

# CSC 212: Data Structures and Abstractions

## Binary search trees (part 1)

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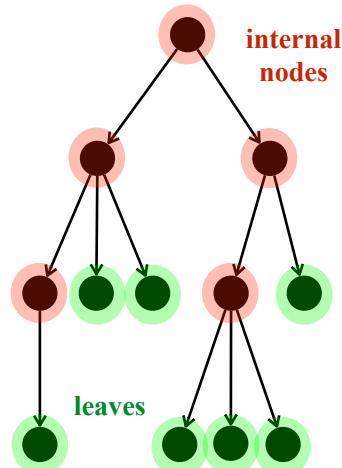
Fall 2025



## Trees

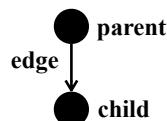
### Definition

- ✓ data structure that consists of **nodes** connected by **edges**
  - hierarchical structure, with a single **root** node
  - each node can have zero or more **children**



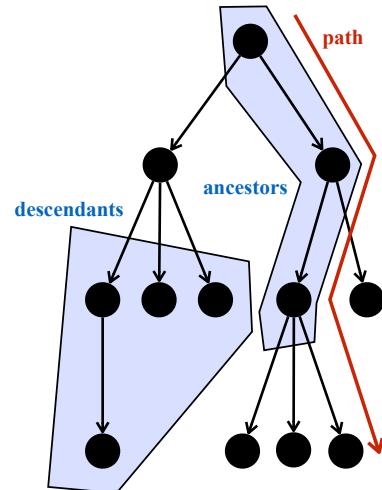
### Terminology

- ✓ each node is either a **leaf** or an **internal node**
  - leaves are nodes with no children, while internal nodes are nodes with one or more children
- ✓ nodes with the same **parent** are **siblings**



## Trees

## Paths

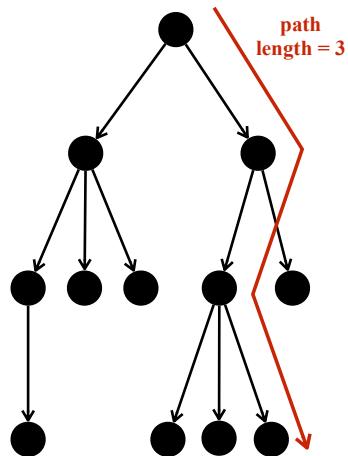


A **path** from node  $v_0$  to  $v_n$  is a sequence of nodes  $v_0, v_1, \dots, v_n$ , where there is a (directed) edge from one node to the next

The **descendants** of a node  $v$  are all nodes reached by a path from node  $v$  to the leaf nodes

The **ancestors** of a node  $v$  are all nodes found on the path from the root to node  $v$

## Depth and height



The length of a **path** is the number of edges in the path

The **depth** (level) of a node  $v$  is the length of the path from the root node to  $v$

The **height** of a node  $v$  is the length of the path from  $v$  to its deepest descendant

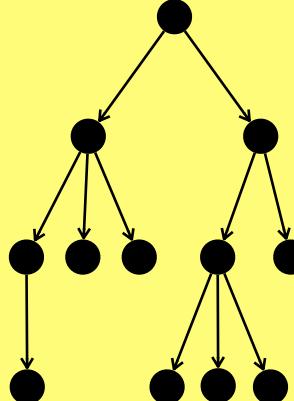
The **depth of the tree** is the depth of deepest node

The **height of the tree** is the height of the root

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## Practice

- Label all nodes with height and depth
  - indicate the height and the depth of the tree



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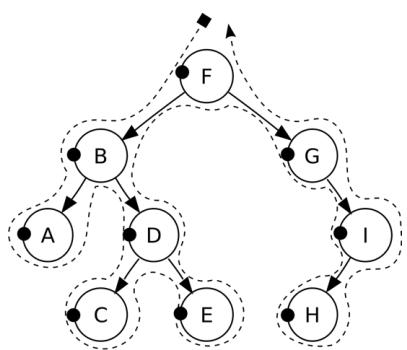
## Traversals

### Definition

- a **traversal** is a way of visiting all the nodes in a tree

### Types of traversals:

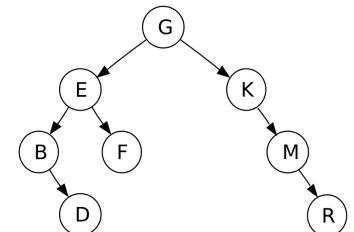
- pre-order traversal:** visit the root node first, then recursively visit all subtrees
- post-order traversal:** recursively visit all subtrees first, then visit the root node



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## Pre-order traversal

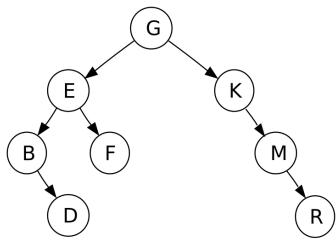
```
algorithm preorder(p) {  
    visit(p)  
    for each child c of p {  
        preorder(c)  
    }  
}
```



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## Post-order traversal

```
algorithm postorder(p) {
    for each child c of p {
        postorder(c)
    }
    visit(p)
}
```



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## Binary trees

## k-ary trees

- k-ary tree
  - ✓ every node has between 0 and k children

- Full k-ary tree

- ✓ every node has exactly 0 or k children

- Complete k-ary tree

- ✓ every level is entirely filled
  - ✓ except possibly the deepest, where all nodes are as far left as possible

