

Q1

Demodulation of DSBSC using synchronous or coherent. and find the expressions for frequency error and phase error.

A

DSBSC - Double side band suppressed carrier

→ Demodulation of DSBSC can be done in 2 types.

① synchronous (or) coherent detector.

② Costas loop.

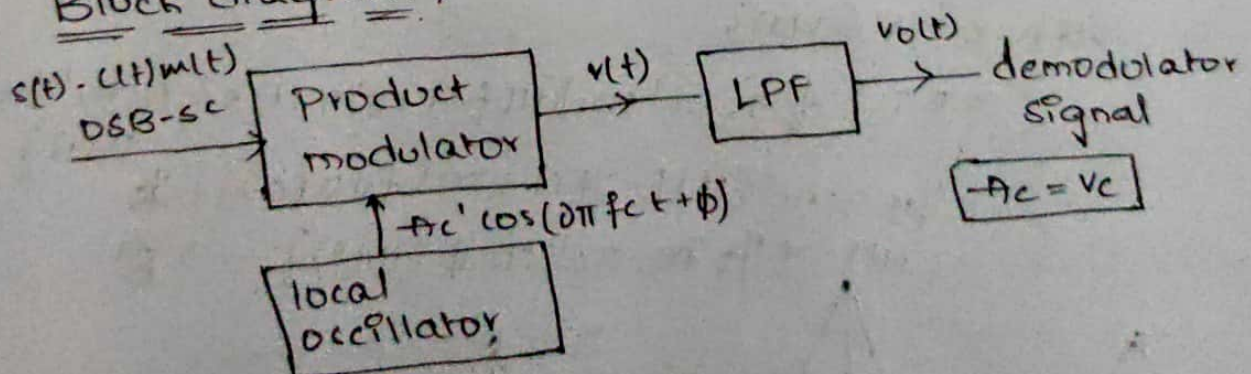
→ Synchronous or coherent detector:-

We know that, envelope of DSBSC modulated wave form is different than the msg. sig so we must employ coherent detection at a synchronous detection

→ in this process to multiply the DSBSC modulated w/f with a locally generated sinusoidal waveform & then LPF. then original msg can be obtained.

→ it is assumed that local oscillator used as the detector (demodulation) is of same frequency and phase (ie coherent w.r.t oscillator etc) used in Tx and is synchronous to it

Block diagram:-



w.k.t $s(t) = A_c \cos(2\pi f_c t) m(t)$

Product modulator $\Rightarrow v(t) = s(t) * L_o(t)$
DSB-SC

$$\begin{aligned}
 \rightarrow v(t) &= s(t) A_c' \cos[2\pi f_c t + \phi] m(t) \\
 &= A_c A_c' \cos 2\pi f_c t + \cos[2\pi f_c t + \phi] m(t) \\
 &= \frac{A_c A_c'}{2} [2 \cos 2\pi f_c t \cos[2\pi f_c t + \phi]] m(t) \\
 &= \frac{A_c A_c'}{2} [\cos(4\pi f_c t + \phi) + \cos \phi] m(t) \\
 v(t) &= \frac{m(t)}{2} A_c A_c' \cos(4\pi f_c t + \phi) + \boxed{\frac{1}{2} A_c A_c' \cos \phi m(t)} \\
 &\quad \downarrow \quad \quad \quad \downarrow \\
 &\quad \text{high frequency} \quad \quad \text{low frequency}
 \end{aligned}$$

\rightarrow this $v(t)$ from product modulator is sent to a low pass filter which allow only low frequency signal to pass through it.

\rightarrow o/p of bpf

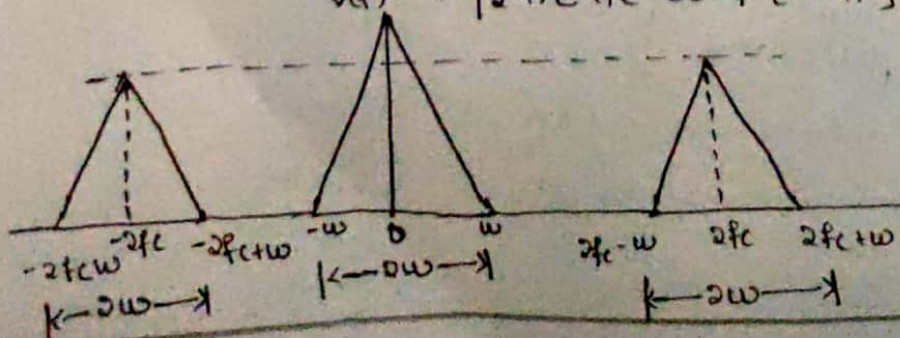
$$v_o(t) = s(t) \text{ demodulator} = \frac{A_c A_c'}{2} m(t) \cos \phi \quad \rightarrow \textcircled{2}$$

