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RV COLLEGE OF ENGINEERING®

Autonomous Institution affiliated to VTU V Semester B. E. Examinations Jab/Feb-21

Computer Science and Engineering

Computer Science and Engineering

ADVANCED ALGORITHMS (ELECTIVE)

Time: 03 Hours

Maximum Marks: 100

Instructions to candidates:

- 1. Answer all questions from Part A. Part A questions should be answered in first three pages of the answer book only.
- 2. Answer FIVE full questions from Part B. In Part B question number 2, 7 and 8 are compulsory. Answer any one full question from 3 and 4 & one full question from 5 and 6

PART-A

| 1 | 1.1 | Compute $\sum_{1 \le k \le n} O(n)$. | 02 |
|---|------|--|----|
| | 1.2 | Solve the following recurrence relation | |
| | | $T(n) = 3T(n/2) + n^2$. | 02 |
| | 1.3 | State the basic principle of Rabin Karp algorithm. | 01 |
| | 1.4 | What is the number of edges present in a complete graph having n | |
| | | vertices? | 01 |
| | 1.5 | Bellmann ford algorithm provides solution for problems. | 01 |
| | 1.6 | Find the GCD of 244 and 117 using Euclid's method. | 02 |
| | 1.7 | What is the special property of red-black trees and what root should | |
| | | always be? | 02 |
| | 1.8 | Consider the following graph: | |
| | 1.9 | Find the minimum cost to travel from node A to node C. Show the result of inserting 50 into the Red-Black tree depicted below: | 02 |
| | | 30 | |
| | | | |
| | | | |
| | | 15 45 | |
| | | | |
| | | 35 60 | |
| | | | |
| | | 55 | |
| | | 35 | 02 |
| | 1.10 | What are splay trees? | 01 |

| 1.11 1.12 1.13 | What is the time complexity of Johnson's algorithm? What is the worst-case running time of Rabin-Karp algorithm? Obtain a splay tree for following tree, after inserting 40 to it. | 01 01 |
|----------------------|--|----------|
| | 80 | |
| | 50 90 | |
| | 30 70 | 02 |

PART-B

| 2 | a b | What are asymptotic notations? Explain them. Solve the following recurrence using master's theorem. Also state which case is applicable? | 06 |
|---|--------|--|----|
| | | which case is applicable? $T(n) = 4T(n/2) + n^2.$ | 05 |
| | c | Solve the following recurrence relation using recursion tree method. | |
| | | T(n) = 4T(n/2) + n. | 05 |
| 3 | а | Write the Naïve string matching algorithm. Show the operation of the | |
| | | same, for the pattern $p = 0001$ in the test. | |
| | _ | $T = 0\ 0\ 0\ 1\ 0\ 0\ 1\ 0\ 1\ 0\ 0\ 1$ | 08 |
| | b | Construct the string matching automation for the pattern $p = aabab$ and illustrate its operation on the text string. | |
| | | T = $a a a b a b a a b a a b a a b a b a a b$ | 08 |
| | | OR | |
| 4 | a | Demonstrate with an algorithm, the working procedure Bellman-Ford algorithm for solving single source shortest path problem for the graph shown below. | |
| | b | Write an algorithm for single-source shortest path in BAG. Also apply the algorithm for the following graph and taking source vertex as 's'. | 08 |
| | | E P | 08 |

| 5 | а | Find the maximum flow using basic ford Fulkerson algorithm. | |
|---|--------|--|----------|
| | b | Explain the properties of red-black tree. Construct a red-black tree by inserting following sequence of number: 8, 18, 5, 15, 17, 25, 40 & 80. | 08 |
| | | OR | |
| 6 | a | Define Fibonacci heap. Write an algorithm to extract minimum node from the Fibonacci heap. | 05 |
| | b | Describe how to find maximum bipartite matching for a given graph, considering suitable example. | 05 |
| | c | Perform the splay delete operation on the given tree shown in figure below to node x. | |
| | | (C) (G) | |
| | | 4 7 | |
| | | (2)2 | 06 |
| 7 | a | Write modular-linear-equation-solver algorithm and using the same, solve the following $14 \times \equiv 30 \pmod{100}$. | 08 |
| | b | Apply the Chinese remainder theorem, to the following equations: i) $a \equiv 2 \pmod{5}$ ii) $a \equiv 3 \pmod{13}$ | 08 |
| | | u = 3(muu + 13) | 08 |
| 8 | a b | Investigate the two trays of representing polynomials. Characterize the efficient implementation of iterative FFT. | 05 05 |
| | С | Characterize the pseudocode for Artificial Bee Colony (ABC) algorithm. | 06 |