

# Graph-based extractive text summarization based on single document

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### Abstract

Day by day, the amount of online and offline text data is growing tremendously from various sources like legal documents, medical documents, news articles, etc. Manual text summarization of large documents is unfeasible and costly because it takes much time and requires more effort. As a consequence, various graph-based text summarization techniques have been designed which provide thoroughly and well-prepared summaries of documents. The problems issues that exist in these techniques are redundancy of data, loss of information and readability. To overcome these problems, we have proposed a textual graph-based extractive text summarization technique called TGETS, for extracting essential information from a single document. In the proposed approach, a graph's node is denoted as group of sentences in the document and an edge of the graph is represented as an association between two sentences. The summary generation is based on the sum of sentence weight and the average weight of the textual graph. The performance of proposed approach is evaluated on the BBC news articles dataset through the ROUGE-metric ( $R_1$  and  $R_2$ ). The proposed approach in the range of 100-200 words length summary offers better scores of 19.88%, 38.76%, and 30.73% for  $R_1$  under precision, recall and  $F_1$ -score with respect to the existing PageRank (PR) method. Similarly, for  $R_2$ , the proposed approach exceeds by 32%, 26.99%, and 29.01% for precision, recall, and  $F_1$ -score with respect to existing PageRank (PR) method.

 $\textbf{Keyword} \ \ \text{Text summarization} \cdot \text{Extractive text summarization} \cdot \text{Lemmatization} \cdot \text{Textual graph} \cdot \text{ROUGE}$ 

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### 1 Introduction

Nowadays, the growth of textual data information in digital format is huge on the website and almost 80% of text data information is available on the Internet. Due to overloaded textual information over Internet, several indispensable issues and challenging tasks arise. These issues include summarization of multiple languages of text documents, single document summarization based on extractive text summarization, positioning of sentence order of the summary, loss of information [16], quality of summary, and computationally expensive [8, 25]. On the way to resolve these issues, there are several challenges, such as to build an extractive text summarization method for huge text corpus (documents) like news articles, novels, and stories [40, 53], to address relevant keywords from text documents based on summarizer tools. Another challenge while summarizing a lengthy document is the compression ratio [5]. The efficiency of a system in terms of computation cost is affected by the length of a text document. Currently, researchers and academicians find it challenging to create an effective extractive summary for long text documents. Several researchers and academics are now working on text corpus in fields such as text categorization, information retrieval, document summary, sentiment analysis [5], question answering [8], i.e., Chatbot, mining large data, social media analysis, radio news, scientific papers, encyclopedias, technical reports, journal articles, web pages, etc. and text summarization is classified into several categories, that is shown in Fig. 1.

- 1. Generality can be classified into query and generic-based summarization (shown in Fig. 1). Query-based summarization has a collection of homogenous documents dealt by multi-documents. It is brought out from the corpus for query results [42]. Query-generated summaries always focus on query-related content. Generic summarization is extracting relevant information from one or more input documents, providing it to the common sense of its content [1, 16]. In comparison, generic-based cannot depend on user query but query-based summarization depend on the user query.
- Purpose can be categorized into a general and specific domain i.e., shown in Fig. 1. Both
  domains are independent of the text summarization document. There are different types
  of domains used in a particular field, such as sports documents, legal documents, medical
  documents, news articles, etc.
- 3. Input-type documents are divided into single and multi-document, as shown in Fig. 1. A single document provides single input and then generates a single output summary but a multi-document provides a multi-input at the time of summarization and generates a single output summary. In existing work, several authors have used single or multi-document types such as [29, 42, 45].

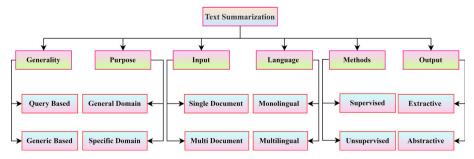


Fig. 1 Classification of text summarization approaches



- 4. Languages are separated into two groups: monolingual and multilingual, i.e., also shown in Fig. 1. When both the source and target documents are in the same language, a summarization system is known as monolingual language. If the source text is written in multiple languages (for example, Hindi, English, Nepali and Urdu), and the summary is produced in each of those languages, the text summarization system is called multilingual.
- 5. Methods for text summarization can be divided into two categories: supervised and unsupervised, i.e., also shown in Fig. 1. Both are possible depending on whether or not training data is necessary. A supervised approach is trained using labeled data to pick out concepts from text documents. The most common method is unsupervised, and it produces summaries from text documents. They do not rely on any training examples with labels applied by users.
- 6. Output is classified into extractive text summarization and abstractive text summarization, as shown in Fig. 1. Extractive text summarization generates an extractive summary from the given text documents. Extractive text summarization focuses on significant sentences from a given text document with many approaches such as machine learning, linguistics, statistics, optimization approach [24], etc. Extractive text summarization has a conspicuous rank assigned to sentences in text documents. Conspicuous sentences are selected on the rank of sentences previously chosen to produce the original documents' summary. Abstractive text summarization creates an abstract overview containing phrases and words in the original document. Besides this, the overview generated by abstractive text summarization also includes words that are not there in the document but takes those words from the dictionary to generate a meaningful summary. Abstractive text summarization has a more challenging task because it has semantic restrictions and language dependency due to paraphrasing. Abstractive text summarization can be applied in relatively small documents for the most straightforward tasks like sentence fusion, sentence compression [21, 24, 40], and generation of keywords, headlines, or titles [35, 37]. However, abstractive text summarization is more complicated than extractive text summarization. The extractive text summarization raises the achievability to attain the quality of document summarization. Extractive text summarization and abstractive text summarization, when combined, they are known as a hybrid approach. The extractive text summarization approach is dissimilar to the abstractive text summarization approach. Several researchers have focused their literature study on extractive text summarization summarization approaches. In this article, the proposed approach use extractive text summarization techniques.

In this paper, we focus on the extractive text summary based on textual graph-based extractive text summarization (TGETS) approach. The textual graph is created from a single documents. The graph's vertices represent the sentences of the text document, and edges represent the common words between two sentences. Several approaches have opted for the extractive text summarization (ETS) process. Subsequently, the Latent Semantic Analysis (LSA) [12, 19, 47], PageRank [11], TextRank and LexRank [13, 30], Graph-based approach [11, 12], Hidden Markov Models [52], and frequency-based term weight approaches [1, 16] are used in ETS summarization. ROUGE evaluation metrics compare two summaries (such as reference and system-generated summary) to identify the best possible summary. Sentences with the most common words are considered related and given higher priority. Similar sentences are deemed redundant, and one of them is ignored while preparing the summary. The objective of this research is to summarize the large news article of different domain such as sport, business, entertainment, technical, politics in very concise and informative way.



Summarization reduces the time for accessing and understanding the large documents. To achieve this objective, the following contribution are given below.

- We find the keyword from each sentence of single document with the help of preprocessing tool. After that, the root words are generated in sentences by lemmatization process and these root words help to generate textual graph of the single document.
- We propose an approach for computation of common words between two sentences and assign weight to the edges accordingly. Also, the computing score for each sentence (node of the textual graph) is formalized afterwards.
- We propose a method for computing average weight of the textual graph of the single document. This average weight is then used to generated summary by elimination sentences from the document.
- We calculate the result of summarizing the document by using ROUGE-metric, and results of state-of-the-art (i.e., TextRank (TR), KUSH (KH), LexRank (LR), and PageRank (PR)) summary are compared with the proposed approach of the experimental results.

