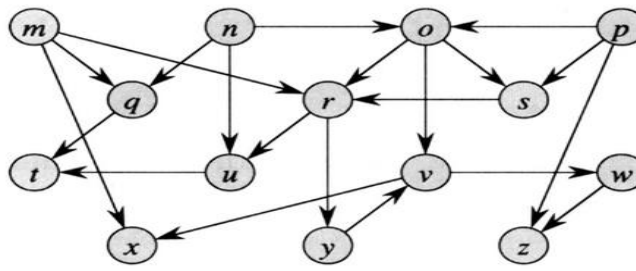


## Department of Computer Science and Engineering

## Program: BE

Date	July 2024	Maximum Marks	10+50
Course Code	CD343AI	Duration	120 min
Sem	IV	CIE-II(Scheme and solution)	
Design and Analysis of Algorithms (Common to AIML/CSE/CD/CY/ISE)			

Sl. No.	Questions	M
	<b>PART A</b>	
1.1	Yes, Run the DFS or BFS from each vertex to find the path to all other vertices.	2
1.2	27	2
1.3	$O(n)$	2
1.4	No matter how many edges are there in the graph the Floyd's Algorithm runs for $O(V^3)$ times therefore it is best suited for Dense graphs.	2
1.5	1. Limited to Integer Sorting 2. Memory Consumption 3. Range Limitation 4. Not Adaptive to the data's distribution or partially sorted input 5. Stability Concerns 6. Preprocessing Overhead	2
	<b>PART B</b>	
1a	<p>Apply DFS traversal to find the topological order of the graph shown in figure 1a from the vertex p (break the ties by the alphabetical order of the vertices)</p>  <p>Topological order: n m q p o s r y v x w z u t</p>	06
1b	<b>Brute force :</b> Time Complexity: $O(N^2)$ ----0.5M	04

