

Q1

Demodulation of DSBSC using synchronous or coherent, and find the expressions for frequency error and phase error.

A

DSBSC - double side band suppressed carrier

→ Demodulation of DSBSC can be done in 2 types.

① synchronous (or) coherent detector.

② Costas loop.

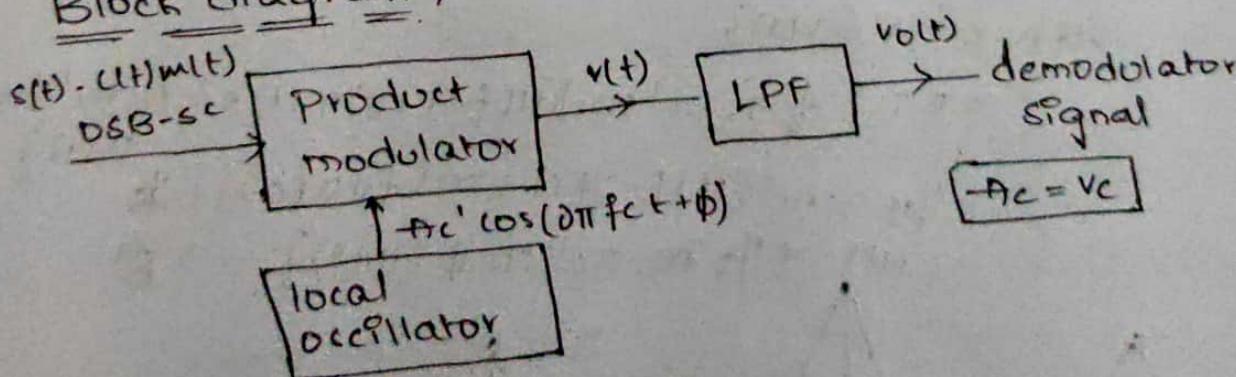
→ synchronous (or) coherent detector:

We know that, envelope of DSBSC modulated wave form is different than the msg. sig so we must employ coherent detection at a synchronous detection.

→ in this process to multiply the DSBSC modulated wlf with a locally generated sinusoidal waveform & then LPF. then original msg can be obtained.

→ it is assumed that local oscillator used as the detector (demodulation) is of same frequency and phase (ie coherent w.r.t oscillator etc) used in Tx & and in synchronous to it

Block diagram:



$$\text{w.k.t } s(t) = A_c \cos(2\pi f_c t + \phi)$$

$$\text{Product modulator} \Rightarrow v(t) = s(t) * L.O. (t)$$

$$\begin{aligned}
 \rightarrow v(t) &= s(t) A c' \cos[2\pi f_c t + \phi] m(t) \\
 &= A c' A c' \cos 2\pi f_c t + \cos[2\pi f_c t + \phi] m(t) \\
 &= \frac{A c' A c'}{2} [2 \cos 2\pi f_c t \cos[2\pi f_c t + \phi] m(t)] \\
 &= \frac{A c' A c'}{2} [\cos(4\pi f_c t + \phi) + \cos(\phi)] m(t) \\
 v(t) &= \frac{m(t)}{2} + \frac{A c' A c'}{2} \cos(4\pi f_c t + \phi) + \boxed{\frac{1}{2} A c' A c' \cos \phi m(t)}
 \end{aligned}$$

High frequency       $\hookrightarrow 0$       Low frequency

→ This  $v(t)$  from product modulator is sent to a lowpass filter which allows only low frequency signal to pass through it.

→ O/P of LPF

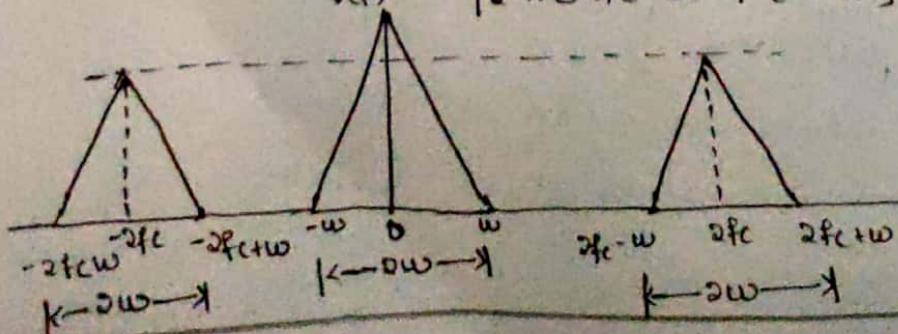
$$v_o(t) = s(t) \underset{\text{demodulator}}{=} \frac{A c' A c'}{2} m(t) \cos \phi \underset{\text{L} \rightarrow \mathbb{R}}{\hookrightarrow}$$

