

Python course work

Question 1:

Codes used:

- **swap_first_last():** Takes the number as a string and swaps the first and last digits using slicing.
- **reverse_number():** Reverses the number by converting it to a string and using `[::-1]`.
- **mathematical_problem():**
 - *) Used a while loop to repeatedly ask for input.
 - *) Validates input using `isdigit()` and checks the number range using `100 <= num <= 9999`.
 - *) Performs operations like swapping digits, finding the difference, reversing the difference, and summing them.
- Please input number at last 3 digit or 4 digits.

Question2:

Libraries used: numpy

- ❖ Part a: using if and else function to check if the number is non-negative.
- ❖ Part b: used codes (**`np.linalg.inv`**) and (**`A.transpose()`**) to find inverse and transpose.
Further, find the answer of given equation $49(B - 1)^2 + 7B^{-1}A^T + 7A^TB^{-1} + (AT)^2$
- ❖ Part c: Find $(B-2C)^{-1}=A$?

Here, I took inverse on both side resulting in $(B-2C)=A^{-1}$ then I got final expression as

$$C=0.5*(B-A^{-1})$$

- ❖ Part d: Show that M is invertible and find M^{-1} ?

First I took determinant of M which was not = to 0 and then find M^{-1}

- ❖ Part e: eigenvalues of matrix $M= 1, -3$ and

an eigenvector corresponding to each eigenvalues were= for 1 it is $[1,1]$ and

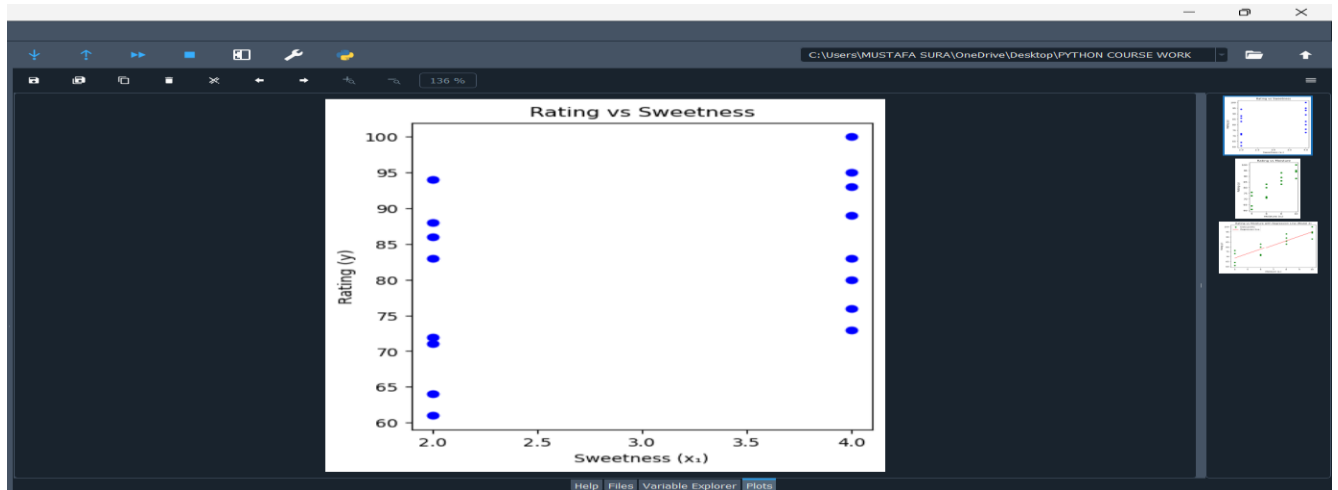
for -3 it is $[0,1]$ both are in column not row. Find out using $\det(M-\lambda I)=0$ equation

- ❖ Part f: $M = P D P^{-1}$ here, matrix P formed by placing $[V1,V2]$ eigenvectors, then took inverse of P and finally find out the diagonal matrix D which is with eigen values on diagonals.

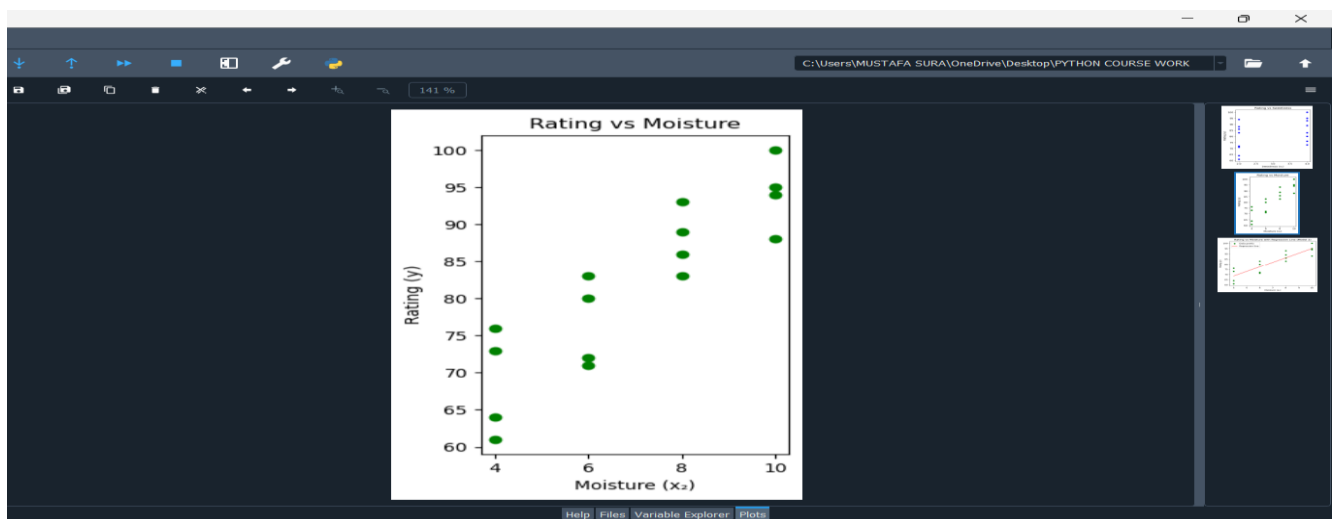
Question 3:

❖ Part b:

Plot 1: Rating vs Sweetness: The scatter plot shows that as Sweetness increases from 2 to 4, the Rating tends to increase for each level of Moisture, suggesting a positive relationship.



Plot 2: Rating vs Moisture: As Moisture increases from 4 to 10, the Rating generally increases, indicating a strong positive relationship.



❖ Part c: Model 1: slope= 4.375 intercept= 68.625

The estimated regression equation for Model 1 is:

$$\text{Rating} = 68.62 + 4.38 * \text{Sweetness}$$

Model 2: slope = 4.425 intercept = 50.77

The estimated regression equation for Model 2 is:

$$\text{Rating} = 50.78 + 4.42 * \text{Moisture}$$

❖ **Part d:** At a significance level of $\alpha=0.05$. Since $0.130 > 0.05$, we fail to reject the null hypothesis. Therefore, it's not a significant relationship between Sweetness and Rating in Model 1 at the 5% significance level because the p-value (0.130) is greater than 0.05.

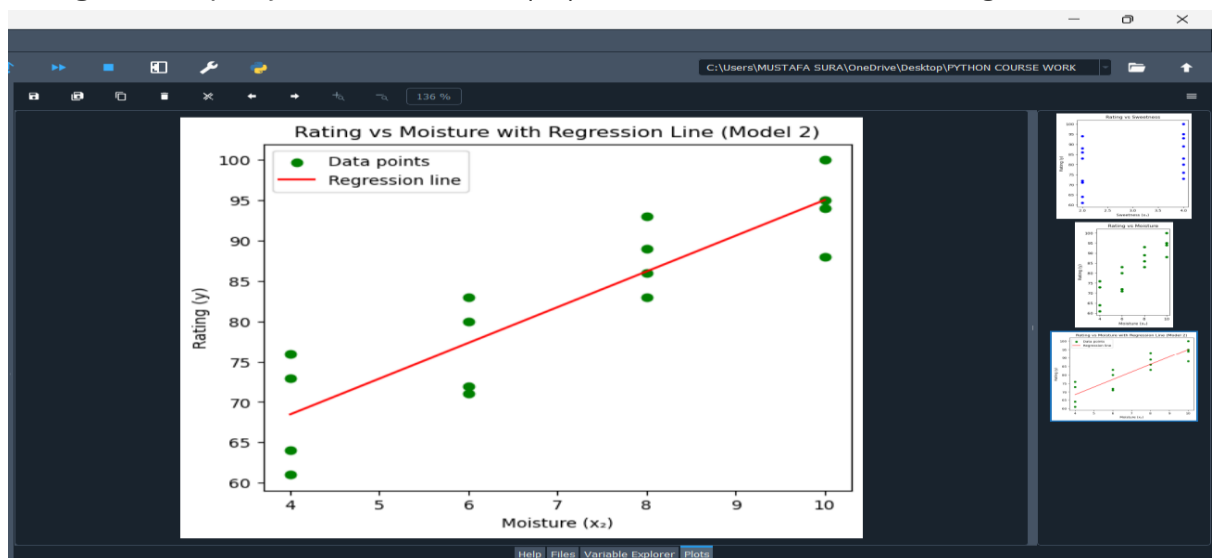
❖ **Part e:** Value of $R^2 = 0.7964$ for model 2

Interpretation: This indicates that 79.6% of the variation in the Rating can be explained by the Moisture level of the pastry.

❖ **Part f:** By comparing R^2 and p-value of both models 1 and 2 the model 2 is more perfect to use in estimating the rating of a pastry.

This is because Model 2 has a **higher R^2 value (0.796)**, indicating better explanatory power, and the predictor **Moisture is statistically significant ($p < 0.05$)**. Contrary to this, Model 1 has a low R^2 and an insignificant predictor.

❖ **Part g:** scatter plot just like the one in (3b) but also with an estimated regression line:



- The plot shows a strong positive linear relationship between Moisture and Rating.
- As Moisture increases, the Rating also tends to increase.

❖ **Part h:** If a new record of ratings on sweetness is 6 and moisture is 10, based on your selected model in (3f), what is the predicted pastry rating?

Can't use Sweetness as in model 2 its **between Rating and Moisture**

Therefore, using Moisture=10

Gives the predicted pastry rating as 95.025