\rightarrow It is not compulsory that the oscillator produce the exact synchronous output carrier wave (or) signal each time. Hence it may produce 2 types of errors they are:-

- ① phase error
- ② frequency error

from eq ①: $v(f)$ can be obtained as

$$\begin{aligned}
 v(f) &= \text{F.T} \{v(t)\} \\
 &= \text{F.T} \left\{ \frac{1}{2} A_c A_c' \cos(4\pi f_c t + \phi) m(t) + \frac{1}{2} A_c A_c' \cos \phi m(t) \right\} \\
 &= \frac{1}{4} A_c A_c' [M(f - 2f_c) + M(f + 2f_c)] + \frac{1}{2} A_c A_c' \cos \phi [M(f)] \rightarrow \textcircled{2}
 \end{aligned}$$



→ Amplitude of demodulated signal is maximum difference iff $\phi = 0$ minimum iff $\phi = \pm \pi/2$

Note: when $\phi = \pm \pi/2$ demodulated signal this is called Quadrature Null effect incoherent detection.

Drawback due to QNE:

→ the phase error ϕ causes demodulator output to be attenuated by a factor of ϕ

→ when $\phi = \text{constant}$, there is no distortion in demodulated o/p else if $\phi = \text{randomly varying} \Rightarrow \cos \phi$ also varies randomly not desired

→ so, a new ckt has to be provided to make sure that b.o in Rx works in perfect synchronisation w.r.t carrier $c(t)$ in Tx w.r.t frequency & phase thus it increases cost at DSBSC demodulator

$$s(t)_{\text{DSBSC}} = m(t)c(t) = A_c \cos(2\pi f_c t) m(t).$$

Phase error:

$$s_1(t) = s(t)_{\text{DSBSC}} * c(t)$$

$$= A_c \cos(2\pi f_c t) m(t) * \cos(2\pi f_c t + \phi)$$

$$= \frac{A_c^2}{2} m(t) [\cos(2\pi f_c t) \cos(2\pi f_c t + \phi)]$$

$$= \frac{A_c^2}{2} m(t) [\cos(4\pi f_c t + \phi) + \cos \phi]$$

$$= \frac{A_c^2}{2} m(t) \cos \phi + \frac{A_c^2}{2} m(t) \cos(4\pi f_c t + \phi)$$

Output after LPF

$$s_1(t)_{\text{demod}} = \frac{A_c^2}{2} m(t) \cos \phi$$

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Frequency error:-

$$s_1(t) = s(t) \cos 2\pi f_c t * c(t)$$

$$= A_c \cos 2\pi f_c t m(t) * A_c \cos (2\pi f_c t + \Delta f)$$

$$= \frac{A_c^2}{2} m(t) [2 \cos 2\pi f_c t \cos (2\pi f_c t + \Delta f)]$$

$$= \frac{A_c^2}{2} m(t) [\cos (4\pi f_c t + \Delta f) + \cos \Delta f]$$

$$= \frac{A_c^2}{2} m(t) \cos \Delta f + \frac{A_c^2}{2} m(t) \cos (4\pi f_c t + \Delta f)$$

output after bpf

$$s(t)_{\text{demodulated}} = \frac{A_c^2}{2} m(t) \cos \Delta f$$

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Amplitude of demodulated signal is max iff $\phi = 0$ and min iff $\phi = \pm \pi/2$.

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2Q Demodulation of SSBsc using synchronous or coherent detector and also find the expression for frequency error and phase error.

