

## Proximal Policy Optimization (PPO)

PPO is a policy gradient technique that balances stability and performance. To avoid significant policy changes that would cause training to become unstable, it employs a clipped surrogate aim. PPO is one of the most reliable contemporary reinforcement learning algorithms since it increases learning stability and efficiency.

### Algorithm 1: Proximal Policy Optimization

Input: Policy network  $\pi_\theta$ , value network  $V_\theta$ , environment env, number of epochs  $K$ , batch size  $B$

Output: Optimized policy  $\pi_\theta$

1. Initialize  $\theta$  randomly
2. for each iteration do
3.   Collect a set of trajectories  $D$  using  $\pi_\theta$  in env
4.   Compute advantages  $\hat{A}$  using generalized advantage estimation (GAE)
5.   for epoch = 1 to  $K$  do
6.     for each minibatch in  $D$  do
7.       Compute ratio  $r(\theta) = \pi_\theta(a|s) / \pi_{\theta\_old}(a|s)$
8.       Compute surrogate loss:
9.        $L(\theta) = E[\min(r(\theta) * \hat{A}, \text{clip}(r(\theta), 1 - \epsilon, 1 + \epsilon) * \hat{A})]$
10.      Perform gradient ascent on  $L(\theta)$
11.      Update value network by minimizing:
12.       $L_v = (V_\theta(s) - R)^2$
13.    end for
14.   end for
15. end for

### Proximal Policy Optimization (PPO) for Lunar Lander

## Advantage Actor-Critic (A2C)

A2C is a synchronous variant of Actor-Critic methods in which the critic assesses the value function while the actor learns the policy. It stabilizes training and lowers update variance by using the advantage function, which is the difference between expected and actual rewards.

### Algorithm 2: Advantage Actor - Critic

Input: Policy network  $\pi_\theta$ , value network  $V_\phi$ , environment env, learning rate  $\alpha$ , discount  $\gamma$

Output: Optimized policy  $\pi_\theta$

1. Initialize  $\theta$  and  $\phi$
2. for each episode do
3.   Initialize state  $s$
4.   for  $t = 1$  to  $T$  do
5.     Select action  $a \sim \pi_\theta(a|s)$
6.     Take action  $a$ , observe reward  $r$  and next state  $s'$
7.     Compute TD error:  $\delta = r + \gamma * V_\phi(s') - V_\phi(s)$
8.     Update  $\theta$  using policy gradient:
9.        $\theta \leftarrow \theta + \alpha * \delta * \nabla_\theta \log \pi_\theta(a|s)$
10.    Update value network:
11.        $\phi \leftarrow \phi - \alpha * \nabla_\phi (V_\phi(s) - (r + \gamma * V_\phi(s')))^2$
12.     $s \leftarrow s'$
13.   end for
14. end for

### Advantage Actor Critic for Lunar Lander

## Monte Carlo

Without bootstrapping, Monte Carlo algorithms learn from entire episodes. The average return from each state visit is used to estimate value functions, and these estimates are used to update rules. It functions well in settings with well-defined episodes.

### Algorithm 3: Monte Carlo

Input: Policy  $\pi$ , state-value table  $V$ , environment  $\text{env}$ , learning rate  $\alpha$ , discount  $\gamma$

Output: Improved policy  $\pi$

1. Initialize  $\pi$  arbitrarily and  $V(s) = 0$  for all  $s$
2. for each episode do
3.   Generate episode:  $S_0, A_0, R_1, \dots, S_T$  using  $\pi$
4.    $G \leftarrow 0$
5.   for  $t = T-1$  to  $0$  do
6.      $G \leftarrow \gamma * G + R_{t+1}$
7.     if  $(S_t, A_t)$  not in  $(S_0, A_0), \dots, (S_{t-1}, A_{t-1})$  then
8.        $V(S_t) \leftarrow V(S_t) + \alpha * (G - V(S_t))$
9.       Update policy  $\pi$  to be greedy w.r.t.  $V$
10.   end for
11. end for

### Monte Carlo for Lunar Lander

## Deep Q – Network

DQN is a value-based reinforcement learning technique that approximates the Q-value function using a deep neural network. To increase stability and learning effectiveness, it uses experience replay and a different target network.

### Algorithm 4: Deep Q-Network

**Input:** Q-network  $Q_\theta$ , target network  $Q_{\theta'}$ , replay buffer  $D$ , environment  $env$

**Hyperparameters:** learning rate  $\alpha$ , discount  $\gamma$ , batch size  $B$ , update frequency  $N$

**Output:** Trained Q-network  $Q_\theta$

1. Initialize  $Q_\theta$  with random weights and set  $Q_{\theta'} \leftarrow Q_\theta$
2. Initialize replay buffer  $D$
3. for each episode do
4.   Initialize state  $s$
5.   for  $t = 1$  to  $T$  do
6.     With probability  $\epsilon$  select random action  $a$
7.     else select  $a = \operatorname{argmax}_a Q_\theta(s, a)$
8.     Execute action  $a$ , observe  $r, s'$
9.     Store  $(s, a, r, s')$  in  $D$
10.    Sample random minibatch from  $D$
11.    For each  $(s, a, r, s')$  in batch:
12.      $y = r + \gamma * \max_{a'} Q_{\theta'}(s', a')$
13.     Update  $Q_\theta$  by minimizing:  $(y - Q_\theta(s, a))^2$
14.    Every  $N$  steps, update target network:  $Q_{\theta'} \leftarrow Q_\theta$
15.     $s \leftarrow s'$
16.   end for
17. end for

## Deep Q – Network for Lunar Lander