

Practical 2(b) :

Regula-Falsi method

Theory: Regula falsi method iteratively determines a sequence of root enclosing intervals, (a_n, b_n) containing the approximate root p_n . Like in Bisection method, the interval under consideration must follow $f(a_n)f(b_n) < 0$ however, p_n is no longer the mid point of the interval (a_n, b_n) . In Regula falsi, p_n is the x intercept of the line joining $(a_n, f(a_n))$ and $(b_n, f(b_n))$. p_n is given by the following formula:

$$p_n = b_n - f(b_n) [b_n - a_n] / f(b_n) - f(a_n) \\ = (a_n \cdot f(b_n) - b_n \cdot f(a_n)) / f(b_n) - f(a_n)$$

Q1 Perform 10 iterations of the Regula-Falsi method to obtain a real root of the following equation in the interval $(-1, 1)$:

$$f(x) = x^3 - 5x + 1 = 0.$$

Solution:

```

→ kill(all)$
f(x):=x^(3)-5·x+1;
'x0=x0:-1.0;
'x1=x1:1.0;
n:10$
if(float(f(x0)·f(x1)>0)) then
print("change values")
else
for i:1 thru n do
(x2:float(((x0·f(x1))-(x1·f(x0)))/(f(x1)-f(x0))),
  if (f(x2)·f(x1)<0) then x0:x2 /*If f(x2)f(x1) < 0,
  then it means x2 and x1 are of opposite signs. The new interval
  is (x2,x1), so we do the replacement x0:x2.*/
  else (x1:x2),print("iteration",i,"gives",x2))$
print("After",n," iterations the root is",x2)$
wxplot2d(f(x),[x,-1,1]);

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(%o1) $f(x) := x^3 - 5x + 1$

(%o2) $x_0 = -1.0$

(%o3) $x_1 = 1.0$

iteration 1 gives 0.25

iteration 2 gives 0.1940298507462687

iteration 3 gives 0.2016886549593477

iteration 4 gives 0.2016397213245381

iteration 5 gives 0.201639675765857

iteration 6 gives 0.2016396757234442

iteration 7 gives 0.2016396757234047

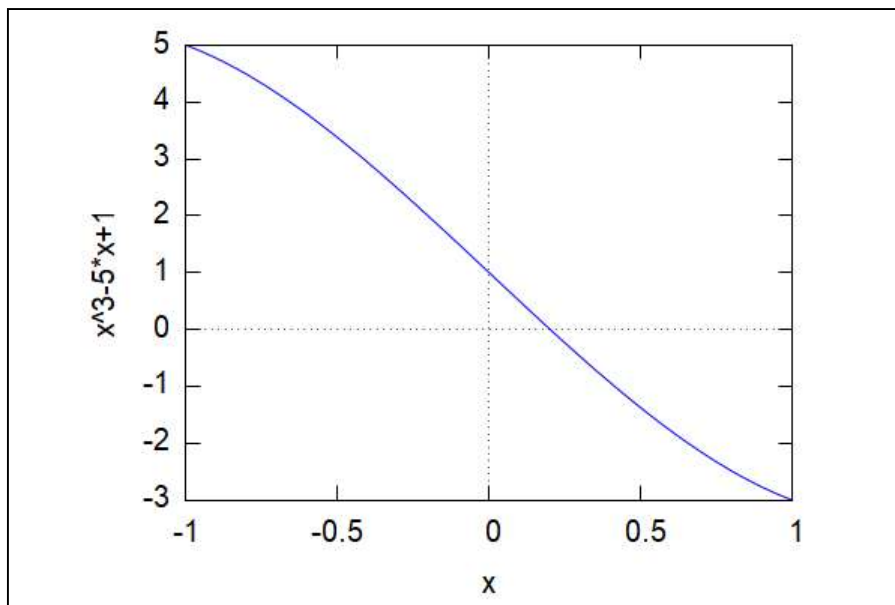
iteration 8 gives 0.2016396757234046

iteration 9 gives 0.2016396757234047

iteration 10 gives 0.2016396757234047

After 10 iterations the root is 0.2016396757234047

(%t7)



(%o7)

Q2 Perform 6 iterations of the Regula-Falsi method to obtain a real root of the following equation in the interval $(-1,1)$:

$$f(x) = x^2 - 4 = 0.$$

Solution:

```
→ kill(all)$
f(x):=x^(2)-4;
x0=x0:-1.0;
x1=x1:1.0;
n:6$
if(float(f(x0)·f(x1)>0)) then
print("change values")
else
for i:1 thru n do
(x2:float(((x0·f(x1))-(x1·f(x0)))/(f(x1)-f(x0))),
  if (f(x2)·f(x1)<0) then x0:x2
  else (x1:x2),print("iteration",i,"gives",x2))$
print("After",n," iterations the root is",x2)$

(%o1) f(x):=x2-4
(%o2) x0=-1.0
(%o3) x1=1.0
change values
After 6 iterations the root is x2
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Assignment: Do two similar questions.