

Ternary Search, Comparison Sort Selection, Bubble Sort

⇒ Ternary Search

0	1	2	3	4	5	6	7	8
20	25	47	56	59	63	65	79	82

$\underbrace{\hspace{1.5cm}}_{m_1}$
 $\underbrace{\hspace{1.5cm}}_{m_2}$

$$\left. \begin{aligned} \text{mid1} &= i + (j-i)/3 \\ \text{mid2} &= j - (j-i)/3 \end{aligned} \right\} \text{Getting 2 mids}$$

$i \rightarrow$ Left Index

$j \rightarrow$ Right Index

i.e $\text{mid1} = 0 + 8/3 = 2$

$\text{mid2} = 8 - 8/3 = 6$

key = 79

1st Path $\rightarrow i, \text{mid1} - 1$

2nd Path $\rightarrow \text{mid1} + 1 \rightarrow \text{mid2} - 1$

3rd Path $\rightarrow \text{mid2} + 1, j$

↳ 3 paths to access 3 parts of array.

ternarySearch(arr, i, j, key):

while $i \leq j$: \rightarrow covers corner cases

if $arr[mid1] == key$:

return mid1 \rightarrow Return mid1

if $arr[mid2] == key$:

return mid2

if $key < arr[mid1]$:

return ternarySearch(arr, i, mid1-1, key)

\rightarrow Navigating to 1st path since key is less than mid1

elif $key > arr[mid2]$:

return ternarySearch(arr, mid2+1, j, key)

\rightarrow Since $key > mid2$ navigate to 3rd path.

else:

return ternarySearch(arr, mid1+1, mid2-1, key)

\rightarrow Navigating to the 2nd path if key

is present.

return -1

Recurrence Relation

$$T(n) = T(n/3) + C$$

$$= T(n/3^2) + C + C = T(n/3^2) + 2C$$

$$= T(n/3^3) + C + C + C = T(n/3^3) + 3C$$

↓ k times

$$n/3^k = 1$$

$$n = 3^k \Rightarrow k = \log_3 n$$

↳ According to log Properties

$$T(n/3^k) + C \cdot k$$

$$\Rightarrow T\left(\frac{n}{3^{\log_3 n}}\right) + C \cdot \log_3 n$$

$$\Rightarrow T\left(\frac{n}{n \log_3}\right) + C \cdot \log_3 n$$

$$\Rightarrow \underline{O(\log_3 n)} \quad \Bigg| \quad \begin{array}{l} \text{Time} \\ \text{complexity} \end{array}$$

Binary Search

Ternary Search

$$O(\log_2 n) > O(\log_3 n)$$

Adobe Interview Question:

Assignment Problem:-

→ Binary Search is more preferable than Ternary Search why??

Lower the Base higher the value in log properties

Difference b/w Binary & Ternary Search

→ Interview Question

(Technical Round Adobe)

Sorting

Comparison-based
Sorting
⇓

Compare the
elements inside
the Array

Non-comparison
based sorting

No comparison within
the elements.

1> Bubble Sort

1> Count Sort

2> Selection Sort

2> Radix Sort

3> Insertion Sort

3> Bucket Sort

4> Quick Sort } Divide & conquer
5> Merge Sort } module

6> Heap Sort

7> Shell Sort

Stable & Unstable Sort

20, 10^a, 5, 15, 10^b, 25, 45

⇓ sorting Algo

20, 10^a, 10^b, 15, 20, 25, 45

⇓ Merge Sort.
Stable sort

→ 20, 10^b, 10^a, 15, 20, 25, 45

⇓ Not a stable sorting Algo.

QuickSort, HeapSort

↳ Not stable sorting Algo.

↳ Does stable or unstable sort matter while sorting?

Index	Name	Sort
→ 23	Suraj	89
47	Suraj	45
150	Suraj	100
171	↓ Suraj	69

↳ Always Stable sort.

Inplace & Outplace Sorting

arr = [— — — — —]

↳ extra space → new Array

↳ Outspace Sorting ⇒ Merge sort

↳ Taking extra space

In place sorting is sorting an array without any extra space.

Swaps:

Best case $\rightarrow 0$

Worst case $\rightarrow (n-1) + (n-2) + \dots + 1$
 $\Rightarrow O(n^2)$

10, 20, 30, 40 \Rightarrow Best case for swaps

40, 30, 20, 10 \Rightarrow worst case for swaps

Time complexity \rightarrow

no. of comparisons + no. of swaps

\downarrow

$n^2 + n^2$

$\Rightarrow \underline{\underline{O(n^2)}}$

Why $(n-1)$?

We get one largest number at each iteration & hence we get length-1, length-2 till last element is reached.

Selection Sort

0 1 2 3 4 5 6
70, 20, 50, 30, 90, 5, 15

$i=0 \rightarrow$ start index

$\text{min} = 0$ & it compares with next index

\rightarrow used to store the index of minimum element

Pass 1:-

0 1 2 3 4 5 6
5, (20, 50, 30, 90, 70, 15) $i=1, \text{min}=1$

\rightarrow Only one swap happens which reduces the costs.

\rightarrow Smallest number will be at first pass.

Pass 2:-

0 1 2 3 4 5 6
5, 15, (50, 30, 90, 70, 20)

Pass 3:-

0 1 2 3 4 5 6
5, 15, 20, (30, 90, 70, 50)

$i=3, \text{min}=3$

Pass 4:-

0 1 2 3 4 5 6
5, 15, 20, 30, (90, 70, 50)

$i=4, \text{min}=4 \& 6$

Pass 5: 5, 15, 20, 30, 50, 70, 90

\Downarrow
Sorted Array

of comparisons
 $\Rightarrow (n-1) + (n-2) + (n-3) + \dots + 1$

$$\Rightarrow \frac{(n-1)n}{2} \Rightarrow O(n^2)$$

of swaps $\Rightarrow 1 + 1 + 1 + 1 + \dots + (n-1)$

$$\Rightarrow O(n)$$

Time complexity \Rightarrow # comparison
+ # swaps

$$\Rightarrow n^2 + n$$

$$\Rightarrow \underline{\underline{O(n^2)}}$$

Here we reduce number of swaps
required so selection sort is better
than Bubble sort than for
lesser cost operations