A SSBsc - (Single side band - suppressed carrier)

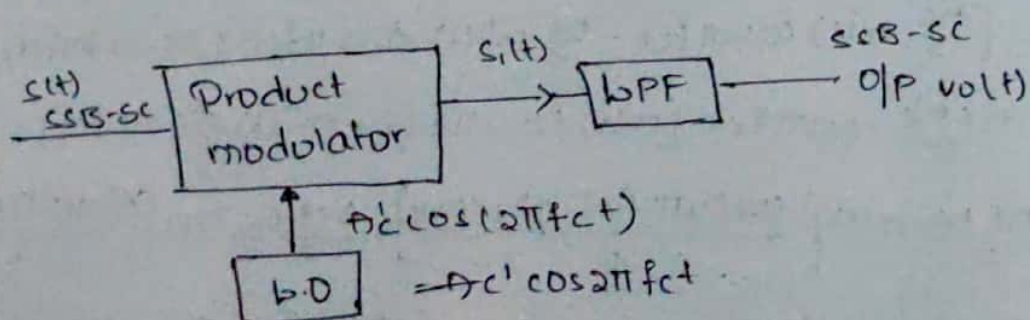
Coherent (or) synchronous detector of - SSB-sc:-

→ Demodulation of SSB is complicated since here carrier as well as one of the sidebands is suppressed when compared to DSB-sc.

→ coherent detection is used where synchronization is needed in both frequency & phase hardware locally generated carrier in Rx w.r.t carrier used in Tx.

→ Although carrier is suppressed, yet info is embedded on carrier phase and frequency is present in side bands of modulated wave.

→ The 2 side bands are mirror images of each other



w.k.T
$$s(t)_{SSB-sc} = \frac{Ac}{2} [m(t) \cos(2\pi f_c t) - m(t) \sin(2\pi f_c t)]$$

$$c(t) = Ac' \cos(2\pi f_c t)$$

$$= Ac' \cos 2\pi f_c t$$

O/P of product modulator $s_1(t) = s(t)_{SSB-sc} * c(t)$

$$\begin{aligned}
 S_1(t) &= \left[\frac{Ac}{2} m(t) (\cos 2\pi f_c t - \frac{A_c}{2} m'(t) \sin 2\pi f_c t) \right] A_c' \cos 2\pi f_c t \\
 &= \frac{Ac A_c'}{2} (\cos^2 2\pi f_c t m(t) - \frac{A_c}{2} m'(t) \sin 2\pi f_c t \cos 2\pi f_c t) \\
 &= \frac{Ac A_c'}{4} m(t) + \frac{Ac A_c'}{4} \cos 4\pi f_c t m(t) - \frac{Ac A_c'}{2} m'(t) \sin 2\pi f_c t \cos 2\pi f_c t
 \end{aligned}$$

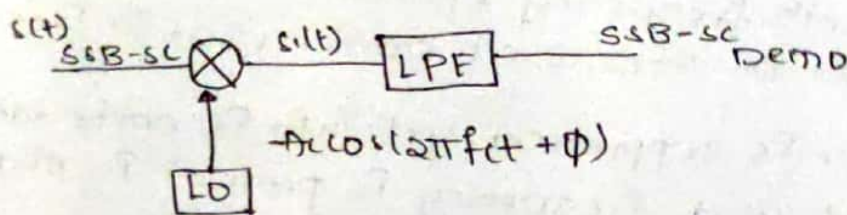
the o/p is sent to low pass filter which allows only low frequency & attenuates high frequency

O/p of LPF $s(t)_{SSB-SC} = \frac{Ac A_c'}{4} m(t)$.

Phase error: $-Ac \cos(2\pi f_c t + \phi)$

frequency error: $-Ac \cos(2\pi f_c t + \Delta f)$

a Phase error:-



$$s(t)_{SSB-SC} = \frac{Ac}{2} m(t) \cos 2\pi f_c t - \frac{A_c}{2} m'(t) \sin 2\pi f_c t$$

$$c(t) = A_c \cos(2\pi f_c t + \phi)$$

$$s_1(t) = \left[\frac{Ac}{2} m(t) \cos 2\pi f_c t - \frac{A_c}{2} m'(t) \sin 2\pi f_c t \right] A_c' \cos 2\pi f_c t$$

$$= \frac{Ac A_c'}{2} \cos 2\pi f_c t [m(t) \cos 2\pi f_c t - m'(t) \sin 2\pi f_c t]$$

