

# 12.8.1.2

EE24BTECH11033 - KOLLURU SURAJ

**Question:** Find the area of the region bounded by  $y^2 = 9x$ ,  $x = 2$ ,  $x = 4$  and the x-axis in the first quadrant.

**Solution:**

**Some theory about Trapezoidal rule:**

The idea behind the trapezoidal rule is to approximate the region under the curve of the function as a series of trapezoids, rather than using rectangles. The area of each trapezoid is then computed and summed to estimate the total area under the curve (the integral). First we need to set up the integral

Area under curve is given by

$$A = \int_2^4 3\sqrt{x} dx \quad (0.1)$$

We will approximate this using trapezoidal rule. Divide the interval [2,4] into 100 subintervals with each of width  $h = \frac{4-2}{100} = \frac{1}{50}$ , Let:

$$x_0 = 2, x_1 = x_0 + h, x_2 = x_1 + h, \dots, x_n = 4 \quad (0.2)$$

The trapezoidal rule for approximating the integral becomes:

$$A \approx \frac{h}{2} [f(x_0) + 2 \sum_{i=1}^{n-1} f(x_i) + f(x_n)] \quad (0.3)$$

where  $f(x) = \sqrt{3}x$ . Substituting it in 0.1 gives

$$A \approx \frac{3h}{2} [\sqrt{x_0} + 2 \sum_{i=1}^{n-1} \sqrt{x_i} + \sqrt{x_n}] \quad (0.4)$$

This is a difference equation because it expresses the total area A as a sum of terms at discrete points  $x_i$ , with a recurrence-like structure for the summation.

Using a C code to find the area using trapezoidal rule, The area is

$$A \approx 10.343135 \quad (0.5)$$

If the area is calculated directly using integration it would be 10.343146 which is so close to the one we found using trapezoidal rule

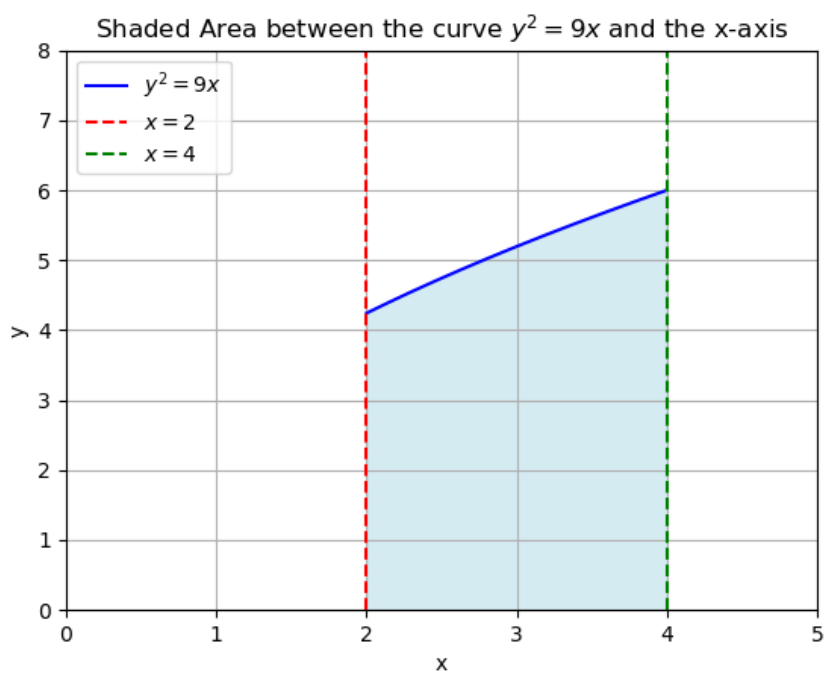


Fig. 0.1