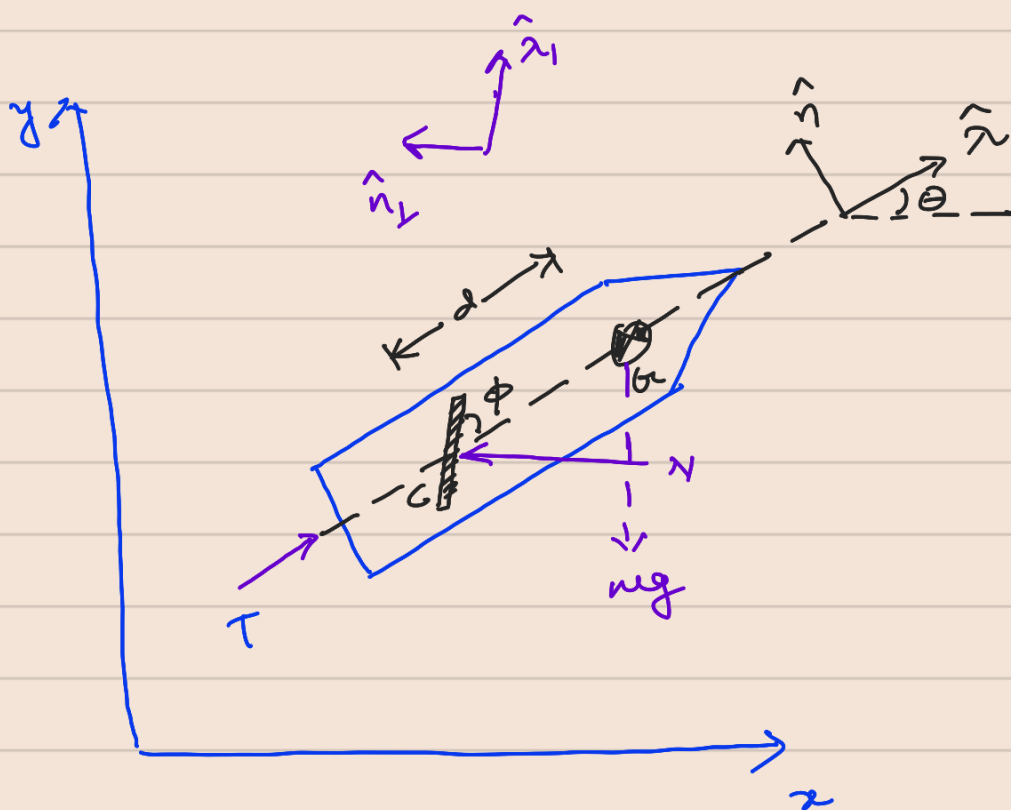


①



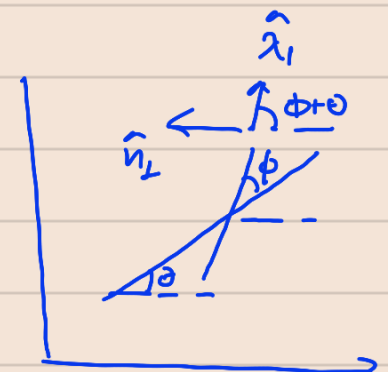
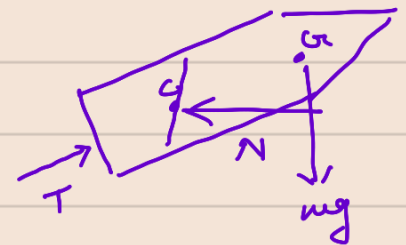
AMB:

$$\vec{T} + \vec{N} + m\vec{g} = m \vec{a}_G$$

$$T \hat{\lambda} + N \hat{n}_\perp - mg \hat{j} = m \vec{a}_G \quad (1)$$

$$\rightarrow \omega \theta \hat{i} + \omega \phi \hat{j}$$

$$\hat{n}_\perp = -\sin(\theta + \phi) \hat{i} + \cos(\theta + \phi) \hat{j}$$



(1) · i :

$$T \hat{\lambda} \cdot \hat{i} + N \hat{n}_\perp \cdot \hat{i} - mg \hat{j} \cdot \hat{i} = m \vec{a}_G \cdot \hat{i}$$