$$= \frac{Ac A_c'}{2} m(t) \left[\frac{\cos(4\pi f_c t + \phi) + \cos \phi}{2} \right] - \frac{Ac A_c'}{2} m'(t) \left[\frac{\sin(4\pi f_c t + \phi) + \sin \phi}{2} \right]$$

$$s_1(t) = \underbrace{\frac{Ac A_c'}{4} m(t)}_{\text{desired}} + \underbrace{\frac{Ac A_c'}{4} m(t) \cos 4\pi f_c t - \frac{Ac A_c'}{4} m'(t) \sin 4\pi f_c t}_{\text{undesired}}$$

O/p of LPF

$$s(t) = \frac{Ac A_c'}{4} (m(t) \cos \phi + m'(t) \sin \phi)$$

→ Applying Fourier T/F

$$\begin{aligned}
 s(f) &= \frac{A_c A_c'}{4} m(f) \cos \phi + \frac{A_c A_c'}{4} m^*(f) \sin \phi \\
 s(f) &= \frac{A_c A_c'}{4} m(f) \cos \phi + \frac{A_c A_c'}{4} m(f) (\downarrow) \sin \phi \\
 &= \frac{A_c A_c'}{4} m(f) \cos \phi - j \frac{A_c A_c'}{4} m(f) \sin \phi \\
 \boxed{s(f) = \frac{A_c A_c'}{4} m(f) e^{-j\phi}} &\Rightarrow \underline{v_o(t)}
 \end{aligned}$$

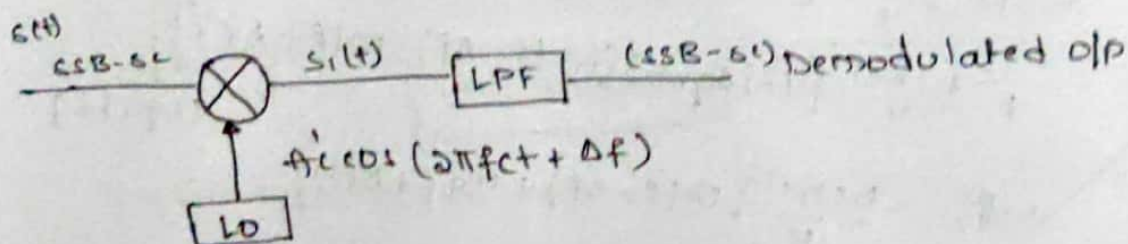
there is no Quadrature Null effect in coherent detection of SSB-SC

Effects of phase and frequency error in SSB-Demodulation

→ for effective coherent detection Rx should generate coherent frequency and phase of carrier as that of Tx. this can be done by.

- b Using stable local oscillator at receiver
- b providing pilot carrier along with SSB during Tx.

b frequency error:



→ It produces phase shift of $+0 \text{ (or)} +\pi$ for the negative frequencies & $-0 \text{ (or)} -\pi$ for the positive frequencies.

→ let Δf be the frequency error in locally generated carrier $A_c' \cos(2\pi(2f_c + \Delta f)t)$ is used

$$\begin{aligned}
 s(t)_{\text{SSBSC}} &= \frac{A_c}{2} m(t) \cos 2\pi f_c t - \frac{A_c}{2} m^*(t) \sin 2\pi f_c t \\
 c(t) &= A_c' \cos 2\pi(f_c + \Delta f)t
 \end{aligned}$$

O/P of product modulator

$$s_1(t) = s(t) * (t)$$

$$s_1(t) = \left[\frac{A_c}{2} m(t) \cos 2\pi f_c t - \frac{A_c}{2} \hat{m}(t) \sin 2\pi f_c t \right] A_c' \cos(2\pi f_c t + \Delta f)$$

$$= \frac{A_c A_c'}{2} m(t) [\cos 2\pi f_c t + \cos 2\pi (f_c + \Delta f) t - \frac{A_c A_c'}{2} \hat{m}(t) \sin 2\pi f_c t \cos 2\pi (f_c + \Delta f) t]$$

$$s_1(t)_{SIS-SC} = \frac{A_c A_c'}{4} m(t) [\cos(2\pi f_c t + 2\pi \Delta f) t + \cos 2\pi \Delta f t]$$