The rest of this paper is structured as follows: Section 2 deals with related works of ETS. Section 3 gives a proposed textual graph-based extractive text summarization (TGETS) approach. Section 4 discuss experimental setup and result analysis based on experiments. At last concludes the paper and highlights future directions.

## 2 Related work

The most frequent technique for automated ETS summarization is ranking sentences or phrases and generating summaries. The majority of the current approaches have used sentence ranking. Graph, phrase, and word ranking are the three types of ranking methodologies. Ranks are calculated using sentence ranking algorithms. These algorithms use the relevant sentence as their aide to create ranks. Frequent words are given higher priority. Also, objects, proper nouns, and locations are given higher priority. The formal qualities of the phrase (underlined, quotation, italicized, typography, emphasis, emboldened) are considered in text ranking algorithms. Furthermore, sentences beginning with phrases like "As a result," "Finally," and "Briefly" is defined as assigned phrases throughout the text and the subsequent statements in these sentences are designated as crucial sentences. Similarly, the title of the content (text) to be summarized is used to evaluate it. Sentences with terms from the title are deemed to be added to the summary. The proportions of sentences are also considered by sentence ranking algorithms, with more significant sentences being given more weight. Sentences are given weightage based on their position and whether or not they contain numerical values. Elbarougy et al. [11] described an Arabic-specific ETS summarization method. The authors presented a graph-based document representation model with sentences as vertices. The Modified PageRank (MPR) method is used, with an initial score of the number of nouns in this sentence given to each node. The cosine similarity of two words is used to calculate the weight of each edge between them. The suggested method has three primary steps: pre-processing, feature extraction, and graph formation, followed by applying the new MPR algorithm and creating a relevant summary. Roul [41] suggested an ETS method for the Hindi language. They tagged lexical and meaningful information from Hindi novels and stories utilizing topic modeling and LDA. There is a lack of corpus and processing tools for Hindi, authors created their own corpus and tools. Experiments conducted result in the best outcomes when compared to baseline and definitive topic modeling methods. The authors (Nandhini and Balasundaram [36]) detailed the creation and evaluation of an extractive sum-



mary strategy to assist learners with reading challenges. Text analysis algorithms commonly use graph-based representations because they offer very effective solutions. The authors presented TextRank (Mihalcea and Tarau [30, 31]), which includes a graph-based model for ETS summarization based on text document intersections. LexRank, a node centrality approach based on eigenvector centrality, was introduced by Erkan and Radev [13]. The PageRank (PR) (Brin and Page [7]) technique, introduced to obtain central sentences in a document utilizing mutual information between sentence sets and words, inspired both the LexRank (LR) and TextRank (TR) methods. Parveen et al. [38] used the LexRank and TextRank methods. Uçkan and Karcı [49] proposed KUSH pre-processing tools and maximum independent sets (MIS). KUSH (KH) tool performs closed-meaning words which differ from other alternative search words. MIS has removed the vertices from the textual graph to generate a relevant summary.

Canhasi and Kononenko [8] performed query-focused multi-document summarization (Q-MDS) using weighted Archetypal Analysis, a matrix factorization technique. The artificial data set was displayed as an undirected sentence similarity network, where nodes represented sentences, edges represented similarity between connected nodes, and each phrase was related to the given query. Salton et al. [43] used link creation for automated document summary and characterized texts with graphs. They defined the structure by analyzing the documents' text relationships and compared the summary to reference generated summary by human's. Medelyan [28] proposed a graph-based method to provide semantic continuity, with nodes representing document concepts and edges indicating semantic linkages between them. The longest and shortest pathways are described as the strongest and weakest links, respectively after a graph diameter computation is conducted for all nodes in the graph. Local similarities were used to create nodes and edges, whereas graph topologies and documents were produced by Chen et al. [9]. Although most authors have concentrated on ETS, some have succeeded with abstractive summarization too. The RNN structure was used to do abstractive multi-sentence summarization in Nallapati et al. [35]. Similarly, Moawad and Aref [32] did abstractive summarizing works. Belwal et al. [6] discussed the similarity between nodes of the textual graph and the weight of graph edges. Authors calculated the rank of sentences through TextRank algorithms, and these ranks are kept in descending order. The compression ratio (CR) generates a relevant summary from the input documents taken from two datasets, Opinosis (total 51 documents) and CNN/DailyMail News (related to technical articles, social, and political). Azadani et al. [4] discussed graph-based biomedical text summarization using sentence clustering and itemset mining. Authors generated a meaningful summary and evaluated the result of the summary by ROUGE metric from the huge number of datasets. A brief summary of the literature analysis is also provided in Table 1.

On the study of the above-related work, following are the research gaps related to text summarization.

- For single-document text summarization, there has been few research that uses a graphbased approach and relatively few works have tried to use edge-weighted method to determine the most appropriate relevant sentences of the text document.
- 2. In the previous work, redundancy still exists in the summarized document. This leads to reduce the quality of summary.
- The earlier developed method does not use the benefit of common-word edge weight to find the most significant sentence.
- The task of cutting down on document processing and summarization time has yet to receive much focus.
- 5. Most of the existing work take more time even for a small summary generation.



Table 1 Literature Survey of ETS approaches

Authors, Year	Model/Approach	ToD (S/M)	ToS	Datasets
Canhasi and Kononenko [8]	Matrix Factorization and Graph-based Methods	M	Query-Focused	DUC-2005, DUC-2006
Rani and Lobiyal [40]	LDA tool	S	Extractive	Hindi novels (Munshi Premchand's)
Nasar et al. [37]	Itemset and graph Clustering	S	Extractive	DUC-2002, DUC-2004
Nallapati et al. [35]	Recurrent Neural Network	M	Abstractive	CNN/DailyMail, DUC-2002
El-Kassas et al. [12]	Statistical Approach	S	Extractive	DUC-2001, DUC-2002
Erkan and Radev [13]	Eigen Centrality and Graph-based Methods	M	Extractive	DUC-2004
Roul [41]	PageRank	S, M	Extractive	DUC-2002, DUC-2006
Nandhini and Balasundaram [36]	Machine Learning	S	Extractive	Educational Data
Parveen et al. [38]	ILP and Graph-based Methods	S	Extractive	DUC-2002
Uçkan and Karcı [49]	KUSH Tool/Eigen Vector Centrality	S	Extractive	DUC-2002
Salton et al. [43]	HLGA	M	Abstractive	Encyclopedia Article
Medelyan [28]	Lexical Chain and Graph-based Method	S	Key phrases Extraction	Offline Document Data
Chen et al. [9]	Random Walk and Graph-based Method	∞	Key Term Extraction	Mandarin and the Sinica Taiwan English corpus
Moawad and Aref [32]	Semantic Graph Reducing	S	Abstractive	None
Belwal et al. [6]	Topic Modeling	S	Extractive	CNN/DailyMail, Opinosis
Azadani et al. [4]	TGraph Clustering & Frequent Itemset/TextRank	S	Extractive	Biomedical articles
Tomer and Kumar [48]	Genetic Algorithm (GA)	M	Extractive	DUC-2002, DUC-2003, DUC-2004
Awan and Beg [3]	Top-Rank and Graph-based Methods	S	Key-phrases Extraction	KDD
Mutlu et al. [34]	Machine Learning	S	Extractive	SIGIR -2018
Al-Sabahi et al. [2]	Hierarchical Structured, Self-Attentive Model	S	Extractive	CNN/DailyMail, DUC-2002
Fang et al. [14]	Graph-based Method	S	Extractive	News Article and DUC-2002
Fattah and Ren [15]	FFNN, PNN, MR, GMM, and GA-based models	M	Extractive	DUC-2001
H O - F T T C - F C - F C - F		1		

ToD Type of Document, ToS Type of Summarization, S Single document, M Multi-document



Section 3 provide more detail about the textual graph-based extractive text summarization approach.