	<b>Instance simplification method(Presorting)</b> Time Complexity: O(N * logN)----0.5M Comparison with algorithm ---02M																																																																																																																																
2a	<table><tr><td colspan="2">Array A[0---6]</td><td>94</td><td>73</td><td>26</td><td>11</td><td>05</td><td>77</td><td>31</td></tr><tr><td>Initially</td><td>Count[]</td><td>0</td><td>0</td><td>0</td><td>0</td><td>0</td><td>0</td><td>0</td></tr><tr><td>After pass</td><td>i=0</td><td>6</td><td>0</td><td>0</td><td>0</td><td>0</td><td>0</td><td>0</td></tr><tr><td></td><td>i=1</td><td></td><td>4</td><td>0</td><td>0</td><td>0</td><td>1</td><td>0</td></tr><tr><td></td><td>i=2</td><td></td><td></td><td>2</td><td>0</td><td>0</td><td>2</td><td>1</td></tr><tr><td></td><td>i=3</td><td></td><td></td><td></td><td>1</td><td>0</td><td>3</td><td>2</td></tr><tr><td></td><td>i=4</td><td></td><td></td><td></td><td></td><td>0</td><td>4</td><td>3</td></tr><tr><td></td><td>i=5</td><td></td><td></td><td></td><td></td><td></td><td>5</td><td>3</td></tr><tr><td></td><td>Index of the item in the final array</td><td>6</td><td>4</td><td>2</td><td>0</td><td>3</td><td>5</td><td>1</td></tr><tr><td colspan="2">Array S[0----6]</td><td>05</td><td>11</td><td>26</td><td>31</td><td>73</td><td>77</td><td>94</td></tr></table>								Array A[0---6]		94	73	26	11	05	77	31	Initially	Count[]	0	0	0	0	0	0	0	After pass	i=0	6	0	0	0	0	0	0		i=1		4	0	0	0	1	0		i=2			2	0	0	2	1		i=3				1	0	3	2		i=4					0	4	3		i=5						5	3		Index of the item in the final array	6	4	2	0	3	5	1	Array S[0----6]		05	11	26	31	73	77	94	06																														
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2b	<b>ALGORITHM</b> <i>Warshall(A[1..n, 1..n])</i> //Implements Warshall's algorithm for computing the transitive closure //Input: The adjacency matrix A of a digraph with n vertices //Output: The transitive closure of the digraph $R^{(0)} \leftarrow A$ <b>for</b> k $\leftarrow$ 1 <b>to</b> n <b>do</b> <b>for</b> i $\leftarrow$ 1 <b>to</b> n <b>do</b> <b>for</b> j $\leftarrow$ 1 <b>to</b> n <b>do</b> $R^{(k)}[i, j] \leftarrow R^{(k-1)}[i, j] \text{ or } (R^{(k-1)}[i, k] \text{ and } R^{(k-1)}[k, j])$ <b>return</b> $R^{(n)}$  -----02M  Proof-----02M								04																																																																																																																								
3a	<b>Heap construction -----01M</b> <table><tr><td>8</td><td>12</td><td>15</td><td>3</td><td>5</td><td>1</td><td>43</td><td>-7</td></tr><tr><td>8</td><td>12</td><td>43</td><td>3</td><td>5</td><td>1</td><td>15</td><td>-7</td></tr><tr><td>43</td><td>12</td><td>8</td><td>3</td><td>5</td><td>1</td><td>15</td><td>-7</td></tr><tr><td>43</td><td>12</td><td>15</td><td>3</td><td>5</td><td>1</td><td>8</td><td>-7</td></tr></table> <b>Maximum deletion----02M</b> All Heap construction iteration in the process of sorting -----03M <table><tr><td>43</td><td>12</td><td>15</td><td>3</td><td>5</td><td>1</td><td>8</td><td>-7</td></tr><tr><td>-7</td><td>12</td><td>15</td><td>3</td><td>5</td><td>1</td><td>8</td><td>43</td></tr><tr><td>15</td><td>12</td><td>8</td><td>3</td><td>5</td><td>1</td><td>-7</td><td></td></tr><tr><td>-7</td><td>12</td><td>8</td><td>3</td><td>5</td><td>1</td><td>15</td><td></td></tr><tr><td>12</td><td>5</td><td>8</td><td>3</td><td>-7</td><td>1</td><td></td><td></td></tr><tr><td>1</td><td>5</td><td>8</td><td>3</td><td>-7</td><td>12</td><td></td><td></td></tr><tr><td>8</td><td>5</td><td>1</td><td>3</td><td>-7</td><td></td><td></td><td></td></tr><tr><td>-7</td><td>5</td><td>1</td><td>3</td><td>8</td><td></td><td></td><td></td></tr><tr><td>5</td><td>3</td><td>1</td><td>-7</td><td></td><td></td><td></td><td></td></tr><tr><td>-7</td><td>3</td><td>1</td><td>5</td><td></td><td></td><td></td><td></td></tr><tr><td>3</td><td>-7</td><td>1</td><td></td><td></td><td></td><td></td><td></td></tr></table>								8	12	15	3	5	1	43	-7	8	12	43	3	5	1	15	-7	43	12	8	3	5	1	15	-7	43	12	15	3	5	1	8	-7	43	12	15	3	5	1	8	-7	-7	12	15	3	5	1	8	43	15	12	8	3	5	1	-7		-7	12	8	3	5	1	15		12	5	8	3	-7	1			1	5	8	3	-7	12			8	5	1	3	-7				-7	5	1	3	8				5	3	1	-7					-7	3	1	5					3	-7	1						06
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<b>K</b>	<b>N</b>	<b>A</b>	<b>R</b>	<b>*</b>
4	1	3	2	11

K	Pattern	$d_2$
1	RNARNAK <u>ARNA</u>	3
2	RNARNAKARNA	11
3	RNARNAKARNA	8
4	RNARNAKARNA	5
5	RNARNAKARNA	8
6	RNARNAKARNA	8
7	RNARNAKARNA	8
8	RNARNAKARNA	8
9	R <u>N</u> ARNAKARNA	8
10	RNARNAKARNA	8

10

### Good suffix table-----04M

R	A	V	A	N	A	K	A	R	N	A	-	R	A	M	A	Y	A	N	A	-	E	P	I	C	-	S	E	E	T	H	A	-	-	-	N	N	A	R	N	A	-	R	N	A	R																
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N	N	A	R	N	A		R	N	A	R	N	A	K	A	R	N	A
R	N	A	R	N	A	K	A	R	N	A	d1=2						
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		R	N	A	R	N	A	K	A	R	N	A	d1=1, d2=5				
							R	N	A	R	N	A	K	A	R	N	A

*Go, change the world<sup>®</sup>*