$$= \frac{A_c A_c'}{4} m(t) [\sin(2\pi f_c t + 2\pi \Delta f) t - \sin 2\pi \Delta f t]$$

$$= \frac{A_c A_c'}{4} m(t) \underbrace{\cos(2\pi f_c t + 2\pi \Delta f) t}_{\text{Unwanted}} + \frac{A_c A_c'}{4} m(t) \underbrace{\cos 2\pi \Delta f t}_{\text{Desired}}$$

$$- \frac{A_c A_c'}{4} \hat{m}(t) \underbrace{\sin[2\pi f_c t + 2\pi \Delta f t]}_{\text{Unwanted}} + \frac{A_c A_c'}{4} \underbrace{\sin 2\pi \Delta f t}_{\text{Desired}} m(t)$$

O/P of low pass filter.

$$v_o(t) = \frac{A_c A_c'}{4} m(t) \cos 2\pi \Delta f t + \frac{A_c A_c'}{4} \sin 2\pi \Delta f \hat{m}(t)$$

$$= \frac{A_c A_c'}{4} [m(t) \cos 2\pi \Delta f t + \hat{m}(t) \sin 2\pi \Delta f t]$$

Apply F.T

$$v_o(f) = \frac{A_c A_c'}{4} \left[\frac{m(f - \Delta f) + m(f + \Delta f)}{2} \right]$$

$$+ \frac{A_c A_c'}{4} [(1 - j \operatorname{sgn} f) [m(f - \Delta f) - m(f + \Delta f)]]$$

$j \operatorname{sgn} f = 1$

$$v_o(f) = \frac{A_c A_c'}{8} [m(f - \Delta f) + m(f + \Delta f)]$$

$$- \frac{A_c A_c'}{8} [m(f - \Delta f) - m(f + \Delta f)]$$

$$= \frac{A_c A_c'}{8} m(f - \Delta f) + \frac{A_c A_c'}{8} m(f + \Delta f) - \frac{A_c A_c'}{8} m(f - \Delta f)$$

$$+ \frac{A_c A_c'}{8} m(f + \Delta f)$$

$$\boxed{v_o(f) = \frac{A_c A_c'}{4} m(f + \Delta f)} \rightarrow \text{demodulated o/p}$$

