

**SADS-II problem-11****Date: 24-04-2024**

Perspiration from a sample of 20 healthy females was analyzed. Three components,  $X_1$  = Sweet rate,  $X_2$  = Sodium content and  $X_3$  = Potassium content, were measured and the results, which we call the sweat data are given in the below table.

Sweat Data			
Individual	$X_1$ (Sweet rate)	$X_2$ (Sodium)	$X_3$ (Potassium)
1	3.7	48.5	9.3
2	5.7	65.1	8.0
3	3.8	47.2	10.9
4	3.2	53.2	12.0
5	3.1	55.5	9.7
6	4.6	36.1	7.9
7	2.4	24.8	14.0
8	7.2	33.1	7.6
9	6.7	47.4	8.5
10	5.4	54.1	11.3
11	3.9	36.9	12.7
12	4.5	58.8	12.3
13	3.5	27.8	9.8
14	4.5	40.2	8.4
15	1.5	13.5	10.1
16	8.5	56.4	7.1
17	4.5	71.6	8.2
18	6.5	52.8	10.9
19	4.1	44.1	11.2
20	5.5	40.9	9.4

Find the principal components of the above data and also find the proportion of total variation explained by first and second principal components.

**Solution:->** `setwd("D:\\dataset\\")`

```
> data=read.csv("principalcom.csv")
```

```
> data
```

```
      x1  x2  x3
1  3.7 48.5  9.3
2  5.7 65.1  8.0
3  3.8 47.2 10.9
4  3.2 53.2 12.0
5  3.1 55.5  9.7
6  4.6 36.1  7.9
7  2.4 24.8 14.0
8  7.2 33.1  7.6
9  6.7 47.1  8.5
10 5.4 54.1 11.3
11 3.9 36.9 12.7
12 4.5 58.8 12.3
13 3.5 27.8  9.8
```

```

14 4.5 40.2 8.4
15 1.5 13.5 10.1
16 8.5 56.4 7.1
17 4.5 71.6 8.2
18 6.5 52.8 10.9
19 4.1 44.1 11.2
20 5.5 40.9 9.4
> head(data)
  x1  x2  x3
1 3.7 48.5 9.3
2 5.7 65.1 8.0
3 3.8 47.2 10.9
4 3.2 53.2 12.0
5 3.1 55.5 9.7
6 4.6 36.1 7.9
> setwd("D:\\dataset\\")
> data=read.csv("principalcom.csv")
> head(data)
  x1  x2  x3
1 3.7 48.5 9.3
2 5.7 65.1 8.0
3 3.8 47.2 10.9
4 3.2 53.2 12.0
5 3.1 55.5 9.7
6 4.6 36.1 7.9
> ##step2: Standardize the data
> scale_data=scale(data)
> head(scale_data)
      x1      x2      x3
[1,] -0.55396106 0.2204127 -0.3491471
[2,]  0.62467949 1.3950038 -1.0316904
[3,] -0.49502903 0.1284267  0.4909061
[4,] -0.84862119 0.5529777  1.0684427
[5,] -0.90755322 0.7157222 -0.1391338
[6,] -0.02357281 -0.6569927 -1.0841937
> ##Step 3: Perform Principal Component Analysis (PCA)
> # Perform PCA
> pca_result <- prcomp(scale_data, scale. = TRUE)
> pca_result
Standard deviations (1, .., p=3):
[1] 1.3440666 0.8955140 0.6257313

Rotation (n x k) = (3 x 3):
      PC1      PC2      PC3
x1  0.6534351 -0.1023336 -0.7500336
x2  0.4870226  0.8153574  0.3130516
x3 -0.5795097  0.5698422 -0.5826219
> # Summary of PCA
> summary(pca_result)
Importance of components:
      PC1      PC2
Standard deviation  1.3441 0.8955
Proportion of Variance 0.6022 0.2673
Cumulative Proportion 0.6022 0.8695
      PC3
Standard deviation  0.6257
Proportion of Variance 0.1305
Cumulative Proportion 1.0000
> ##Step 4: Interpret Principal Components Extract and Interpret Loadings
> # Extract loadings
> loadings <- pca_result$rotation
>
> # Print loadings
> print(loadings)
      PC1      PC2      PC3
x1  0.6534351 -0.1023336 -0.7500336

```

```
x2 0.4870226 0.8153574 0.3130516
x3 -0.5795097 0.5698422 -0.5826219
> ##step5:Proportion of Variance
> # Proportion of variance explained
> prop_variance <- pca_result$sdev^2 / sum(pca_result$sdev^2)
>
> # Print proportion of variance
> print(prop_variance)
[1] 0.6021717 0.2673151 0.1305132
> ##step6: percentage
> per =((0.6021717+0.2673151)/sum(prop_variance))*100
> per
[1] 86.94868
```