→ It is not compulsory that the oscillator produce the exact synchronous output carries same (or) signal each time. Hence it may produce 2 types of errors they are:

- ① phase error
- ② frequency error

from eq ①:  $v(f)$  can be obtained as

$$\begin{aligned}
 v(f) &= F.T \{ v(t) \} \\
 &= F.T \left\{ \frac{1}{2} A c' A c' \cos(4\pi f_c t + \phi) m(t) + \frac{1}{2} A c' A c' \cos \phi m(t) \right\} \\
 &= \frac{1}{4} A c' A c' [M(f - 2f_c) + m(f_c + 2f_c)] + \frac{1}{2} \\
 &\quad v(f) + \frac{1}{2} A c' A c' \cos \phi [m(f)] \rightarrow ② .
 \end{aligned}$$



→ Amplitude of demodulated signal is maximum difference iff  $\phi = 0$  minimum iff  $\phi = \pm\pi/2$

Note: when  $\phi = \pm\pi/2$  demodulated signal this is called quadrature Null effect in coherent detection.

Drawback due to QNE:

- the phase error  $\phi$  causes demodulator output to be attenuated by a factor of  $\phi$
- when  $\phi = \text{constant}$ , there is no distortion in demodulated o/p else if  $\phi = \text{randomly varying} \Rightarrow \cos\phi$  also varies randomly not desired
- so, a new ckt has to be provided to make sure that b.o in Rx works in perfect synchronisation w.r.t Carrier C(t) in Tx w.r.t frequency & phase this pt increases cost at DSBSC demodulator

$$s(t)_{\text{DSBSC}} = m(t) \cos(2\pi f_c t + \phi)$$

$$\begin{aligned} \text{Phase error: } s_i(t) &= s(t)_{\text{DSBSC}} * C(t) \\ &= A_C \cos(2\pi f_c t + m(t) + 2\pi Rf t + \phi) \\ &= \frac{A_C^2}{2} m(t) [2\cos(m(t) + 2\pi(f_c t + \phi))] \\ &= \frac{A_C^2}{2} m(t) [\cos(4\pi f_c t + \phi)] + (\text{DS} \phi) \\ &= \frac{A_C^2}{2} m(t) (\cos\phi + \frac{A_C^2}{2} m(t) \cos(4\pi f_c t + \phi)) \end{aligned}$$

Output after Lpc

$$s_i(t)_{\text{Demod}} = \frac{A_C^2}{2} m(t) \cos\phi$$

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Frequency error:-

$$\begin{aligned}s_1(t) &= s(t) DSBSC * c(t) \\&= A_c \cos 2\pi f_c t m(t) * A_c \cos (2\pi f_c t + \Delta f) \\&= \frac{A_c^2}{2} m(t) [2 \cos 2\pi f_c t \cos (2\pi f_c t + \Delta f)] \\&= \frac{A_c^2}{2} m(t) [\cos (4\pi f_c t + \Delta f) + \cos (\Delta f)] \\&= \frac{A_c^2}{2} m(t) \cos \Delta f + \frac{A_c^2}{2} m(t) \cos (4\pi f_c t + \Delta f)\end{aligned}$$

Output after BPF

$$s(t) \text{ demodulated} = \frac{A_c^2}{2} m(t) \cos \Delta f$$

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Amplitude of demodulated signal remains if  $\phi = 0$   
and min if  $\phi = \pm \pi/2$ .

19BDIA0482  
K. Srivastava

2Q

Demodulation of SSB-SC using synchronous or coherent detector and also find the expression for frequency error and phase error.