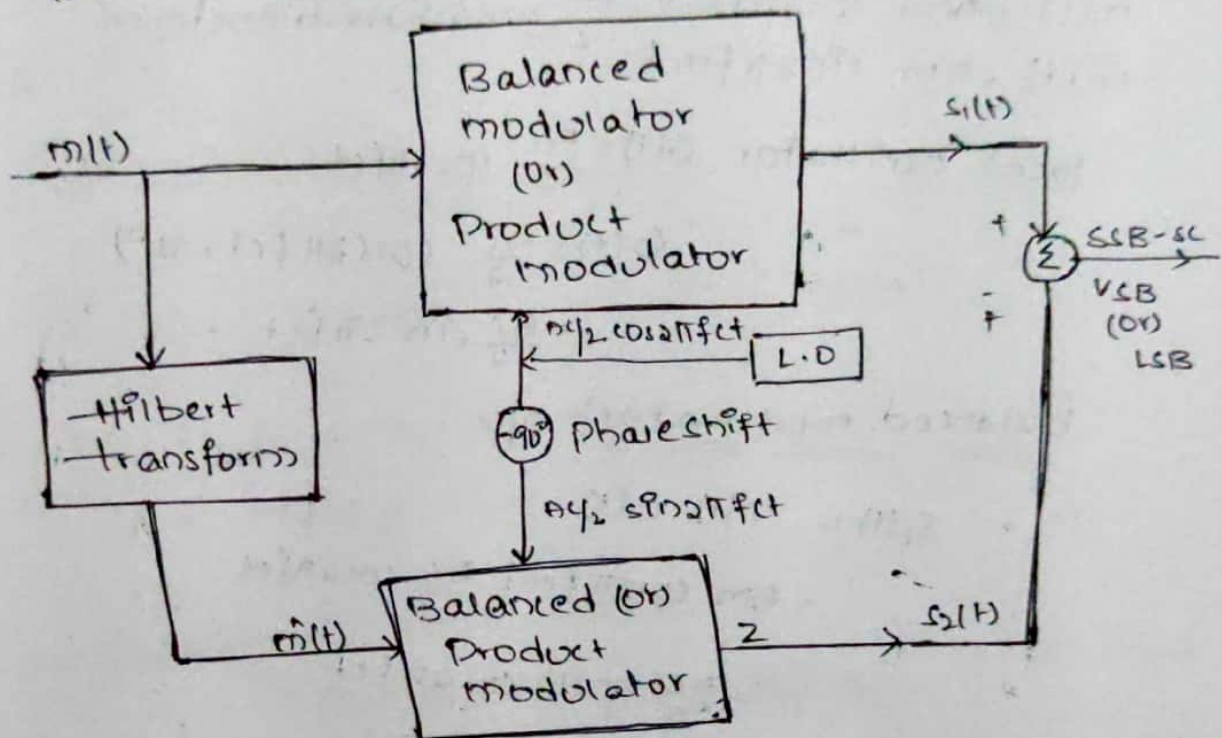
3Q

A

Generate SSB-SC waves using 2nd and 3rd method.
Generating SSB-SC wave by using 2nd and 3rd method

→ second method:

second method is also known as phase discrimination
(or) Hartley modulator.



Its implementation follows from time domain description of SSB waves.

→ It has got 2 paths → Inphase path
→ Quadrature path.

Each path has got product modulator they receive inphase carrier $\cos \omega_c t$ and out of phase carrier by 90° i.e. $\sin \omega_c t$ respectively.

→ wide band phase shifter is designed to produce $\hat{m}(t)$ i.e. H.T of $m(t)$.

→ the quadrature path integrates with inphase path and eliminates the power in one of the 2 side bands, depend on whether upper ssb (or) lower ssb is request

→ In this method wideband phase shifter requires special attention whereas in frequency discrimination method only BPF is required.

mathematical analysis:-

$$m(t) = A_m \cos 2\pi f_m t \quad \rightarrow \text{Hilbert transform.}$$

$$\hat{m}(t) = A_m \sin 2\pi f_m t$$

$$\text{local oscillator } c_1(t) = \frac{A_c}{2} \cos 2\pi f_c t$$

$$c_2(t) = \frac{A_c}{2} \cos(2\pi f_c t - 90^\circ)$$

$$= -\frac{A_c}{2} \sin 2\pi f_c t$$

Balanced modulator:- o/p.

$$s_1(t) = m(t) c_1(t)$$

$$= A_m \cos 2\pi f_m t \cdot \frac{A_c}{2} \cos 2\pi f_c t$$

$$= \frac{A_c}{2} m(t) \cos 2\pi f_c t$$

$$s_2(t) = \hat{m}(t) c_2(t)$$

$$= \frac{A_c}{2} \hat{m}(t) \sin 2\pi f_c t$$

$$s(t)_{\text{SSB-SC}} = s_1(t) - s_2(t) \quad \text{for USB}$$

$$= \frac{A_c}{2} m(t) \cos 2\pi f_c t - \frac{A_c}{2} \hat{m}(t) \sin 2\pi f_c t$$

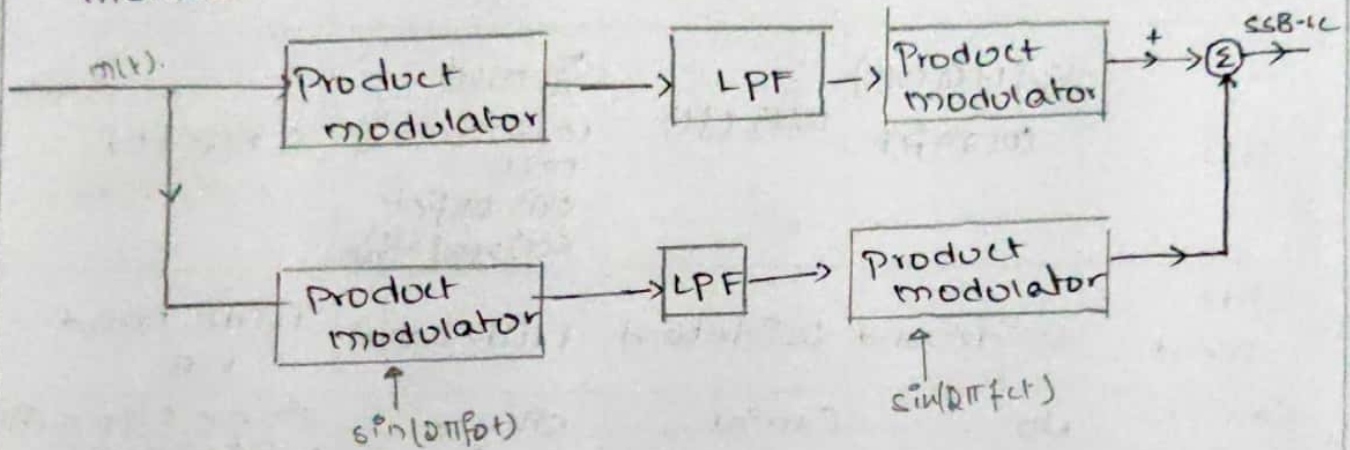
$$s(t)_{\text{SSB-SC}} = s_1(t) + s_2(t) \quad \text{for LSB}$$

