Assignment-5

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(1)

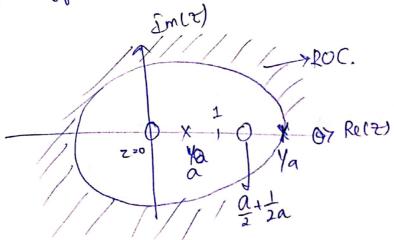
1:0)
$$x(u) = a^{n}u(n) + \overline{a}^{n}u(n)$$

 $x(z) = \frac{1}{1-\frac{a}{z}} + \frac{1}{1-\frac{1}{az}} = \frac{z(az-1) + az(z-a)}{(az-1)(z-a)}$
 $= \frac{2az^{2} - (a^{2}+1)z}{(az-1)(z-a)}$

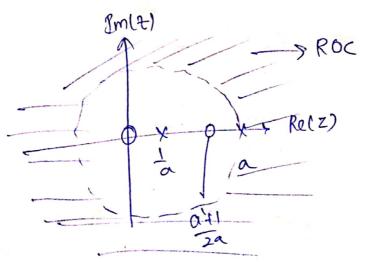
:. 36 | a|
$$\frac{1}{4}$$
 => ROC = | $\frac{1}{2}$ | $\frac{1}{1}$ | $\frac{1}{1}$ | ROC => $\frac{1}{2}$ | $\frac{1}{1}$ | \frac

Pole-tero plot

3



Care-1! If la171



$$\frac{(1\cdot1)}{Sol} \times (N) = (-1)^{N} \sum_{i=1}^{N} u(i)$$

$$\frac{1}{2} \times (u) = (-1)^{N} \sum_{i=1}^{N} u(i)$$

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$$\frac{1}{1+\frac{1}{2}} = \frac{2x}{1+2x}$$

$$\frac{1}{2} \times (1+2x) = \frac{2x}{1+2x}$$

$$\frac{1}{2} \times (1+2x)$$

$$\frac{1}{2} \times (1+2x)$$

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$$\frac{1}{$$

(1.2)
$$x(n) = Ar''\cos(\omega_{0}n+\phi)$$
; $ocrci$
 $= \frac{Ar''}{2}(e^{j(\omega_{0}n+\phi)} + e^{j(\omega_{0}n+\phi)})$
 $= \frac{Ae^{j\phi}(re^{j(\omega_{0}n+\phi)})}{2} + \frac{Ae^{j\phi}(re^{j(\omega_{0}n+\phi)})}{2}$

Using Result (1): Heaves

 $= \frac{Ae^{j\phi}(re^{j(\omega_{0}n+\phi)})}{2} + \frac{Ae^{j\phi}(re^{j(\omega_{0}n+\phi)})}{2}$

For $x(z) = \frac{Ae^{j\phi}(re^{j(\omega_{0}n+\phi)})}{2} + \frac{Ae^{j\phi}(re^{j(\omega_{0}n+\phi)})}{2} + \frac{Ae^{j\phi}(re^{j(\omega_{0}n+\phi)})}{2}$

For $y(z)$ to be finite: $(re^{j(\omega_{0}n+\phi)}) < 1 + \frac{Ae^{j\phi}(re^{j(\omega_{0}n+\phi)})}{2} < 1$

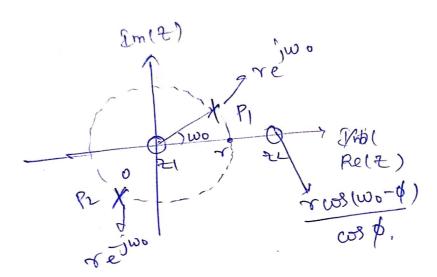
$$|\nabla z| = \frac{1}{2} \left(\frac{1}{2} |x|^2 \right) \left(\frac{1}{2} |x|^2 \right) = \frac{1}{2} |x|^2$$

$$|\nabla z|^2 + \frac{1}{2} |x|^2 \left(\frac{1}{2} |x|^2 \right) = \frac{1}{2} |x|^2$$

$$|\nabla z|^2 + \frac{1}{2} |x|^2 \left(\frac{1}{2} |x|^2 \right) + \frac{1}{2} |x|^2 \left(\frac{1}{2} |x|^2 |x|^2 \right)$$

$$|\nabla z|^2 + \frac{1}{2} |x|^2 +$$

(1.2)



$$(\frac{1.3}{501})$$
 $y(14) = \sqrt{(\frac{1}{3})^{4}} = 2^{4}$; $n \ge 0 = (\frac{1}{3})^{4} = 2^{4}$) $u(n)$.

$$\chi(u) = (\frac{1}{3})^n u(u) - 2^n u(u)$$

$$\frac{1}{\chi(z)} = \frac{1}{1 - \frac{1}{3z}} - \frac{1}{1 - \frac{2}{z}} = \frac{3z}{3z - 1} - \frac{z}{z - 2}$$

$$= 3z(z-2)-z(3z-1) - 5z$$

$$(3z-1)(z-2) - 3z^2-7z+2$$

$$\frac{(32)^{2}}{32^{2}-72+2} = \frac{(32)(2)(2)(2)}{(2)(2)(2)(2)}$$

Pole-zero plot)