A

SSB-SC - (single side band - suppressed carrier)

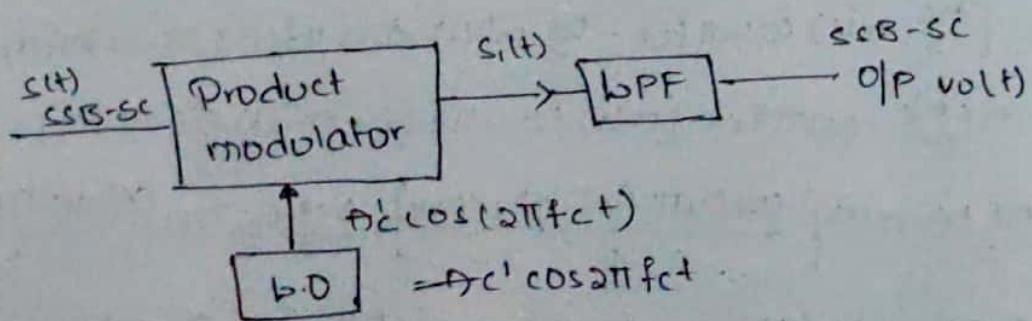
Coherent (or) synchronous detector of - SSB-SC :-

→ Demodulation of SSB is complicated since here carrier as well as one of the sidebands is suppressed when compared to DSB-SC.

→ Coherent detection is used where synchronization is needed in both frequency & phase hardware locally generated carrier in Rxer w.r.t carrier used in Txer

→ Although carrier is suppressed, yet info is embedded on carrier phase and frequency is present in side bands of modulated wave.

→ The 2 side bands are mirror images of each other



$$\text{W.K.T} \quad s(t)_{\text{SSB-SC}} = \frac{a_1}{2} [m(t) \cos 2\pi fct - m(t) \sin 2\pi fct]$$

$$m(t) = a_1 \cos(\alpha f t)$$

$$= a_1' \cos 2\pi fct$$

O/P of product modulator  $s_1(t) = s(t)_{\text{SSB-SC}} * (t)$ .

$$\begin{aligned}
 s_1(t) &= \left[ \frac{\alpha c}{2} m(t) (\cos 2\pi f_c t - \frac{\alpha c}{2} m^o(t) \sin 2\pi f_c t) + \alpha' c' \cos 2\pi f_c t, \right. \\
 &= \frac{\alpha c \alpha c'}{2} \cos^2 2\pi f_c t m(t) - \frac{\alpha c \alpha c'}{2} m^o(t) \sin 2\pi f_c t \cos 2\pi f_c t \\
 &= \frac{\alpha c \alpha c'}{4} m(t) + \frac{\alpha c \alpha c'}{4} \cos 2\pi f_c t m(t) - \frac{\alpha c \alpha c'}{2} m^o(t) \sin 2\pi f_c t \\
 &\quad \text{cos 2\pi f_c t.}
 \end{aligned}$$

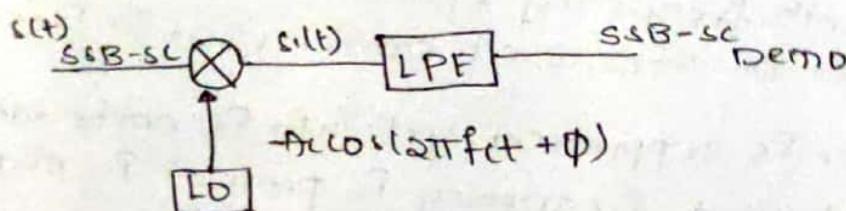
the OLPs sent to low pass filter which allows only low frequency & attenuates high frequency

$$\text{O/P of LPF } \Phi_c s(t)_{\text{SSB-SC}} = \frac{\alpha c \alpha c'}{4} m(t).$$

$$\text{Phase error: } -\alpha c \cos(2\pi f_c t + \phi)$$

$$\text{frequency error: } \alpha c \cos(2\pi f_c t + \Delta f)$$

### Phase error:



$$s(t)_{\text{SSB-SC}} = \frac{\alpha c}{2} m(t) \cos 2\pi f_c t - \frac{\alpha c}{2} m^o(t) \sin 2\pi f_c t$$

$$s(t) = \alpha c \cos(2\pi f_c t + \phi)$$

$$s_1(t) = \left[ \frac{\alpha c}{2} m(t) \cos 2\pi f_c t - \frac{\alpha c}{2} m^o(t) \sin 2\pi f_c t \right] + \alpha' c' \cos 2\pi f_c t$$

$$= \frac{\alpha c \alpha c'}{2} \cos 2\pi f_c t [m(t) \cos 2\pi f_c t - m^o(t) \sin 2\pi f_c t]$$

$$= \frac{\alpha c \alpha c'}{2} m(t) \left[ \frac{\cos(2\pi f_c t + \phi) + \cos \phi}{2} \right] - \frac{\alpha c \alpha c'}{2} m^o(t) \left[ \frac{\sin(2\pi f_c t + \phi)}{2} \right]$$

$$\begin{aligned}
 s_1(t) &= \underbrace{\frac{\alpha c \alpha c'}{4} m(t) + \frac{\alpha c \alpha c'}{4} m(t) \cos 2\pi f_c t}_{\text{desired}} - \underbrace{\frac{\alpha c \alpha c'}{4} m^o(t) \sin 2\pi f_c t}_{\text{undesired.}}
 \end{aligned}$$