$$= \frac{A_c}{2} m(t) \cos 2\pi f_c t + \frac{A_c}{2} \hat{m}(t) \sin 2\pi f_c t$$

Advantages:-

- 1) There is no need of any filters to select a band of frequencies
- 2) It is applicable for all frequencies.

Third method is also known as [1 & 2 method] or weaver's method



→ $m(t) \Rightarrow$ frequency $f_a \leq |F| \leq f_b$.

→ $f_0 = \frac{(f_a + f_b)}{2}$

→ LPF $\left\{ \begin{array}{l} \text{in phase channel} \\ \text{quadrature phase channel} \end{array} \right\}$ identical

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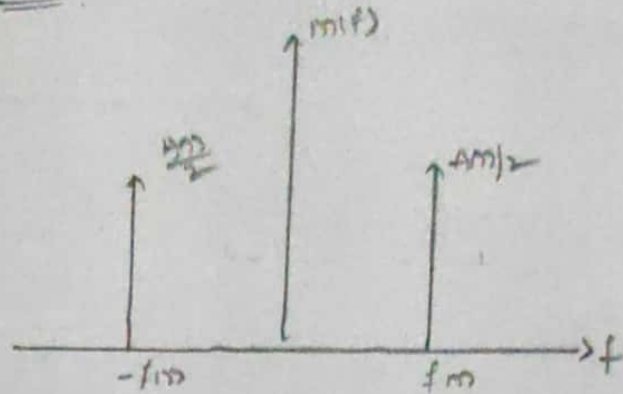
4 write a table comparing the following parameters for AM, DSBSC, SSBSC, & VSB
i) $s(t)$ ii) sidebands iii) carrier suppression iv) bandwidth
v) Power vi) complexity vii) modulation type viii) efficiency
ix) application.

Parameter	AM	DSB-SC	SSBSC	VSB
i) $s(t)$	$V_c [1 + k_a m(t)] \cos 2\pi f_c t$	$m(t) \cos 2\pi f_c t$	$\frac{V_c}{2} m(t) \cos 2\pi f_c t - \frac{V_c}{2} m(t) \sin 2\pi f_c t$ $s(t) = VSB s(t) _{VSB}$	$s(t) = VSB s(t) _{VSB}$
ii) side band	2 sideband	2 sideband	1 sideband	1 side band VSB
iii) carrier suppression	No suppression	Carrier suppression	single suppression	single suppression 2 side band Partially
iv) band width	$2f_m$	$2f_m$	f_m	$f_m + f_v$
v) power	high	medium	low	low but higher than SSBSC
vi) complexity	simple	complex	complex	simple
vii) Application	Radio communication	point to point communication	for voice transmission	TV (or) video broadcasting
viii) modulation type	non-linear	linear	linear	linear
ix) efficiency	minimum	moderate	maximum	moderate

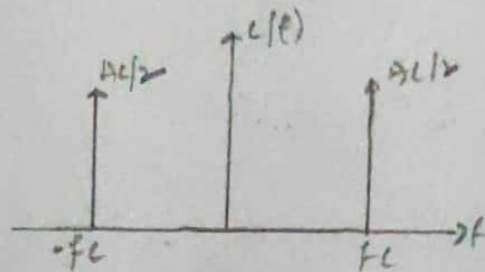
5Q Draw frequency spectrum from Am to VSB in neat diagram.