## 3 Proposed textual graph-based extractive text summarization (TGETS) approach

We propose a textual graph-based extractive text summarization based on a single document summarization methodology for extracting meaningful summary from the input document. There are three key phases to the proposed document summarization approach such as preprocessing, processing, and post-processing, i.e., shown in Fig. 2. In the first phase, preprocessing concerns with paragraph segmentation, sentence segmentation, word tokenization, and elimination of stop-word. After that finding root words based on the lemmatization process. In the second phase, there are several sub-steps, such as creation of textual graph, the common word between two sentences forms the basis of connectivity between the sentences (i.e., edges of the textual graph), and the computation sum of weight of each sentences  $S_i$ , and compute the average weight of textual graph ( $G_T$ ). In last post-processing phase, the selection of sentences based on the average weight of textual graph followed by sentence order. It generates a summary based on the top N phrases at this stage of the proposed technique, and N-word (viz., 100-words, 150-words, 200-words, etc.) summaries are prepared independently.

## 3.1 Text Pre-processing

The vast majority of dense datasets are unconfigured, and just a tiny percentage of essential datasets are structured. Structured datasets may be stated in a table's rows and columns or use several tags. Ignoring complex and time-consuming processes in the current investigation made it possible to provide a specific structure to the data. Some pre-processing is required

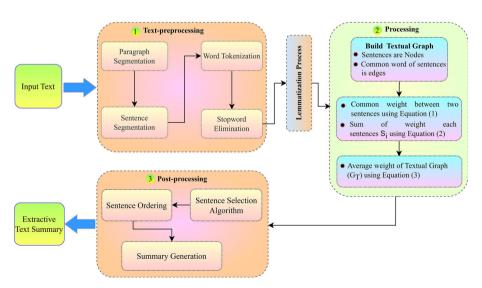


Fig. 2 Architecture of text processing for ETS summarization



for datasets that lack specified integrity yet must be structured. Since dense clusters exist in natural language, it is projected that translating texts to useable formats and isolating them from non-discriminatory data will grow the system's performance. The data to be analyzed in text summarization procedures must be pre-processed. Stop words (conjunctions, pronouns, prepositions) are expressions with no identifying properties and should be deleted before summarizing the dataset. As a result, non-representative terms inside sentences are eliminated from the original datasets, so text summarization can be done by converting the data to a suitable format for analysis. As a result, the processing load is reduced, but certain words are still utilized. Text can be conveyed with graphs and is saved in files with the .txt extension. The BBC News article datasets are utilized in this study. The normalization procedures in this study are carried out using the python language library and tags, which include removing spaces, stop words, and unnecessary characters, i.e., shown in Fig. 2. The data pre-processing and preparation stage begins with these normalization steps.

The pre-processing methods include paragraph segmentation, sentence segmentation, tokenization of words, and stop-word elimination. Most of these strategies are often utilized in an ETS system's pre-processing phase [26, 45, 50, 53].

**Paragraph segmentation** In general, an input text corpus is a collection of paragraphs or sections separated by the user. Each paragraph has its own set of main points, and a varied summary is built by merging the most relevant components from each paragraph [40].

**Sentence segmentation** It separates the sentences of a paragraph into sentences [16]. In many circumstances, utilizing end markers like ".", "?"or "!" to split sentences isn't appropriate. Words like "e.g.,", "i.e.,", "31.5", "Mr.", "Dr.", or "etc." lead to the incorrect detection of sentence borders if we rely on these markers. Regular expressions and basic heuristics address this problem [18, 24].

**Word tokenization** It separates the text into individual words. White space, a dot, a dash, a comma, and other symbols are used to divide words [18]. Example: "Humans are at risk from Covid-19 virus." like ["Humans", "are", "at", "risk", "from", "Covid-19", "virus"], these sentences have a total of seven tokens [46].

**Stopword elimination** Stopwords include auxiliary verbs, prepositions, pronouns, articles, and determiners. They have been left out because they do not add anything to the analysis [20] and have no bearing on how the essential sentences are chosen [16, 46]. In English languages, almost 179 stopwords are there, such as ["he", "she", "our", "am", "they", "where", "have", "can", "could", "may", etc.]. In the above example, three stopwords ["are," "at," "from"] are available; hence, they are eliminated so that sentence behaves as "Human's risk Covid-19 virus".

## 3.2 Process of root-word conversion using lemmatization method

It is the process of putting together the inflected elements of a word so that it can be identified as a single element, known as the word's lemma or meaningful vocabulary form. This is similar to stemming but gives meaning to specific words [23]. It combines content with similar meanings to a single word in simple terms [39], as shown as Fig. 3.

Example: (1) Form= "studies"  $\rightarrow$  Meaningful-information =  $3^{rd}$  person  $\rightarrow$  singular number  $\rightarrow$  present tense of the verb study  $\rightarrow$  lemma word = "study".



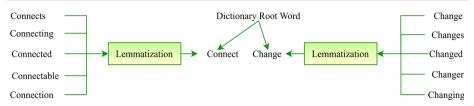


Fig. 3 Representation of keywords through lemmatization process

(2) Form= "studying" → Morphological-information = Gerund of verb study → Lemma = "study".

Lemmatization is the process of converting numerous keywords into dictionary root-words. Table 2 represent several root-words and keywords similar to Fig. 3. These type of root-words are used for connecting two vertices (i.e., two sentences) via a common term that is more useful during the textual graph construction.

Flow chart of lemmatization process According to the flow chart of lemmatization, we can convert the input words into root-words using the database of dictionary words. Its conversion is based on dictionary rules and then provides actual root-words. Lemmatization process always produces meaningful root-words. In this paper, the graph creates an association of two nodes through the common root-word of the two nodes (i.e., two sentences). The conversion of root-words by lemmatization process is shown in Fig. 4 and Algorithm 1.

Furthermore, when building graphs of closely related words that differ in spelling but are semantically derived from the similar root-words are treated as separate words. This makes it more laborious to discern interconnections and associations between the sentences.