O/P of LPF

$$s(t) = \frac{\alpha c \alpha c'}{4} (m(t) \cos \phi + m^o(t) \sin \phi)$$

Applying Fourier T/F

$$\begin{aligned}
 s(f) &= \frac{\alpha C A C I}{4} m(f) \cos \phi + \frac{\alpha C E C I}{4} m^2(f) \sin \phi \\
 s(f) &= \frac{\alpha C A C I}{4} m(f) \cos \phi + \frac{\alpha C E C I}{4} m(f) \left( \frac{1}{2} \operatorname{sgn}(f) \sin \phi \right) \\
 &= \frac{\alpha C A C I}{4} m(f) \cos \phi - \frac{\alpha C E C I}{4} m(f) \sin \phi \\
 s(f) &= \frac{\alpha C A C I}{4} m(f) e^{-j\phi} \Rightarrow \text{volt}
 \end{aligned}$$

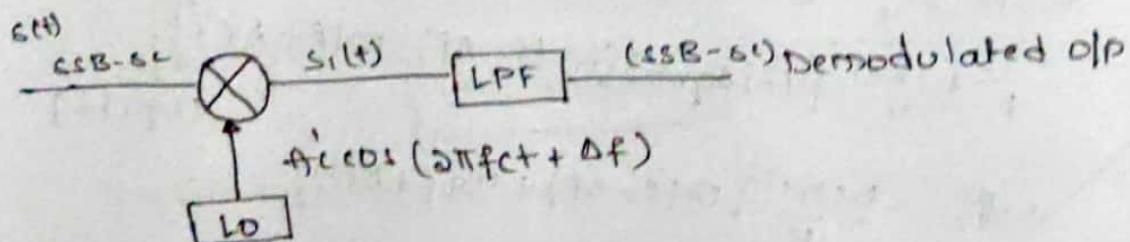
there is no quadrature null effect in coherent detection of SSB-SC

### Effects of phase and frequency error in SSB-Demodulation

→ for effective coherent detection Rx should generate coherent frequency and phase of carrier as that of Tx. This can be done by:

- a Using stable local oscillator at receiver
- b Providing pilot carrier along with SSB during Tx.

### b Frequency error:



→ It produces phase shift of  $+Q(\omega r) + \pi$  for the negative frequencies &  $-Q(\omega r) - \pi$  for the positive frequencies.

→ Let  $\Delta f$  be the frequency error. If locally generated carrier  $A_C \cos(\omega_1 t + \Delta f)t$  is used

$$s(t)_{SSBSC} = A_C/2 \cos(\omega_1 t) \cos \omega_1 fct - \frac{A_C}{2} m^2(t) \sin \omega_1 fct$$

$$c(t) = A_C \cos(\omega_1 fct + \Delta f)t$$

## O/P of Product modulator

$$\begin{aligned}
 s_1(t) &= s(t) + c(t) \\
 s_1(t) &= \left[ \frac{Ac}{2} m(t) \cos(2\pi f_c t - \frac{\pi c}{2}) + \sin(2\pi f_c t) A c' \cos(\omega \pi f_c t + \Delta f) \right] \\
 &= \frac{A(c A c')}{2} m(t) \cos(2\pi f_c t + \cos 2\pi (f_c + \Delta f) t - \frac{A c' \pi}{2} m^2(t)) \\
 &\quad + \sin(2\pi f_c t) \cos(\omega \pi (f_c + \Delta f) t) \\
 s(t)_{SIR-SC} &= \frac{A(c A c')}{u} m(t) [\cos(\omega \pi f_c t + 2\pi \Delta f) t + \cos 2\pi \Delta f t] \\
 &= \frac{A(c A c')}{u} m(t) [\sin(\omega \pi f_c t + 2\pi \Delta f) t - \sin 2\pi \Delta f t] \\
 &= \frac{A(c A c')}{u} m(t) \cos(\omega \pi f_c t + 2\pi \Delta f) t + \frac{A(c A c')}{u} m(t) \cos 2\pi \Delta f t \xrightarrow{\text{Desired}} \\
 &\quad - \frac{A(c A c')}{u} m(t) \sin(\omega \pi f_c t + 2\pi \Delta f) t + \frac{A(c A c')}{u} \sin 2\pi \Delta f t m(t) \xrightarrow{\text{Desired}}
 \end{aligned}$$