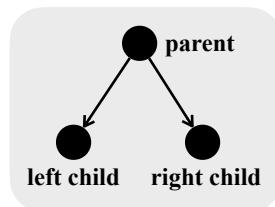
- Perfect k-ary tree

- ✓ every leaf has the same depth and the tree is full

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## Binary trees

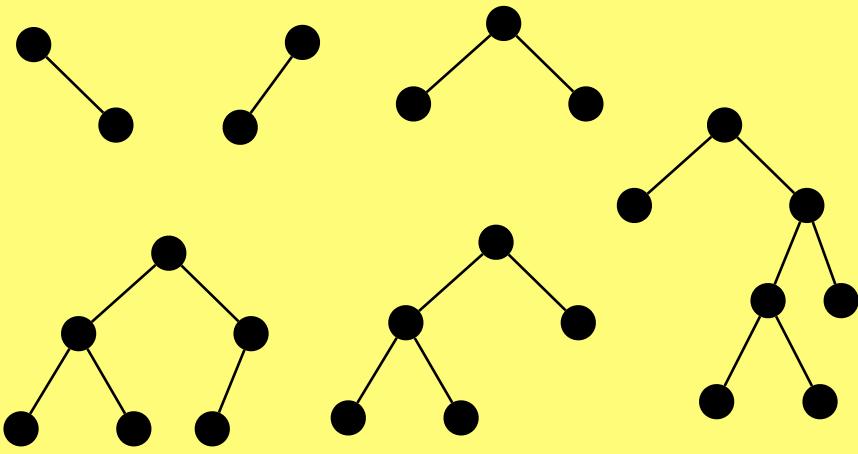
- Definition
  - ✓ a special case of a k-ary tree, where  $k = 2$



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## Practice

- Mark the following binary trees ( $k=2$ ) as full/complete/perfect



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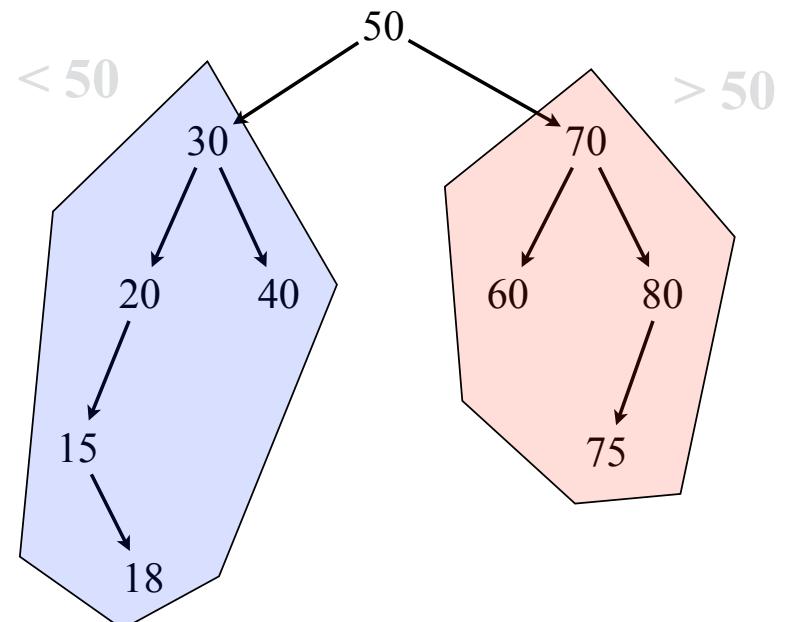
## Binary search trees

### Binary search tree

- A binary search tree (BST) is a **binary tree**
- A BST has **symmetric order**
  - each node  $x$  in a BST has a key denoted by  $key(x)$
  - for all nodes  $y$  in the left subtree of  $x$ ,  $key(y) < key(x)$  \*\*
  - for all nodes  $y$  in the right subtree of  $x$ ,  $key(y) > key(x)$  \*\*

(\*\*) assume that the keys of a BST are pairwise distinct

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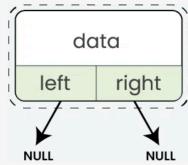


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## Representing a node

```
template <typename T>
struct BSTNode {
    T key;
    BSTNode<T> *left, *right;

    BSTNode(const T& value) {
        data = value;
        left = right = nullptr;
    }
};
```



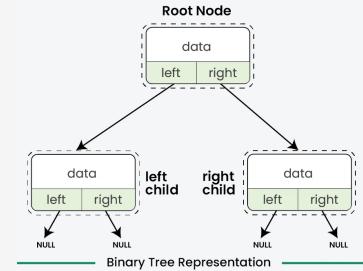
The implementation of a **binary tree node** requires a structure that can accommodate connections to two child nodes

<https://www.geeksforgeeks.org/binary-tree-representation/>

## Representing a binary search tree

```
template <typename T>
class BST {
private:
    struct Node {
        T data;
        Node *left, *right;
        Node(const T& value) {
            data = value;
            left = right = nullptr;
        }
    };
    Node *root;
    size_t size;

public:
    BST() : root(nullptr), size(0) {}
    ~BST() { clear(); }
    size_t getSize() const { return size; }
    bool empty() const { return size == 0; }
    void insert(const T& value);
    void remove(const T& value);
    bool contains(const T& value) const;
    void clear();
};
```



<https://www.geeksforgeeks.org/binary-tree-representation/>

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