## 3.3 Creation of weighted textual graph

In this subsection, a textual graph has been created; the textual graph presents several ways of representing information through weighted and non-directional graphs. The data undergoes pre-processing steps before being used to create the textual graphs. The proposed document summarization model constructs textual graph after data pre-processing and lemmatization. This procedure is shown in the "text processing and building of textual graph" stages of Fig. 2. Figure 5(a) and (b) represent a textual graph for a single text document. The textual

 Table 2 Other lemmatization examples of root words and keywords

Root-word	Keywords			
Study	Study, Studies, Studying, and Studied			
Trouble	Trouble, Troubling, Troubled, and Troubles			
Principle	Principle, Principalities, Principality, and Principles			
Affect	Affect, Affection, Affected, Affecting, Affectation, and Affects			
Change	Change, Changeable, Changes, Changing, Changed, and Changer			
Connect	Connect, Connection, Connecting, Connected, Connects, Connectable, and Connector			
Multiple	Multiplier, Multiply, Multiplied, Multiplying, Multipliable, Multiplies, Multiplicate, Multiplication			



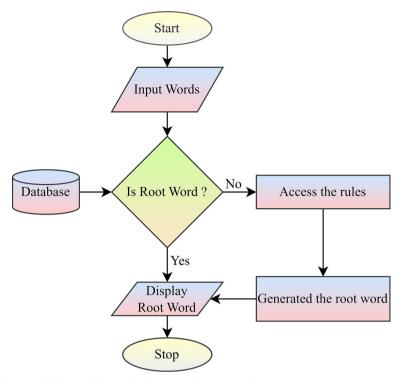


Fig. 4 Systematic diagram of lemmatization process for root-words

graph can be represented as  $G_T$ =(V, E), where  $V \in (v_1, v_2, v_3, ..., v_{n-1}, v_n)$ , and  $E \in (e_1, e_2, e_3, ..., e_{n-1}, e_n)$ . It is a weighted undirected graph, i.e., calculating the intersection of words in between sentence with all other sentences reveals the relationship levels of the sentence pairs  $S_i$  and  $S_j$  is the same as between  $S_j$  and  $S_i$ . The weight of edges has been decided by common words between sentences using (1). The sentences are represented as vertices of the textual graph. The vertex/node values in the set (S) on the textual graph ( $G_T$ ) are connected in an undirected manner. Graphs are stored in an adjacency matrix, where the size of the adjacency matrix is  $N \times N$ . The values of the adjacency matrix are the weight of edges in between two sentences. Complete textual graph are treated as dense matrix whose time complexity is  $O(N^2)$ . Otherwise, the textual graph is a sparse matrix. In the sparse matrix are a smaller number of edges than dense matrix, where the time complexity of textual graph is O(V+E) [10, 22, 51], where vertices (V) is the total number of sentences (S=N) such that E=N then  $O(N+N) \approx O(2N) \simeq O(N)$ . Therefore, worst and best time complexity for the document are  $O(N^2)$  and O(N), respectively.

## (a) Compute common weight between two sentences in the textual graph

Calculate the common weight between  $S_i$  and  $S_j$ . Its edges are determined by the intersection ( $\bigcap$ ) of the sentences  $S_i$  and  $S_j$ . This weight reflects the thickness of the graph edges or their weight. Figure 5(b) illustrates the circular weight graph is used to represent the weighted values of the thickness graph. A general mathematical formula is mentioned in (1) and also detail discuss in Algorithm 2.

Weight of 
$$e(S_i, S_j) = set\ of\ keywords\ (S_i) \cap set\ of\ keywords\ (S_j)$$
 (1)



## Algorithm 1 Find the root keywords using lemmatization techniques

```
Input: Provide input clean sentence (i.e., keywords of sentences) from the text documents D
   Output: Display root keywords
 1 begin
 2
        Dictionary-based rule= [prefix, suffix, infix];
        Vocabulary = [100000 root-words] /* At least 100000 root-words are
 3
            available in the Database file
 4
        Input vocabulary = check input vocabulary (Input keywords, vocabulary)
 5
        if input vocabulary == actual keywords then
           return root word:
 6
 7
        else
 Q
            for rule in rules do
                x = find root - word (Input keywords, rule);
10
                Input vocabulary= check input vocabulary (x, vocabulary);
11
                if input vocabulary == actual keywords then
12
                    return root-word
13
                    break:
                else
15
                    continue;
                end
16
                root-word = root-word;
17
                return root-word
18
19
            end
20
            root-word = root-word:
            return root-word
21
22
        return root keywords
23
24 end
```

## **Algorithm 2** Computation of edge weight between two sentence in Textual graph $(G_T)$

```
Input: Set of keywords for each nodes S_i in Graph 'G', where i=1 to n, and using Algorithm 1.
   Output: Weight of each edges e(S_i, S_i)
 1 begin
        Initilize weight of each edges, e(S_i, S_i)=0;
 2
        for i=1 to n do
 3
 4
            for j=i+1 to n do
                 if i not equal j then
 5
                      Compute e(S_i, S_i) using (1);
 6
                 else
 8
                     e(S_i, S_i)=0;
                 end
10
             end
        end
11
12
        return edge weight, e(S_i, S_i)
13 end
```

where  $\bigcap$  represent the common word between two sentences are called as edge weight of textual graph.

### (b) Weight of each sentence $S_i$ in textual graphs

Consider the text graph's weight in relation to the node (the document's sentences). The following textual graph (from Fig. 6) illustrates the specifics of (2) and also, it is discussed



through Algorithm 3.

$$W(S_i) = \sum_{j=i+1}^{n} S_{ij} \tag{2}$$

## **Algorithm 3** Computation of weight of each sentence in Textual Graph $(G_T)$ )

```
Input: Weight of edges in Graph 'G', using Algorithm 2.
  Output: Weight of each node S_i, (W(S_i)).
1 begin
2
       Initilize each node weight W(S_i)=0, where i=1, 2, ..., n;
3
       for i=1 to n do
4
           for j=i+1 to n do
5
               Compute weight of each sentences S_i (W(S_i)) using (2);
6
           end
7
       end
8
       return W(S_i)
9 end
```

## (c) Average weight of Textual Graph $(G_T)$

Determine the score (weight) of each sentence in the text document to determine the average weight of the textual graph. It requires an integer value for the textual graph's average weight. Once the values are maximized and equal to the sentences' weight values, the mathematical condition is represented in (3).

$$AW(G_T) = \left\lceil \frac{\sum_{i=1}^{n} W(S_i)}{N} \right\rceil$$
 (3)

```
Algorithm 4 Average weight of Textual Graph (G_T)
```

```
Input: Weight of each node W(S_i), where i=1, 2, ..., n; using Algorithm 3.
  Output: Average Weight of textual graph, (AW(G_T)).
1 begin
       Initilize weighted_sum=0;
2
3
       for i=1 to n do
4
       weighted_sum=weighted_sum+W(S_i);
      end
5
      AW(G_T) = \left[\frac{weighted\_sum}{N}\right]
6
7
       return AW(G7
8 end
```

when nodes (sentences) of the textual graph  $(G_T)$  weight are less than the average weight of the graph  $(G_T)$ . So that we pick the better sentence from the text document for the creation summary. Its mathematical condition is shown in (4) and it is described detail in Algorithm 4.

$$W(S_i) < AW(G_T) \tag{4}$$

Algorithm 5 is performed for textual graph-based extractive text summarization (TGETS). The proposed TGETS steps are described in Algorithm 5.



