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R. V. COLLEGE OF ENGINEERING
Autonomous Institution affiliated to VTU
IV Semester B. E. Examinations Oct/Nov-2022
Computer Science and Engineering
THEORY OF COMPUTATION

*Time: 03 Hours**Maximum Marks: 100***Instructions to candidates:**

1. Answer all questions from Part A. Part A questions should be answered in first three pages of the answer book only.
2. Answer FIVE full questions from Part B. In Part B question number 2, 7 and 8 are compulsory. Answer any one full question from 3 and 4 & one full question from 5 and 6.

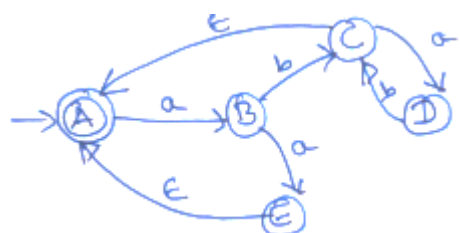
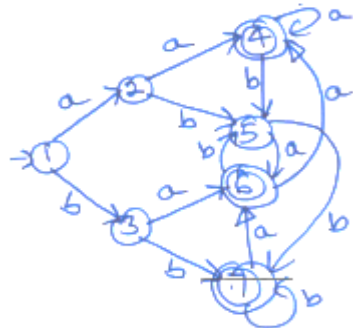


PART A

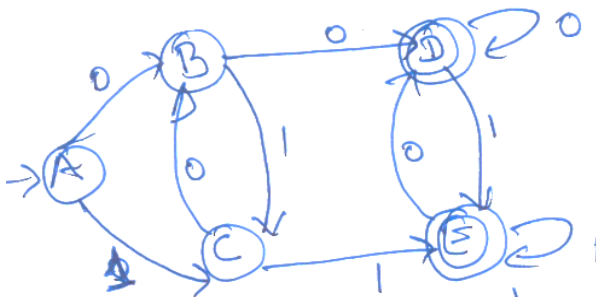
1	1.1	Construct DFA which recognizes language corresponds to the regular expression $(0+11^*0)(0+1)^*$.	02
	1.2	Give the regular expression which generates the language "The set of all strings over $\Sigma=\{0, 1\}$ contains at least two 0's".	01
	1.3	Show that the grammar which indicated productions is ambiguous. $S \rightarrow AB \mid aaB, A \rightarrow a \mid Aa, B \rightarrow b$.	01
	1.4	Identify the language generated by the grammar with productions $S \rightarrow aaS \mid bbS \mid Saa \mid Sbb \mid abSab \mid abSba \mid baSba \mid baSab \mid \epsilon$.	02
	1.5	How many useless variables are in the grammar $S \rightarrow AB \mid AC, A \rightarrow aAb \mid bAa \mid a, B \rightarrow bbA \mid aaB \mid AB, C \rightarrow abCa \mid aDb, D \rightarrow bD \mid ac$.	01
	1.6	Identify the nullable variables in the grammar $S \rightarrow ABCa \mid bD, A \rightarrow BC \mid b, B \rightarrow b \mid \epsilon, C \rightarrow c \mid \epsilon, D \rightarrow d$.	01
	1.7	Write the left linear grammar equivalent to the below right linear grammar. $A \rightarrow aB \mid bD \mid a, B \rightarrow aA \mid bc, C \rightarrow aD \mid bB \mid b, D \rightarrow aC \mid bA$.	02
	1.8	Construct the parser tree for the string aaabaabba from the grammar with productions. $S \rightarrow SS \mid bTT \mid TbT \mid TTB \mid \epsilon, T \rightarrow aS \mid SAS \mid Sa \mid a$	02
	1.9	To derive a string aaabbababb from the grammar with productions $S \rightarrow aB \mid bA, A \rightarrow a \mid aS \mid bAA, B \rightarrow b \mid bS \mid aBB$. How many steps are there in the derivation.	01
	1.10	Write the transition diagram of the tuning machine which accepts the language $L=\{W \mid W \in \{a,b\}^* \text{ and } W \text{ ends with } abb\}$.	02
	1.11	Describe the language generated by the unrestricted grammar with the productions $S \rightarrow FM, F \rightarrow FaA \mid FbB \mid \epsilon$ $Aa \rightarrow aA, Ab \rightarrow bA, Ba \rightarrow aB, Bb \rightarrow bB,$ $AM \rightarrow Ma, BM \rightarrow Mb, M \rightarrow \epsilon$	02
	1.12	If L_1 and L_2 are recursively numerable languages over Σ , then $L_1 \cup L_2$ is _____.	01