$$T \cos \theta - N \sin(\theta + \phi) = m \ddot{x}_G \quad (2)$$

(1) · j :

$$T \hat{\lambda} \cdot \hat{j} + N \hat{n}_\perp \cdot \hat{j} - mg \hat{j} \cdot \hat{j} = m \vec{a}_G \cdot \hat{j}$$

$$T \sin \theta + N \cos(\theta + \phi) - mg = m \ddot{y}_G \quad (3)$$

AMB:

$$\sum \vec{M}_G = \vec{H}_G$$

\rightarrow Angular momentum

$$\Rightarrow \vec{r}_{GC} \times \vec{N} = I_G \ddot{\theta} \hat{k} \quad (4)$$

Constraint: $\vec{V}_C \cdot \hat{n}_1 = 0$

$$\Rightarrow \frac{d}{dt} (\vec{V}_C \cdot \hat{n}_1) = 0 \Rightarrow \frac{d}{dt} (f(\theta, \phi, v_{Gx}, v_{Gy}, \dot{\theta}, \dot{\phi}))$$

$$\Rightarrow \dot{\vec{V}}_C \cdot \hat{n}_1 + \vec{V}_C \cdot \dot{\hat{n}}_1 = 0$$

$$V_C = V_G + \vec{V}_{C/G} \xrightarrow{\omega \times} \vec{\omega} \times \vec{r}_{C/G} \xrightarrow{\downarrow \dot{\theta} \hat{k}} d\hat{n}$$

$$\begin{bmatrix} \dot{x}_G \\ \dot{y}_G \end{bmatrix}$$

$$\hat{n}_1 = -\sin(\theta + \phi) \hat{i} + \cos(\theta + \phi) \hat{j}$$

Dynamics:

$$x = (\tau_G, \theta, v_G, \dot{\theta}), \quad y = \phi$$

$$u = [T, \dot{\phi}], \quad \dot{z} = [x, y]$$

$$\dot{x} = f(x, u), \quad \dot{y} = g(u)$$

$$\dot{z} = \begin{bmatrix} f(x, u) \\ g(u) \end{bmatrix}$$

coded
using symbolic
matlab

Dyn Eqn from matlab:

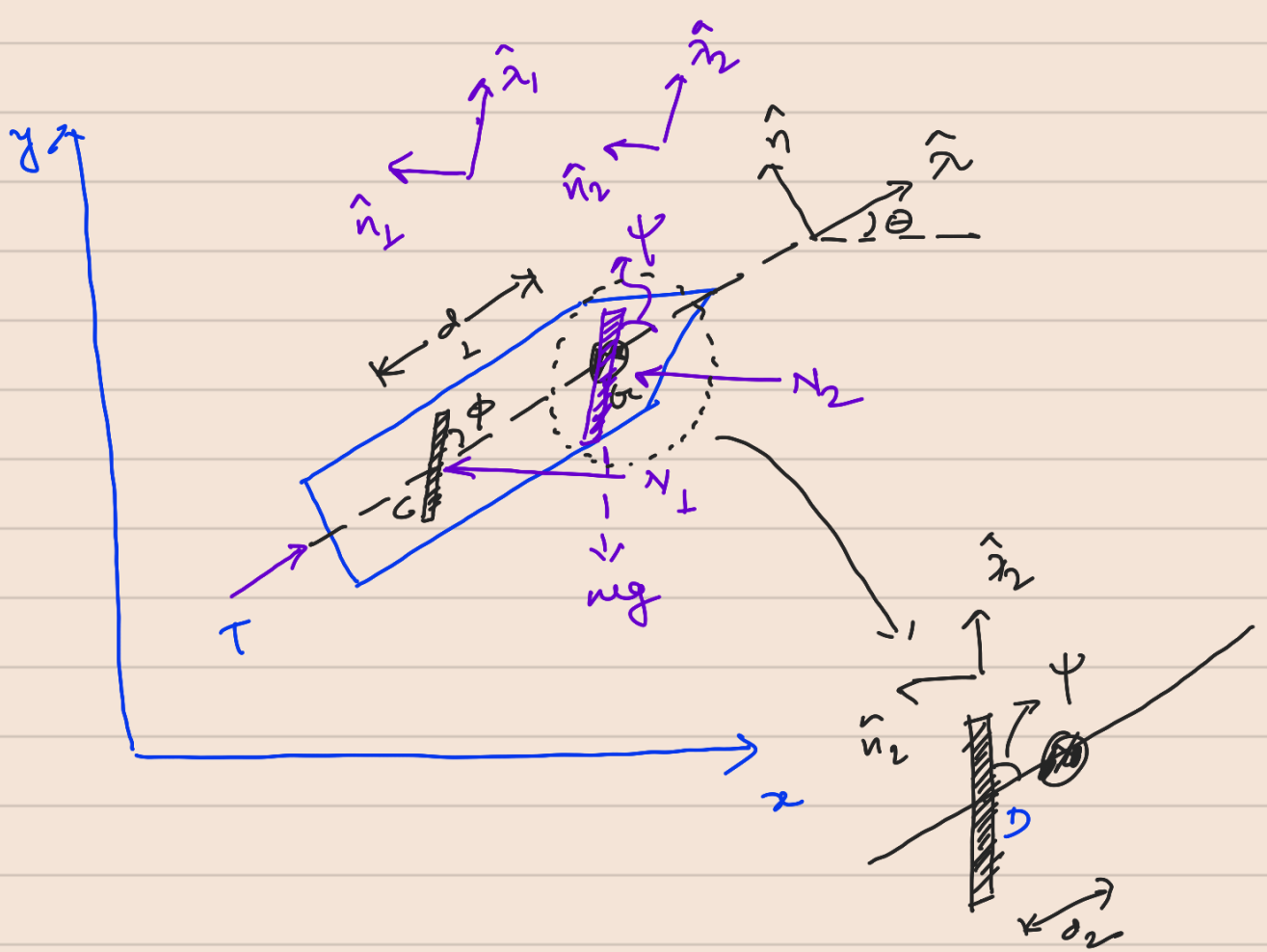
$$T \cos \theta - N \sin(\phi + \theta) = m \ddot{x}$$