## **Algorithm 5** Proposed algorithm of textual graph-based extractive text summarization (TGETS)

Input: Main keywords of text Document, D

Output: Extractive text summary

- 1 begin
- Find the set of keywords in each sentence  $(S_i)$  in Document, D; //call Algorithm 1
- Find the common keywords between each sentence  $S_{i,j}$ , where  $i \in \{1, 2, ..., n \text{ and } j \in \{1, 2, ..., n \text{ for the computing edge weight between } S_{i,j}, //\text{call Algorithm 2};$
- 4 Compute the weight of each sentence  $S_i$ , //call Algorithm 3;
- 5 Compute the average weight of the document, //call Algorithms 2 and 4;
- All sentences  $S_i$  whose weight is less than the average weight of the document, discard sentence from the document;
- Generate a summary of document  $D_i$  by arranging all the sentences whose score is greater than the average weight of the document;
- 8 Summary generated based on the number of words, such as 100-, 150-, 200-, 250-, 300-, and 350-word length;
- 9 return Extractive text summary

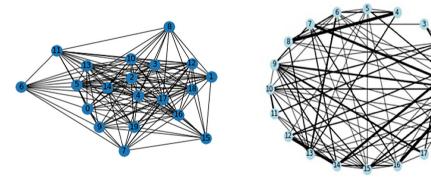
#### 10 end

11 terminated

## 3.4 Post-processing of text document

After the computation of the average weight of textual graph of each node, the next step is to generate the summary. The user decides the summary length in terms of number of words (X) (like 100-word, 200-word, 300-word, etc.), i.e., the number of words between document size and length of the summary generator. The number of sentences constituting the summary vary depending on the length of the individual sentence. A sentence having more rank is treated as the more important sentence in constituting the summary. Thus, we sort the nodes (sentences represented as nodes) in descending order of ranks, depending upon the limitation of summary length (decided by the user). We extract up the top-X number of words in document sentences and arrange them in the proper sentence order of the document, i.e., a quality summary of the single document.

For better sake of understanding of the above algorithm, it has been illustrated by an example. A textual graph  $G_T = (V, E)$  consists of a set of vertices (V) and edges (E) [55],

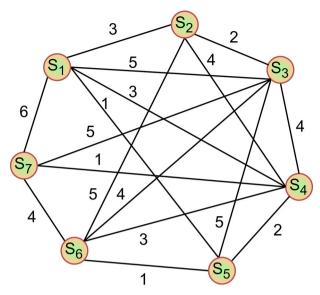


(a) Random generated graph

(b) Circular generated graph

Fig. 5 Graphs (a) and (b) generated from the same input document





**Fig. 6** Representation of weighted Textual Graph  $(G_T (V, E))$ 

where the set of vertices of the graph is sentences of a document and edges (common word) in between two sentences. Figure 6 shows the document's 7-sentences ( $S_1$ ,  $S_2$ , ...,  $S_7$ ), and the weight of the edge between two sentences are common words.

The common words between two sentences are calculated by (1), i.e., the weight of edges. There are seven sentences ( $S_1$ ,  $S_2$ , ...,  $S_7$ ), where each sentence's weight is calculated based on weight of edges between two sentences which is shown in Fig. 6.

$$W(S_1) = S_1S_5 + S_1S_4 + S_1S_3 + S_1S_2 + S_1S_7 = 1 + 3 + 5 + 3 + 6 = 18$$

$$W(S_2) = S_2S_1 + S_2S_3 + S_2S_4 + S_2S_6 = 3 + 2 + 4 + 5 = 14$$

$$W(S_3) = S_3S_1 + S_3S_2 + S_3S_4 + S_3S_5 + S_3S_6 + S_3S_7 = 5 + 2 + 4 + 5 + 4 + 5 = 25$$

$$W(S_4) = S_4S_1 + S_4S_2 + S_4S_3 + S_4S_5 + S_4S_6 + S_4S_7 = 3 + 4 + 4 + 2 + 3 + 1 = 17$$

$$W(S_5) = S_5S_1 + S_5S_3 + S_5S_4 + S_5S_6 = 1 + 5 + 2 + 1 = 9$$

$$W(S_6) = S_6S_2 + S_6S_3 + S_6S_4 + S_6S_5 + S_6S_5 + S_6S_7 = 5 + 4 + 3 + 1 + 4 = 17$$

$$W(S_7) = S_7S_1 + S_7S_3 + S_7S_4 + S_7S_6 = 6 + 5 + 1 + 4 = 16$$

Calculate the average weight of the textual graph (from Fig. 6)

$$AW(G_T) = \left\lceil \frac{W(S_1) + W(S_2) + W(S_3) + W(S_4) + W(S_5) + W(S_6) + W(S_7)}{7} \right\rceil$$

$$AW(G_T) = \left\lceil \frac{18 + 14 + 25 + 17 + 9 + 17 + 16}{7} \right\rceil$$

$$AW(G_T) = \left\lceil \frac{116}{7} \right\rceil = \lceil 16.571429 \rceil$$

$$AW(G_T) = 17$$



Now, we can eliminate the less important sentences from the text document based on an average weight of sentences and their weight of sentences using (4), such as,

$$W(S_2), W(S_5), W(S_7) < W(S_1), W(S_3), W(S_4), W(S_6)$$

According to the example, the values of  $W(S_2)$ ,  $W(S_5)$ ,  $W(S_7)$  are lower than  $AW(G_T)$ . It is eliminated from the text document since it does not meet the criterion for the average weight of the textual graph. Other weight of sentences are  $W(S_1)$ ,  $W(S_3)$ ,  $W(S_4)$ ,  $W(S_6)$  then user generates a summary from the important sentences-based weight of sentences  $S_1$ ,  $S_3$ ,  $S_4$ ,  $S_6$ . These weights of sentences are put into descending order of weight sentences. The user-definable summary is based on the number of words summarized from the remaining sentences after they hold the criterion of the average weight of  $G_T$  to generate a relevant summary of the text document.

## 4 Experimental setup and result analysis

The detail experimental setup is performed on the computer with the processor (an Intel (R)  $Core^{(TM)}$  i5-1035G1  $10^{th}$  Gen.) and CPU (Central Processing Unit) @ 1.19 GHz, 8.00 GB RAM size, Ubuntu 21.04 using Jupyter Notebook (Python3.6). The texts in the BBC news article dataset are saved in .csv files. The Python language library and tags is used to perform the normalization procedures, including removing unwanted characters, whitespace, expressions, and non-discriminatory words known as stop words. Also, we discuss details of dataset in next subsection.

## 4.1 Description of dataset

The BBC-article dataset is used in two major sections; one is reference article and other one is its corresponding reference summary. In the BBC-article dataset, there are multiple articles on different domain with their respective reference summaries. News articles are given in different contexts, including entertainment, sport, business, etc. The details about the BBC-article dataset are listed as part of Table 3.

This paper summarizes the BBC news articles' document using index data value on ten positions of entertainment articles', with 25 sentences and 533 words used to summarize the documents.

Table 3	The descrip	tion of BE	C-article	dataset
---------	-------------	------------	-----------	---------

Dataset Name	Deatils	Brief descrip	otion of datasets
BBC-article (total 2225 articles)	Domain-Name	Reference Article	Reference Summary
	Entertainment articles	386	386
	Sport articles	511	511
	Politics articles	417	417
	Business articles	510	510
	Technical articles	401	401



## 4.2 Evaluation performance metric

The ROUGE metric is regarded as the gold standard for measuring the quality of generated summaries with the reference summary. Here, both summaries are matched, and the score is calculated based on common content in both summaries. The match content refers to a number of uni-gram matching and bi-gram matched. These matching are termed as  $ROUGE_1$  and  $ROUGE_2$ , respectively [33, 40, 44–46, 53, 54]. Now on the basis of matching, we compute in terms of precision, recall, and  $F_1$ -score for  $ROUGE_1$  and  $ROUGE_2$  independently. Equation (5) is used to determine the ROUGE-metric for various granularities and discuss the following ROUGE-metric below [17, 50].