1.13	Find the solution to the below instance of port correspondence problem	i	A	B
		1	10	101
		2	01	100
		3	0	10
		4	100	0
		5	1	010

02

PART B

2	a	Explain the algorithm to find an equivalent NFA from the given NFA for the NFA- ϵ . Use the algorithm to draw an NFA for the NFA- ϵ given below.	8
	b	Explain the algorithm to minimize the states in DFA. Minimize the DFA below.	
		 	8
3	a	State and prove the pumping lemma for regular languages. Use pumping lemma to show the language $L = \{WW \mid W \in \{0,1\}^*\}$ is not regular.	10
	b	Let M_1 and M_2 are the two DFA's pictured below which recognizes language L_1 and L_2 respectively. Find DFA's for i) L_1 ii) $L_1 \cup L_2$ iii) $L_1 \cap L_2$	
		 	06
		OR	
4	a	Give the context free grammars which generates the following languages i) $L_1 = \{a^i b^j c^k \mid i=j \text{ or } j=k\}$ ii) $L_2 = \{a^i b^j c^k \mid i=j+k\}$	08

	b	Find the context free grammar with the productions as follows, find an equivalent grammar in Chomsky normal form $S \rightarrow AaA \mid CA \mid BaB$ $A \rightarrow aaBa \mid CDA \mid aa \mid DC$ $B \rightarrow bB \mid bAB \mid bb \mid aS$ $C \rightarrow Ca \mid bC \mid bb \mid a \mid b$ $D \rightarrow bD \mid b$	04
	c	Find the equivalent grammar by eliminating left recursion in the grammar with productions $S \rightarrow 0S1 \mid 1S0 \mid 01S \mid 10S \mid S01 \mid S10 \mid \epsilon$	04
5	a	Construct PDA to recognize $L = \{W \mid W \in \{a, b\}^* \text{ and } W \text{ is a palindrome}\}$. Show by using instantaneous descriptions the abbbba is accepted.	08
	b	What are the steps to be followed find an equivalent PDA from the given CFG. Find the PDA which is equivalent to the below grammar. $S \rightarrow S + S \mid S - S \mid S \times S \mid S / S \mid (S) \mid a$ Let $W = (a + a) \times a$. Show that this string is accepted by the equivalent PDA constructed.	08
		OR	
6	a	State and prove pumping lemma for CFLs. Apply this lemma on $L = \{WW \mid W \in \{a, b\}^*\}$ is not context free.	08
	b	Show that the context free language are closed under union operation but not closed under intersection operation.	04
	c	Describe the algorithms for the following decision problem. "Given a CFG, is $L(G)$ is finite or empty".	04
7	a	Give the equivalent left linear grammar for the language accepted by the finite automata whose transition diagram shown below: 	08
	b	Write the DFA such that the language of the DFA is same as the language generated by the grammar $B \rightarrow Aa \mid Cb \mid a,$ $C \rightarrow Da \mid Bb,$ $D \rightarrow Ca \mid Ab \mid b,$ $A \rightarrow Ba \mid Db$	08
8	a	Design Turing machine which accepts the language $L = \{W \mid W \in \{a, b\}^* \text{ and } W \text{ is a palindrome}\}$. Using instantaneous descriptions show that the string babbab is accepted by the Turing machine.	08
	b	Write a note on the following: i) Multitape Turing machine ii) Chomsky hierarchy	08