## O/P of low pass filter.

$$\begin{aligned}
 v_o(t) &= \frac{A(c A c')}{u} m(t) \cos 2\pi \Delta f t + \frac{A(c A c')}{u} \sin 2\pi \Delta f t m(t) \\
 &= \frac{A(c A c')}{u} [m(t) \cos 2\pi \Delta f t + m(t) \sin 2\pi \Delta f t]
 \end{aligned}$$

APPLY F.T

$$\begin{aligned}
 v_o(f) &= \frac{A(c A c')}{4} \left[ \frac{m(f - \Delta f) + m(f + \Delta f)}{2} \right] \\
 &\quad + \frac{A(c A c')}{u} \left[ (1 - i \sqrt{u}) [m(f - \Delta f) - m(f + \Delta f)] \right] \xrightarrow{j \in \mathbb{Q}, n \neq 1}
 \end{aligned}$$

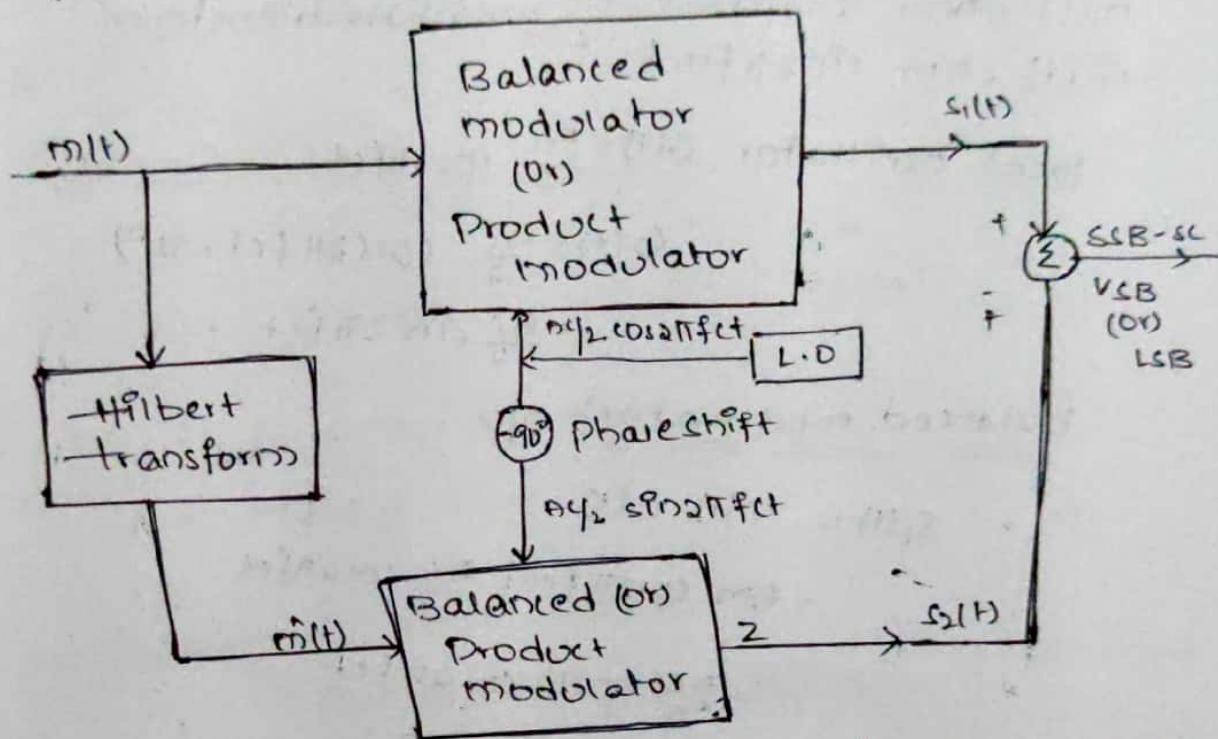
$$\begin{aligned}
 v_o(f) &= \frac{A(c A c')}{8} [m(f - \Delta f) + m(f + \Delta f)] \\
 &\quad - \frac{A(c A c')}{8} [m(f - \Delta f) - m(f + \Delta f)] \\
 &\quad - \frac{A(c A c')}{8} m(f - \Delta f) + \frac{A(c A c')}{8} m(f + \Delta f) - \frac{A(c A c')}{8} m(f - \Delta f) \\
 &\quad + \frac{A(c A c')}{8} m(f + \Delta f)
 \end{aligned}$$

$$v_o(f) = \frac{A(c A c')}{u} m(f + \Delta f) \rightarrow \text{demodulated O/P}$$