 $ROUGE_N$  ( $R_N$ ):  $R_N$  is based on N-gram comparison of a reference and candidate summary, where N=1, 2.

 $ROUGE_1$  ( $R_1$ ):  $R_1$  is based on uni-gram comparison of a reference and candidate summary.

 $ROUGE_2$  ( $R_2$ ):  $R_2$  is based on a bi-gram comparison of a reference and candidate summary.

$$ROUGE_{N} = \frac{\sum_{S \in (RefSumm)} \sum_{N-gram \in (S)} Count_{match}(N - gram)}{\sum_{S \in (RefSumm)} \sum_{N-gram \in (S)} Count (N - gram)}$$
(5)

$$ROUGE_L = \frac{LCS(P, Q)}{n}$$
 (6)

where N is the  $gram_n$  length, and  $Count_{match}$  (N-gram) is count of several numbers of n-grams present in the reference and candidate summary.  $ROUGE_N$  is evaluated by (5). In this case, the denominator equals the sum of the count of n-grams in the reference summary. Similarly, The  $ROUGE_L$  value also determines the longest common word sequence in the two sub-word sequences P and Q. Two-word sequences, P (i.e., reference summary length is n) and Q (i.e., candidate summary length is m) are supplied. Equations (7), (8), and (9) are used to calculate the  $ROUGE_L$  value of the sequences [1, 24, 33, 46, 50, 54].

$$R_{LCS} = \frac{LCS(P, Q)}{n} \tag{7}$$

$$P_{LCS} = \frac{LCS(P, Q)}{m} \tag{8}$$

$$F_{LCS} = \frac{(1 + \gamma^2).R_{LCS}.P_{LCS}}{\gamma^2.R_{LCS} + P_{LCS}}$$
(9)

where, LCS(P, Q) is the length of a longest common subsequence of P and Q, and  $\gamma$  is the ratio of  $P_{LCS}$  and  $R_{LCS}$ . In the next sub-section, we discuss about the results obtained and compare with the state-of-the-art methods.

## 4.3 Experimental setting

In this section, we discuss experimental work with state-of-the-art methods and perform the analysis in detail in the form of tabular as well as graphical ways. In the Appendix section, the input single text document and reference summary are given in Appendix A and B covers system generated summary of the given document on the number of words length provided by users. This has been done to show as an example for a better understanding of the proposed approach.



## 4.4 Described various methods

Here, we discuss various methods (such as LexRank (LR), TextRank (TR), PageRank (PR) and KUSH (KH)) used in the experimental section, which are discussed below in detail with mathematical formulas.

**LexRank (LR)** "The strength of the similarity link can be used to calculate LexRank. It generates the similarity network directly from the cosine values and frequently ends up with a considerably denser yet weighted graph. It has a stochastic matrix and normalizes the row sums of the appropriate transition matrix."

For weighted or unweighted graphs, the resulting equation is a modified version of LexRank and represented in (10).

$$L(V_i) = \left[ \left( \frac{d}{N} \right) + (1 - d) * \sum_{V_j \in adj(V_i)} \frac{W(V_i, V_j)}{\sum_{k \in adj[V_j]} W(k, V_j)} L(V_j) \right]$$
(10)

where  $L(V_i)$  = LexRank value of the sentence  $V_i$ , N = the total number of sentences (nodes) in the graph, d = empirically determined damping factor but it lies  $d \in [0...1]$ . by default, d=0.85,  $adj(V_i)$  = set of the sentences that are neighbors of  $V_i$  in the graph, and  $W(V_i, V_j)$  = the weight of the link bewteen sentence  $V_i$  and  $V_i$ .

**TextRank (TR)** "TextRank is a graph-based algorithm for text summarization and keyword extraction. It ranks words or phrases based on connections and patterns of co-occurrence within a text. The algorithm ranks the tokens in the text according to their scores, highlighting the most crucial ones for summary or keyword detection [30]."

The vertices  $(V_i)$  are connected to a set of vertices  $(V_j)$ . Here,  $V_i$  and  $V_j$  are sentences. Then the TextRank of vertices,  $T(V_i)$  is shown in (11) [27, 31].

$$T(V_i) = \left[ (1 - d) + d * \sum_{j \in V_i} \frac{T(V_j)}{V_j} \right]$$
 (11)

**PageRank (PR)** "The PageRank value for a page  $V_i$  is calculated by dividing the PageRank values for each page  $V_j$  in the set  $V_i$  (all pages linked to the page  $V_i$ ) by the number  $|V_j|$  of outbound links from the page  $V_i$  [7]".

The vertices  $(V_i)$  are connected to a set of vertices  $(V_j)$ . Then the PageRank of vertices  $(V_i)$  is shown in (12).

$$P(V_i) = \left[ \left( \frac{1 - d}{N} \right) + d * \sum_{j \in n}^{n} \frac{P(V_j)}{|V_j|} \right]$$
 (12)

**KUSH (KH)** Based on Uçkan and Karcı [49] concept that terms relating to the nodes in the independent set should be eliminated from the summary. The nodes forming the Independent Sets (IS) on the graphs were determined and erased from the graph. As a result, the evaluation of the summary was constrained before the nodes' impact on the global graph. Because of this



ROUG	E Metric	TGETS	TR	KH	LR	PR
$R_1$	Precision	0.98275	0.57857	0.89915	0.75164	0.79523
	Recall	0.81428	0.78641	0.76428	0.58362	0.45925
	$F_1$ -score	0.89062	0.66667	0.82625	0.65705	0.58225
$R_2$	Precision	0.92934	0.67607	0.82901	0.81931	0.60185
	Recall	0.74672	0.80126	0.69868	0.55720	0.57259
	$F_1$ -score	0.82808	0.73336	0.75829	0.66329	0.58686

 Table 4
 100-word length text summary (BBC News Article)

restriction, the summary could not repeat word grouping, resulting in more comprehensive summaries. The centrality values of the collected nodes were determined in the last stage using node centrality computations. This study employs eigenvector centrality to weigh the nodes of the textual graph (networks).

The experimental study is examined on BBC news article dataset and testing method is undertaken independently. It has been executed over 100-iterations for summaries of 100, 150, 200, 250, 300, and 350 words to completely analyze the proposed summarizing system's performance. The ROUGE performance measures are used to assess the proposed document summarization, as shown in Tables 4, 5, 6, 7, 8 and 9.

In 100 words length text summary, TGETS has the highest recall values than other existing state-of-the-art methods (i.e., TR, KH, LR, and PR) for ROUGE ( $R_1$ ), as shown in Table 4. Similarly, TGETS has the highest precision values than other methods for ROUGE ( $R_2$ ). However,  $F_1$ -score values corresponding to the ROUGE ( $R_1$  and  $R_2$ ) are 0.89062 and 0.82808, respectively.

In Table 5, all parameters (precision, recall, and  $F_1$ -score) corresponding to ROUGE ( $R_1$  and  $R_2$ ) are better for proposed approach (TGETS) than other existing state-of-the-art methods (i.e., TR, KH, LR, and PR).

