            new_board[x][y], new_board[new_x][new_y] = new_board[new_x][new_y],  
            new_board[x][y]
```

```
            successors.append(BoardNode(new_board, node, move_name))
```

```
    return successors
```

```
def find_zero(self, board):
```

```
    for i in range(3):
```

```
        for j in range(3):
```

```
            if board[i][j] == 0:
```

```
                return i, j
```

```
def get_solution_path(self, node):
```

```
    path = []
```



```

while node:
    if node.move:
        path.append(node.move)
        node = node.parent
    return path[::-1] # Reverse path to show from start to goal

def print_solution(self, path):
    print("Solution moves:", path)

def get_user_input():
    print("Enter the initial state (3 rows of 3 numbers, use 0 for empty space):")
    board = []
    for _ in range(3):
        row = list(map(int, input().strip().split()))
        board.append(row)
    return board

def main():
    initial_board = get_user_input()
    print("Enter the goal state (3 rows of 3 numbers, use 0 for empty space):")
    goal_state = []
    for _ in range(3):
        row = list(map(int, input().strip().split()))
        goal_state.append(row)
    dfs_solver = DFS(initial_board, goal_state)
    dfs_solver.search()

if __name__ == "__main__":
    main()

```

Output:

Enter the initial state (3 rows of 3 numbers, use 0 for empty space):

1 2 3

0 4 6

7 5 8

Enter the goal state (3 rows of 3 numbers, use 0 for empty space):

1 2 3

4 5 6

7 8 0

Total unique states encountered: 852

Total permutations encountered: 852