

PRACTICAL 4 (b)

Aim: To solve the
system of equations
using Gauss Jordan
method.

ASSIGNMENT

1 Q1. Solve the following system of equations

$$2x_1 + x_2 - x_3 = 1$$

$$5x_1 + 2x_2 + 2x_3 = -4$$

$$3x_1 + x_2 + x_3 = 5$$

using the Gauss-Jordan method.

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→ kill(all)$
keepfloat:true$

A:matrix(                                /*...Coefficient Matrix...*/
    [2.0, 1.0, -1.0],
    [5.0, 2.0, 2.0],
    [3.0, 1.0, 1.0])$

B:matrix(                                /*...Constants Matrix...*/
    [1.0], [-4.0], [5.0])$

X:matrix(                                /*...Variables Matrix...*/
    [x], [y], [z])$

print("Now, the augmented matrix will be,")$
Aug:addcol(A,B);                        /*...Creating Augmented Matrix...*/
print(" ");

print("Now, the Echelon Form is,")$
S : echelon(Aug);                       /*..Calculates Echolen Form of Matrix..*/
print(" ");

print("R2 -> R2 - ",float(S[2][3])," * R3")$
S[2] : S[2] - S[2][3].S[3]$
S;
print(" ");

print("R1 -> R1 - ",float(S[1][3])," * R3")$
S[1] : S[1] - S[1][3].S[3]$
S;
print(" ");

print("R1 -> R1 - ",float(S[1][2])," * R2")$
S[1] : S[1] - S[1][2].S[2]$
S;
print(" ");

print("The Solution Matrix is: ")$
X=col(S,4);
Now, the augmented matrix will be,
(%o6) 
$$\begin{pmatrix} 2.0 & 1.0 & -1.0 & 1.0 \\ 5.0 & 2.0 & 2.0 & -4.0 \\ 3.0 & 1.0 & 1.0 & 5.0 \end{pmatrix}$$


(%o7)
Now, the Echelon Form is,
(%o9) 
$$\begin{pmatrix} 1 & 0.5 & -0.5 & 0.5 \\ 0 & 1 & -9.0 & 13.0 \\ 0 & 0 & 1 & -5.0 \end{pmatrix}$$


(%o10)
R2 → R2 - -9.0 * R3

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2 Q2.Solve the following system of equations

$$x + y - z = -3$$

$$6x + 2y + 2z = 2$$

$$-3x + 4y + z = 1$$

using the Gauss-Jordan method.

```

→ kill(all)$
keepfloat:true$

A:matrix(                                /*...Coefficient Matrix...*/
    [1.0, 1.0, -1.0],
    [6.0, 2.0, 2.0],
    [-3.0, 4.0, 1.0])$

B:matrix(                                /*...Constants Matrix...*/
    [-3.0], [2.0], [1.0])$

X:matrix(                                /*...Variables Matrix...*/
    [x], [y], [z])$

print("Now, the augmented matrix will be,")$
Aug:addcol(A,B);                        /*...Creating Augmented Matrix...*/
print(" ");

print("Now, the Echelon Form is,")$
S : echelon(Aug);                       /*..Calculates Echolen Form of Matrix..*/
print(" ");

print("R2 -> R2 - ",float(S[2][3])," * R3")$
S[2] : S[2] - S[2][3].S[3]$
S;
print(" ");

print("R1 -> R1 - ",float(S[1][3])," * R3")$
S[1] : S[1] - S[1][3].S[3]$
S;
print(" ");

print("R1 -> R1 - ",float(S[1][2])," * R2")$
S[1] : S[1] - S[1][2].S[2]$
S;
print(" ");

print("The Solution Matrix is: ")$
X=col(S,4);
Now, the augmented matrix will be,
(%o6) 
$$\begin{pmatrix} 1.0 & 1.0 & -1.0 & -3.0 \\ 6.0 & 2.0 & 2.0 & 2.0 \\ -3.0 & 4.0 & 1.0 & 1.0 \end{pmatrix}$$


(%o7)
Now, the Echelon Form is,
(%o9) 
$$\begin{pmatrix} 1 & 1.0 & -1.0 & -3.0 \\ 0 & 1 & -2.0 & -5.0 \\ 0 & 0 & 1 & 2.25 \end{pmatrix}$$


(%o10)
R2 → R2 - -2.0 * R3