Frequency spectrum:-

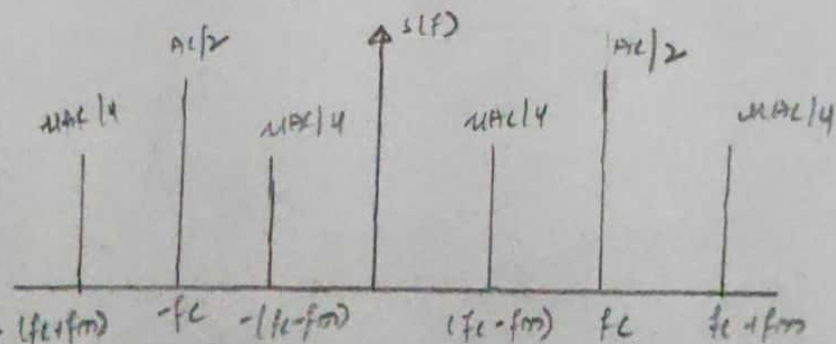
Message signal



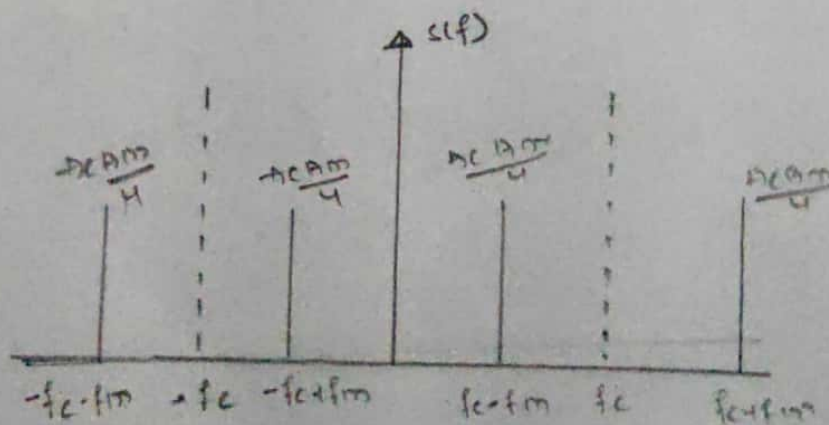
carrier signal



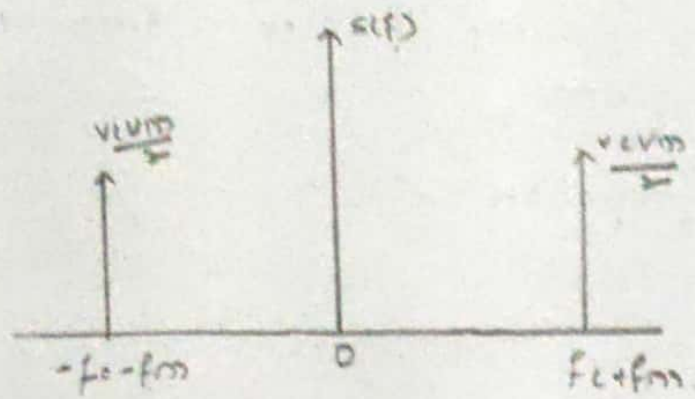
Am



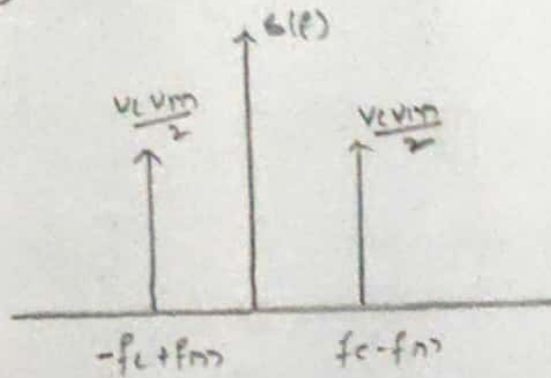
DSB-SC



SSB-SC (VSB)



SSB-SC (LSB)



VSB