3Q  
A  
Generate SSB-SC waves using 2nd and 3rd method.  
Generating SSB-SC wave by using 2nd and 3rd method.

→ second method:

second method is also known as phase discrimination  
(or) Hartley modulator.



Its implementation follows from time domain description of SSB waves.

→ Pt has got 2 paths  
 ↗ Inphase path  
 ↗ Quadrature path.

Each path has got product modulator they receive inphase carrier cosinifct and out of phase carrier by  $90^\circ$  i.e. sinifct respectively.

→ wide band phase shifter is designed to produce  $m_1(t)$  i.e H.T of  $m_1(t)$ .

→ the quadrature path integers with inphase path and eliminates the power in one of the SSB bands, depend on whether upper SSB (or) lower SSB is required.

→ In this method wideband phase shifter requires special attention whereas in frequency discrimination method only BPF is required.

### mathematical analysis:-

$$m(t) = A_m \cos 2\pi f_m t \quad \xrightarrow{\text{Hilbert transform}}$$

$$\hat{m}(t) = A_m \sin 2\pi f_m t$$

$$\text{local oscillator } c_1(t) = \frac{A_c}{2} \cos 2\pi f_c t$$

$$c_2(t) = \frac{A_c}{2} \cos(2\pi f_c t - 90^\circ)$$

$$= \frac{A_c}{2} \sin 2\pi f_c t$$

### Balanced modulator: O/P.

$$s_1(t) = m(t) c_1(t)$$

$$= A_m \cos 2\pi f_m t \cdot \frac{A_c}{2} \cos 2\pi f_c t$$

$$= \frac{A_c}{2} m(t) \cos 2\pi f_c t$$

$$s_2(t) = \hat{m}(t) c_2(t)$$

$$= \frac{A_c}{2} \hat{m}(t) \sin 2\pi f_c t$$

$$s(t)_{SSB-SC} = s_1(t) - s_2(t) \quad \text{for U.S.B}$$

$$= \frac{A_c}{2} m(t) \cos 2\pi f_c t - \frac{A_c}{2} \hat{m}(t) \sin 2\pi f_c t$$

$$s(t)_{SSB-SC} = s_1(t) + s_2(t) \quad \text{for L.S.B}$$

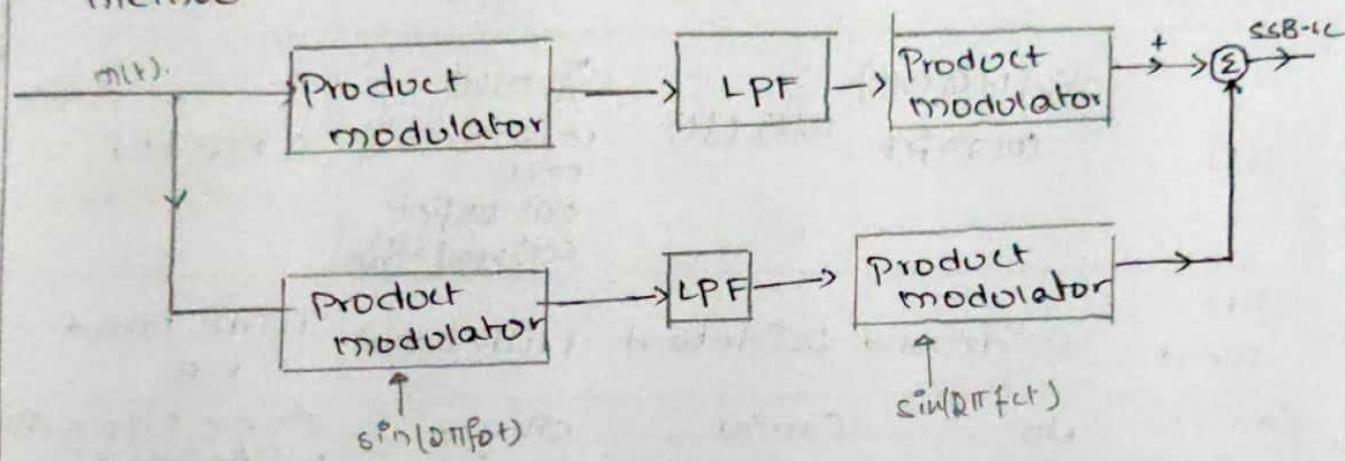
$$= \frac{A_c}{2} m(t) \cos 2\pi f_c t + \frac{A_c}{2} \hat{m}(t) \sin 2\pi f_c t$$