```

3 Q3.Using the Gauss-Jordan method, find the inverse of the following matrix.

$$([1 \ 2 \ 3]$$

$$[0 \ 1 \ 5]$$

$$[5 \ 6 \ 0])$$

```

→ kill(all)$
keepfloat:true$
A:matrix(                                     /*...Given Matrix...*/
    [1.0, 2.0, 3.0],
    [0.0, 1.0, 5.0],
    [5.0, 6.0, 0.0])$
B:matrix(                                     /*...Identity Matrix...*/
    [1.0,0.0,0.0],
    [0.0,1.0,0.0],
    [0.0,0.0,1.0])$

print("Now, the augmented matrix will be,")$
Aug:addcol(A,B);                             /*...Creating Augmented Matrix...*/
print("")$

print("The Echelon Form is :")$
S : echelon(Aug);                             /*..Calculates Echolen Form of Matrix..*/
print(" ")$

/*..Operations so as to form reduced row echelon form..*/
print("R2 -> R2 - ",float(S[2][3])," * R3")$
S[2] : S[2] - S[2][3].S[3]$
S;
print(" ")$

print("R1 -> R1 - ",float(S[1][3])," * R3")$
S[1] : S[1] - S[1][3].S[3]$
S;
print(" ")$

print("R1 -> R1 - ",float(S[1][2])," * R2")$
S[1] : S[1] - S[1][2].S[2]$
S;
print(" ")$

print("The Inverse of the Given Matrix is: ")$
Inv: submatrix(S,1,2,3);
Now, the augmented matrix will be,
(%o5) 
$$\begin{pmatrix} 1.0 & 2.0 & 3.0 & 1.0 & 0.0 & 0.0 \\ 0.0 & 1.0 & 5.0 & 0.0 & 1.0 & 0.0 \\ 5.0 & 6.0 & 0.0 & 0.0 & 0.0 & 1.0 \end{pmatrix}$$


The Echelon Form is :
(%o8) 
$$\begin{pmatrix} 1 & 1.2 & 0 & 0 & 0 & 0.2 \\ 0 & 1 & 5.0 & 0 & 1.0 & 0 \\ 0 & 0 & 1 & -1.0 & 0.8 & 0.2 \end{pmatrix}$$


R2 → R2 - 5.0 * R3
(%o12) 
$$\begin{pmatrix} 1 & 1.2 & 0 & 0 & 0 & 0.2 \\ 0 & 1 & 0.0 & 5.0 & -3.0 & -1.0 \\ 0 & 0 & 1 & -1.0 & 0.8 & 0.2 \end{pmatrix}$$


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**4 Q4.Solve the following given
system of equations**

$$-3y + 7z = 2$$

$$x + 2y - z = 3$$

$$5x - 2y = 2$$

using the Gauss-Jordan method

```

→ kill(all)$
keepfloat:true$

A:matrix(                                /*...Coefficient Matrix...*/
    [0.0, -3.0, 7.0],
    [1.0, 2.0, -1.0],
    [5.0, -2.0, 0.0])$

B:matrix(                                /*...Constants Matrix...*/
    [2.0], [3.0], [2.0])$

X:matrix(                                /*...Variables Matrix...*/
    [x], [y], [z])$

print("Now, the augmented matrix will be,")$
Aug:addcol(A,B);                        /*...Creating Augmented Matrix...*/
print(" ");

print("Now, the Echelon Form is,")$
S : echelon(Aug);                        /*..Calculates Echolen Form of Matrix..*/
print(" ");

print("R2 -> R2 - ",float(S[2][3])," * R3")$
S[2] : S[2] - S[2][3].S[3]$
S;
print(" ");

print("R1 -> R1 - ",float(S[1][3])," * R3")$
S[1] : S[1] - S[1][3].S[3]$
S;
print(" ");

print("R1 -> R1 - ",float(S[1][2])," * R2")$
S[1] : S[1] - S[1][2].S[2]$
S;
print(" ");

print("The Solution Matrix is: ")$
X=col(S,4);
Now, the augmented matrix will be,
(%o6) 
$$\begin{pmatrix} 0.0 & -3.0 & 7.0 & 2.0 \\ 1.0 & 2.0 & -1.0 & 3.0 \\ 5.0 & -2.0 & 0.0 & 2.0 \end{pmatrix}$$


(%o7)
Now, the Echelon Form is,
(%o9) 
$$\begin{pmatrix} 1 & -0.4 & 0 & 0.4 \\ 0 & 1 & -0.4166666666666666 & 1.0833333333333333 \\ 0 & 0 & 1 & 0.9130434782608696 \end{pmatrix}$$


(%o10)
R2 → R2 - -0.4166666666666666 * R3

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5 Q5. Show that the following system of equations have infinite number of solutions :

$$\begin{aligned}x + y - 3z &= 4 \\2x + y - z &= 2 \\3x + 2y - 4z &= 6.\end{aligned}$$

```

→ kill(all)$
keepfloat:true$
A:matrix( /*...Coefficient Matrix...*/
  [1.0, 1.0, -3.0],
  [2.0, 1.0, -1.0],
  [3.0, 2.0, -4.0])$
B:matrix( /*...Constants Matrix...*/
  [4.0], [2.0], [6.0])$
X:matrix( /*...Variables Matrix...*/
  [x], [y], [z])$

print("Now, the augmented matrix will be,")$
Aug:addcol(A,B); /*...Creating Augmented Matrix...*/
print(" ");

print("Now, the Echelon Form is,")$
S : echelon(Aug); /*..Calculates Echolen Form of Matrix..*/
print(" ");

print("R2 -> R2 - ",float(S[2][3])," * R3")$
S[2] : S[2] - S[2][3].S[3]$
S;
print(" ");

print("R1 -> R1 - ",float(S[1][3])," * R3")$
S[1] : S[1] - S[1][3].S[3]$
S;
print(" ");

print("R1 -> R1 - ",float(S[1][2])," * R2")$
S[1] : S[1] - S[1][2].S[2]$
S;
/*..The last row after solving the matrix consists of all zeroes
this shows that the given set of equations has infinite number of
solutions...*/

```

Now, the augmented matrix will be,

(%o6)

$$\begin{pmatrix} 1.0 & 1.0 & -3.0 & 4.0 \\ 2.0 & 1.0 & -1.0 & 2.0 \\ 3.0 & 2.0 & -4.0 & 6.0 \end{pmatrix}$$

(%o7)

Now, the Echelon Form is,

(%o9)

$$\begin{pmatrix} 1 & 1.0 & -3.0 & 4.0 \\ 0 & 1 & -5.0 & 6.0 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

(%o10)

R2 → R2 - -5.0 * R3

(%o13)

$$\begin{pmatrix} 1 & 1.0 & -3.0 & 4.0 \\ 0 & 1 & -5.0 & 6.0 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$