In Table 6, the proposed approach produces better recall and  $F_1$ -score than existing state-of-the-art methods, but precision is not better than LR methods for both ROUGE ( $R_1$  and  $R_2$ ) metrics.

In Table 7, the proposed approach produces better results for evaluating ROUGE ( $R_1$ ) for all parameters (Precision, recall, and  $F_1$ -score). Still, for the evaluation of  $R_2$ : precision values are lower than LR, and other methods, such as TR, KH, and PR, are better. Similarly,

 Table 5
 150-word length text summary (BBC News Article)

ROUG	E Metric	TGETS	TR	KH	LR	PR
$R_1$	Precision	0.98013	0.71507	0.92414	0.84190	0.67321
	Recall	0.92500	0.60551	0.83750	0.65271	0.59203
	$F_1$ -score	0.95177	0.65575	0.87869	0.73533	0.63002
$R_2$	Precision	0.94619	0.68105	0.86916	0.57334	0.51702
	Recall	0.89029	0.73525	0.78481	0.82163	0.57839
	$F_1$ -score	0.91739	0.70711	0.82483	0.67539	0.54599



 Table 6
 200-word length text summary (BBC News Article)

E Metric	TGETS	TR	KH	LR	PR
Precision	0.73134	0.57021	0.71144	0.73628	0.69003
Recall	0.91875	0.84950	0.89375	0.70032	0.57660
$F_1$ -score	0.81440	0.68238	0.79224	0.71785	0.62824
Precision	0.67320	0.69972	0.66667	0.80127	0.61433
Recall	0.86919	0.72619	0.85232	0.69842	0.67884
$F_1$ -score	0.75875	0.71271	0.74815	0.74632	0.64498
	Precision Recall $F_1$ -score Precision Recall	Precision $0.73134$ Recall $0.91875$ $F_1$ -score $0.81440$ Precision $0.67320$ Recall $0.86919$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$

 Table 7
 250-word length text summary (BBC News Article)

E Metric	TGETS	TR	KH	LR	PR
Precision	0.62331	0.49375	0.53744	0.59372	0.45000
Recall	0.99285	0.74528	0.87142	0.76750	0.80000
$F_1$ -score	0.76584	0.59398	0.66485	0.66952	0.57599
Precision	0.58445	0.48484	0.48186	0.62626	0.45625
Recall	0.95196	0.96000	0.81222	0.52100	0.89024
$F_1$ -score	0.72425	0.64429	0.60487	0.56880	0.60330
	Precision Recall $F_1$ -score Precision Recall	Precision $0.62331$ Recall $0.99285$ $F_1$ -score $0.76584$ Precision $0.58445$ Recall $0.95196$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	Precision $0.62331$ $0.49375$ $0.53744$ Recall $0.99285$ $0.74528$ $0.87142$ $F_1$ -score $0.76584$ $0.59398$ $0.66485$ Precision $0.58445$ $0.48484$ $0.48186$ Recall $0.95196$ $0.96000$ $0.81222$	Precision $0.62331$ $0.49375$ $0.53744$ $0.59372$ Recall $0.99285$ $0.74528$ $0.87142$ $0.76750$ $F_1$ -score $0.76584$ $0.59398$ $0.66485$ $0.66952$ Precision $0.58445$ $0.48484$ $0.48186$ $0.62626$ Recall $0.95196$ $0.96000$ $0.81222$ $0.52100$

 Table 8
 300-word length text summary (BBC News Article)

ROUGE	Metric	TGETS	TR	KH	LR	PR
$R_1$	Precision	0.60392	0.56102	0.57563	0.65532	0.53602
	Recall	0.96250	0.79113	0.85625	0.69023	0.77391
	$F_1$ -score	0.74217	0.65649	0.68844	0.67232	0.63336
$R_2$	Precision	0.54293	0.47193	0.50409	0.54921	0.54791
	Recall	0.90717	0.72261	0.78059	0.69170	0.83785
	$F_1$ -score	0.67931	0.57097	0.61258	0.61227	0.66255

 Table 9
 350-word length text summary (BBC News Article)

ROUG	E Metric	TGETS	TR	KH	LR	PR
$R_1$	Precision	0.65258	0.53712	0.55932	0.60175	0.48570
	Recall	0.99285	0.88210	0.94285	0.77389	0.81073
	$F_1$ -score	0.78753	0.66768	0.70212	0.67705	0.60747
$R_2$	Precision	0.60387	0.59188	0.52405	0.53007	0.49662
	Recall	0.95196	0.84721	0.90393	0.79389	0.85005
	F <sub>1</sub> -score	0.73898	0.69689	0.66346	0.63569	0.62696



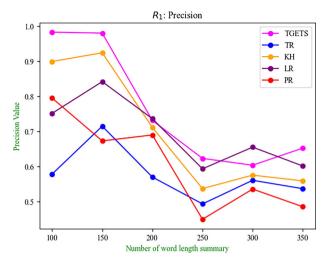


Fig. 7 Comparison of word length summary for parameter (Precision) under  $ROUGE_1$ 

the recall value is less than TR, and better than others (LR, KH, and PR). Finally, the proposed approach produced good results as compared to other state-of-the-art methods.

For 300-word length text summary (Table 8), recall and  $F_1$ -score parameters corresponding to ROUGE evaluation for  $R_1$  and  $R_2$  are better than other state-of-the-art methods. Still, the method of LR is higher than the proposed method's precision values in ROUGE ( $R_1$  and  $R_2$ ) metric.

For 350-word length text summary (Table 9), the proposed approach produces better performance than other state-of-the-art methods (TR, KH, LR, and PR), in terms of precision, recall, and  $F_1$ -score for ROUGE ( $R_1$  and  $R_2$ ) metric.

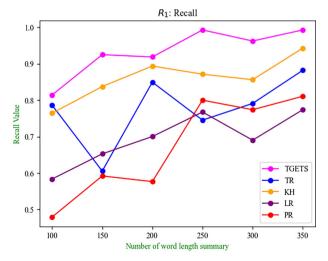


Fig. 8 Comparison of word length summary for parameter (Recall) under  $ROUGE_1$ 



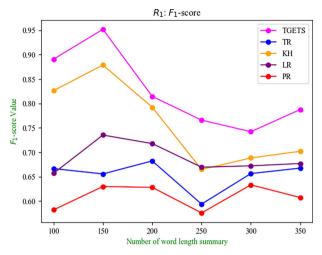


Fig. 9 Comparison of word length summary for parameter ( $F_1$ -score) under  $ROUGE_1$ 

All tabular results are represented in graphical way format (in terms of precision, recall, and  $F_1$ -score) to compare all methods such as proposed (TGETS), TR, KH, LR, and PR.

The line chart plotting for the ROUGE ( $R_1$ ) metric corresponds to the parameter of precision, recall, and  $F_1$ -score and the comparison between the proposed work and existing models, shown in Figs. 7, 8, and 9.

Figures 10, 11, and 12 represents the comparison of proposed and existing methods using the parameter of precision, recall, and  $F_1$ -score for the ROUGE ( $R_2$ ) metric.