Advantages:

- 1) There is no need of any filters to select a band of frequencies.
- 2) It is applicable for all frequencies.

II

Third method is also known as [1 & 2 method] or Weaver's method



$\rightarrow m(t) \Rightarrow$  frequency  $f_a \leq |f_i| \leq f_b$ .

$$\rightarrow f_o = \frac{(f_a + f_b)}{2}$$

$\rightarrow$  BPF  $\begin{cases} \text{im phase channel} \\ \text{quadrature phase channel} \end{cases} \rightarrow$  identical

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Write a table comparing the following parameters for AM, DSBSC, SSBSC, & VSB

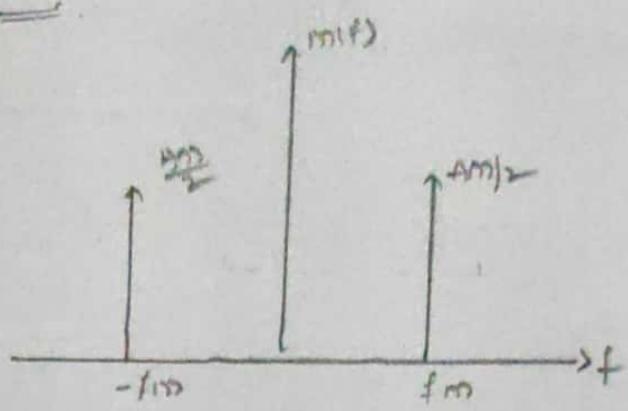
- i) S(t)
- ii) sidebands
- iii) carrier suppression in bandwidth
- iv) Power
- v) complexity
- vi) modulation type
- vii) efficiency
- viii) application.

Parameter	AM	DSB-SC	SSBSC	VSB
i) S(t)	$v_c [1 + f_m(t)]$ constant.	$m(t) \cos \omega t$	$\frac{v_c}{2} m(t)$ $(m^2 - \frac{v_c^2}{2})$ sin affect $S(t)_{VSB} = \frac{S(t)}{\sqrt{2}}$	$S(t)_{VSB}$
ii) side band	2 sideband	2 sideband	1 sideband	1 side band VSB
iii) carrier suppression	No suppression	Carrier suppression	single suppression	single suppression 2 sideband Partially
iv) band width	$2f_m$	$2f_m$	$f_m$	$f_m + f_r$
v) power	high	medium	low	low but higher than SSBSC
vi) complexity	simple	complex	complex	simple
vii) Application	Radio communication	Point to Point communication	for voice transmission	TV or video broadcasting
viii) modulation type	non-linear	linear	linear	linear
ix) efficiency	minimum	moderate	maximum	moderate