$$T \sin \theta + N \cos(\phi + \theta) - m g = m \ddot{y}$$

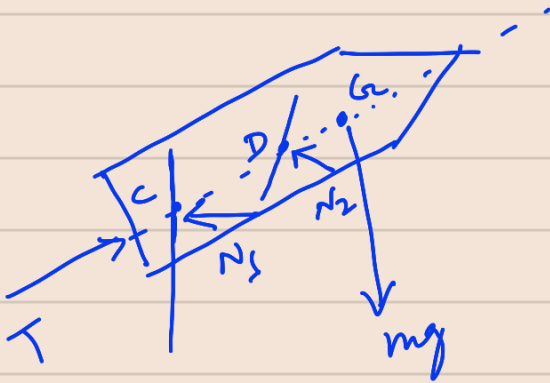
$$-N d \cos(\phi + \theta) d\theta - N d \sin(\phi + \theta) d\phi = I_G \ddot{\omega}$$

$$\ddot{x} + c(\phi + \theta) - \ddot{u} \sin(\phi + \theta) - \omega \dot{x} \cos(\phi + \theta) - \dot{\phi} \dot{x} \sin(\phi + \theta) - \alpha d \cos \phi - \omega \dot{y} \sin(\phi + \theta) - \dot{\phi} \dot{y}$$

(2)



FBD



$$\begin{aligned} \hat{n}_1 &= -s(\theta + \phi) \hat{i} + c(\theta + \phi) \hat{j} \\ \hat{n}_2 &= -s(\theta + \psi) \hat{i} + c(\theta + \psi) \hat{j} \end{aligned}$$

LMB:

$$\begin{aligned} \vec{T} + \vec{mg} + \vec{N}_1 + \vec{N}_2 &= m \vec{a}_G \\ \Rightarrow T \hat{\lambda} + mg(-\hat{k}) + N_1 \hat{n}_1 + N_2 \hat{n}_2 &= m \vec{a}_G \quad (1) \end{aligned}$$

AMB: $\vec{r}_{GC} \times N_1 + \vec{r}_{GD} \times N_2 = I_G \ddot{\theta} \hat{k}$

Constraint:

$$\begin{aligned} \vec{v}_C \cdot \hat{n}_1 &= 0 \\ \vec{v}_D \cdot \hat{n}_2 &= 0 \end{aligned}$$

