

Quiz: Context-Free Grammars and Pushdown Automata

Section 1: Context-Free Grammars (CFGs) and Parse Trees

1. Which of the following is NOT a component of a context-free grammar (CFG)?

- A) A finite set of non-terminals
- B) A start symbol
- C) A stack
- D) A finite set of productions

Answer: C

2. A string that can be generated in more than one way by a CFG is called _____.

Answer: Ambiguous

3. All ambiguous grammars generate ambiguous languages.

Answer: False

4. Define a leftmost derivation in a CFG.

Answer: A derivation in which the leftmost non-terminal is always replaced at each step.

5. Which of the following is used to show ambiguity in a grammar?

- A) Left recursion
- B) Parse trees
- C) Finite automata
- D) Null productions

Answer: B

Section 2: Ambiguity in Grammars and Languages

6. Every ambiguous language must have at least one ambiguous grammar.

Answer: True

7. Which grammar is ambiguous for arithmetic expressions?

- A) $E \rightarrow E + E \mid E * E \mid id$
- B) $E \rightarrow id$
- C) $S \rightarrow aSb \mid$
- D) $A \rightarrow aA \mid a$

Answer: A

8. How do you remove ambiguity from a grammar for arithmetic expressions?

Answer: By defining operator precedence and associativity.

9. In a parse tree, the _____ is always the start symbol.

Answer: Root

10. Ambiguity can be completely removed from every CFG.

Answer: False

Section 3: Pushdown Automata (PDA)

11. Which of the following pairs correctly represents a transition in PDA?

A) $(q, a) = (p)$

B) $(q, a, Z) = \{(p,)\}$

C) $(q,) = (p, a)$

D) $(p, a, p) = q$

Answer: B

12. The stack in PDA allows it to recognize nested structures like balanced parentheses.

Answer: True

13. What is the purpose of ϵ -transitions in PDA?

Answer: To change states without consuming input, enabling non-determinism.

14. Which of the following languages cannot be accepted by a PDA?

A) $\{ ab \mid n \geq 0 \}$

B) $\{ abc \mid n \geq 0 \}$

C) $\{ w \mid w \in \{a,b\}^* \text{ and } w \text{ is a palindrome} \}$

D) $\{ ab \mid n > 0 \}$

Answer: B

15. PDA is to context-free languages as DFA is to _____.

Answer: Regular languages

16. A PDA can accept a language either by empty stack or by final state.

Answer: True

17. What happens if a PDA has no transition for a given input and stack symbol?

A) It crashes

B) It continues with an empty stack

C) It accepts

D) It loops infinitely

Answer: A

18. Why are PDAs more powerful than DFAs?

Answer: Because PDAs use a stack to recognize context-free languages.

Section 4: Equivalence of PDA and CFG

19. For every PDA, there exists an equivalent CFG that generates the same language.

Answer: True

20. Which of the following best represents the relationship between PDA and CFG?

- A) $PDA \subsetneq CFG$
- B) $PDA \supsetneq CFG$
- C) $PDA = CFG$
- D) $PDA \cap CFG = \emptyset$

Answer: C