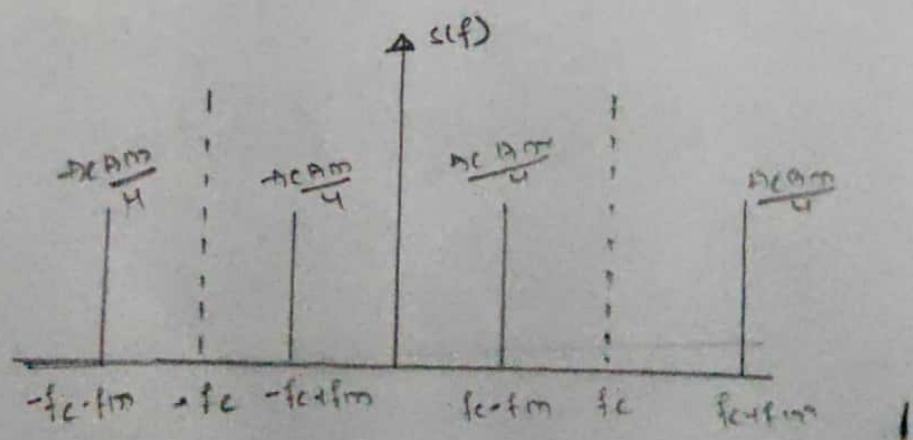
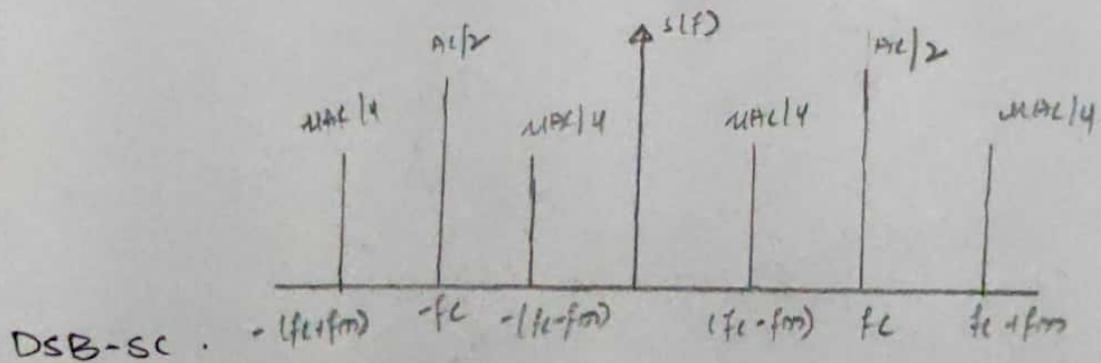
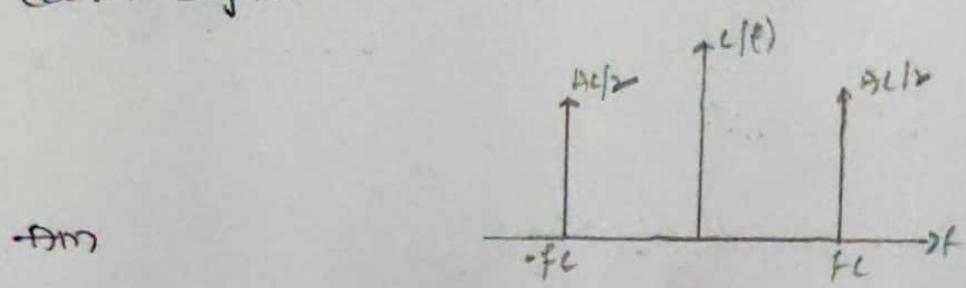
5Q Draw frequency spectrum from DSB-SC in neat diagram.

### Frequency spectrum :-

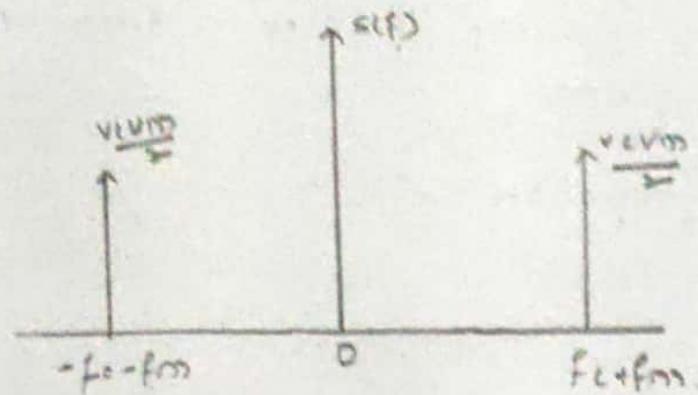
Message signal



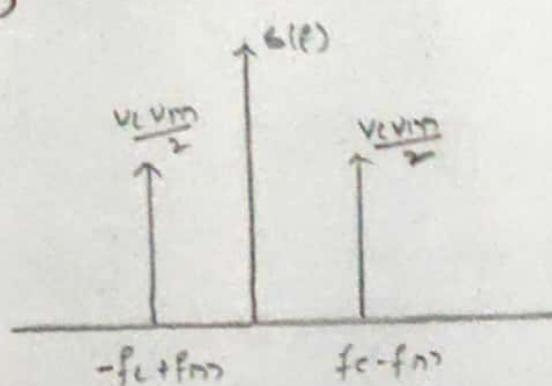
carrier signal



SSB-SC (VSB)



SSB-SC (LSB)



VSB