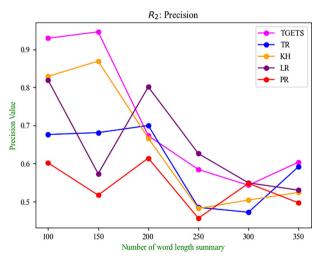


Fig. 10 Comparison of word length summary for parameter (Precision) under  $ROUGE_2$ 



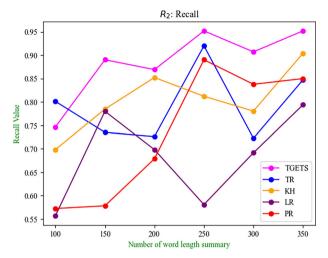
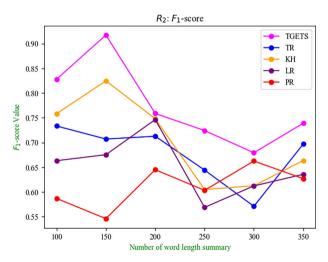


Fig. 11 Comparison of word length summary for parameter (Recall) under  $ROUGE_2$ 

## 4.5 Comparison with existing research

We compare our experimental results with TR, KH, LR, and PR to evaluate the effectiveness on the extractive text summarization. From all summarizers' (generated summary (users) and provided a summary (given)), various ROUGE scores are shown in Tables 4–9 and have a value of ROUGE ( $R_1$ ,  $R_2$ ) corresponding to the parameter precision, recall, and  $F_1$ -score. The results in Tables 4 to 9 compare various summary techniques according to the caliber of the summaries they produce. First, we compare the ROUGE ( $R_1$ ) metric for all size of word



**Fig. 12** Comparison of word length summary for parameter ( $F_1$ -score) under  $ROUGE_2$ 



length summaries (100-, 150-, 200-, 250-, 300-, and 350-words) for the precision, recall, and  $F_1$ -score measurement in Figs. 7–9. In between 100 to 200-word length, the summary varies by 30.82% in the precision values which shows that the proposed method generate good results compared to the TR method. The summary's overall percentage variation under recall value is 38.76% than PR method and that the overall variation in the  $F_1$ -score for summaries of 100-200 words is 30.73% than PR method. After that, variation in between 250-350-word length text summary: precision varies by 15.13% than TR method, recall varies by 24.31% than LR method, and  $F_1$ -score varies by 20.86% than PR method. In ROUGE ( $R_1$ ), overall summary length performance is improved than existing state-of-the-art methods.

For the ROUGE metric ( $R_2$ ), 100-200 words length text summary; the precision, recall, and  $F_1$ -score measurement in Figs. 10–12 are 32% than PR methods, 27% than PR method, and 29% than PR method, respectively. Similarly to evaluate the variation for 250-350-words length text summary, precision, recall, and  $F_1$ -score exceeds by 13.35% than PR method, 28.62% than LR method, and 15.21% than LR method, respectively. The proposed method improved the performance of the summary than the existing state-of-the-art methods.

## 5 Conclusion and future directions

Nowadays, a large volumes of data continue to grow, and some textual features must be gathered by analyzing document data to reduce the time required to access information. This fascinating endeavor has piqued scholarly interest in automatic summarizing systems that can assist end users in this field. This paper proposes a new unsupervised ETS algorithm to achieve the goal. Using a lemmatization that applies text summarizing through a unique method avoids abnormalities in text documents in the ETS approach. Lemmatization yields positive results in generating discrete and quantitative linkages between sentences. Common terms represent the second finite set, whereas sentences reflect the first finite set in the representation of a graph. As a result, non-directional and weighted graphs were used to implement the proposed text representation method. The sentence weight and average weight of graph are calculated in order to eliminate less important sentences from the text document. The summarizing method used in the offered techniques produces values sorted in increasing order, and the amount of text data they carried about the strings that make up textual graphs is quantified. The datasets collected from BBC News articles are extensively used in this field to test the proposed methodology. The influence of exponential transformation on recall-oriented ROUGE-metric  $(R_1, R_2)$  performance measures is demonstrated. For summaries of 100, 150, 200, 250, 300, and 350 words, the effect of using a polynomial time complexity algorithm is investigated. On an average 100 to 200-words length text summary, the proposed approach (TGETS)  $ROUGE_1$  value is better than other existing methods under the precision, recall and  $F_1$ -score, respectively. However, for  $ROUGE_2$ , 100 to 200-words length text summary perform better than others word length text summary in term of precision, recall and  $F_1$ -score. In the future, we will try abstractive text summarization using the LSTM techniques, neural network (NN), and fuzzy-logic-based approaches.



## Appendix A: Text document and reference summary of BBC news articles

Sentences	Sentences of the text document
$S_1$	Young book fans have voted Fergus Crane, a story about a boy who is taken on an adventure by a flying horse, the winner of two Smarties Book Prizes.
$S_2$	Paul Stewart and Chris Riddell's book came top in the category for six to eight year olds and won the award chosen by after-school club members.
$S_3$	Sally Grindley's Spilled Water, about a Chinese girl sold as a servant, was top in vote of readers aged nine to 11.
$S_4$	Biscuit Bear by Mini Grey took the top award in the under-five category.
$S_5$	Winners were voted for by about 6,000 children from a shortlist picked by an adult panel.
$S_6$	The prize, which is celebrating its $20^{th}$ year, is billed as the UK's biggest children's book award.
$S_7$	Fergus Crane includes text by Stewart and illustrations by Riddell, who also created The Edge Chronicles together.
$S_8$	As well as the six to eight prizes, it won the 4-Children Special Award voted for by after-school club members.
$S_9$	Julia Eccleshare, chair of the adult judging panel, said children's literature had "never looked stronger" in the prize's 20 years.
$S_{10}$	This award counts because the final choice of winners is made by children, who are the toughest critics of all," she said.
$S_{11}$	This year's young judges chose the winners from an exceptionally strong and varied shortlist which showcases the very best in children's books today.
$S_{12}$	Previous winners have included JK Rowling, Jacqueline Wilson and Dick King- Smith.
Sentences	Reference summary of text document
$S_1$	Young book fans have voted Fergus Crane, a story about a boy who is taken on an adventure by a flying horse, the winner of two Smarties Book Prizes.
$S_2$	Paul Stewart and Chris Riddell's book came top in the category for six to eight year olds and won the award chosen by after-school club members.
$S_6$	The prize, which is celebrating its $20^{th}$ year, is billed as the UK's biggest children's book award.
$S_8$	As well as the six to eight prizes, it won the 4-Children Special Award voted for by after-school club member.
$S_{11}$	This year's young judges chose the winners from an exceptionally strong and varied shortlist which showcases the very best in children's books today.



## Appendix B: Sample of system generated summary for BBC-news articles dataset from Appendix A text document

Sentences	System generated summary
$S_1$	Young book fans have voted Fergus Crane, a story about a boy who is taken on an adventure by a flying horse, the winner of two Smarties Book Prizes.
$S_2$	Paul Stewart and Chris Riddell's book came top in the category for six- to eight- year-olds and won the award chosen by after-school club members.
$S_5$	Winners were voted for by about 6,000 children from a shortlist picked by an adult panel.
<i>S</i> <sub>7</sub>	Fergus Crane includes text by Stewart and illustrations by Riddell, who also created The Edge Chronicles together.
$S_{11}$	This year's young judges chose the winners from an exceptionally strong and varied shortlist which showcases the very best in children's books today.

Data availability The dataset is available on demand.

## **Declarations**

**Conflict of interest** There is no potential for a conflict of interest.

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