(1.4) [convolution;
$$x(n) = x_1(m * x_2(n))$$

80] $x(n) \leftarrow x(2)$
 $x(2) = \frac{x_2}{2} x_1(n) + \frac{x_2}{2} = \frac{x_2}{2} (\frac{x_2}{2} x_2(n-k)) + \frac{x_2}{2} = \frac{x_2}{2} =$

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$$(z) = X_{1}(z) \cdot X_{2}(z)$$

$$= \left(\frac{1}{1-\frac{1}{2}}\right) \left(\frac{1}{1+\frac{1}{2}}\right) \Rightarrow Y(z) = \frac{9z^{2}}{(9z-1)(z+1)}$$

$$= \frac{1}{1-\frac{1}{2}} \left(\frac{1}{1+\frac{1}{2}}\right) \Rightarrow Y(z) = \frac{1}{1+\frac{1}{2}} \Rightarrow Y(z) = \frac{1}{1+\frac$$

(1.5)
$$Y(z) = \frac{z^{b} + z^{7}}{1 - z^{-1}}$$

Proof:
$$\chi(z) = \frac{\pi}{2} \chi(n) + \chi(z)$$
 $\chi(z) = \frac{\pi}{2} \chi(n) = \frac{\pi}{$

Vising Result-1:
$$X(z) = \frac{z^6}{1 - \frac{1}{2}} + \frac{z^7}{1 - \frac{1}{2}}$$

we know that (4) u(n) (-) 1-1. isince it's causal.

1.6)
$$\chi(z) = \frac{1}{4} \left(\frac{1+6z^{1}+z^{2}}{(-2z^{1}+2z^{2})(1-\frac{1}{2}z^{1})} \right)$$

Sol.

Dividing them into paritial fractions.

$$A(1/2)$$
) $\chi(2) = \frac{A}{1-\frac{2}{2}} + \frac{B+(2^{-1}+2)}{1-22^{-1}+22^{-2}}$

$$\chi(z) = \frac{17/20}{1 - 0.5z^{-1}} - \frac{3/5(1 - .2^{-1})}{1 - 2z^{-1} + 2z^{-2}} + \frac{23/10z^{-1}}{1 - 2z^{-1} + 2z^{-2}}$$

$$a^{\prime\prime}$$
 cos(woN) cum) $\longleftrightarrow \frac{1-2a^{\frac{1}{2}}\cos(wo)+a^{\frac{1}{2}}e^{-2}}{1-4a^{\frac{1}{2}}\cos(wo)+a^{\frac{1}{2}}e^{-2}}$

$$2a^{4}\omega_{1}(\omega_{0})$$
 (ω_{0}) $(\omega_$

$$\frac{1-az'(\omega)(\omega_0)}{1+a^{\frac{1}{2}}-2az'(\omega)(\omega_0)}$$

$$a^{\text{M}}\sin(\omega \circ u)u(u) \leftarrow \frac{1}{2!}\left(\frac{z}{z-ae^{j\omega \circ u}}\right) = \frac{2}{z^{2}+a^{2}-2az(\omega \circ u)}$$

(a)
$$\chi(z) = \frac{17/20}{1 - 0.527} + \frac{3/5}{1 - 24^{\frac{1}{2}} + 22^{\frac{1}{2}}} + \frac{33}{10} \left(\frac{z^{\frac{1}{2}}}{z^{\frac{1}{2}}}\right)$$

Using Result - 3: $|w_0| = \frac{1}{10} = \frac{1}{1$

1.4)
$$\chi(z) = 5z^{-1}$$
 $(1-2z^{-1})(3-z^{-1})$
 $=> A(3-z^{-1})+B(1-2z^{-1})=5z^{-1}=> 3A+B=0=> 6A+2B=0$
 $A+2B=0=> A+2B=0=> A+2B=0=0=> A+2B=0=0=> A+2B=0=0=> A+2B=0=0=> A+2B=0=0=> A+2B=0=0=> A+2B=0=0=> A+2B=0=$

(9)
$$\frac{1}{\sqrt{3}} \frac{1}{\sqrt{1}} \frac{1}{\sqrt{2}} \frac{1}$$

1.8)
$$Y(z) = \frac{1-2z^{-1}+2z^{-2}-z^{-3}}{(1-z^{-1})(1-0.5z^{-1})(1-0.2z^{-1})} = \frac{A/}{1-0.5z^{-1}} + \frac{B/}{1-0.5z^{-1}} + \frac{B/}{1-0.5$$

$$\chi(z) = 10 + \frac{5}{1 - 0.52^{-1}} - \frac{14}{1 - 0.22^{-1}}$$
 $\chi(u) = 108(n) + 5(\frac{1}{2})u(n) - \frac{14}{5}u(n)$
 $= : (2172)$ Satisfies both

1.9)
$$\chi(z) = \frac{3}{1 - 10z^{1} + z^{2}} = \frac{918}{z^{1} - 3} - \frac{918}{z^{1} - 1/3}$$

$$= \frac{918}{3} \left(\frac{1}{1 + z^{1}} \right) + \frac{3}{1 - 3z^{-1}} \right)$$

$$= \frac{31}{8} \left(\frac{1}{1 - 3z^{1}} \right) - \left(\frac{3}{8} \right) \left(\frac{1}{1 - z^{-1}} \right)$$
Here There can be 3 ROC's

1.1 12173 , (ii) 121<3 U 121&1/3 (iii) 121&1/3

There can be 3 ROC's

1.2 Civen ROC is 121=1

There can be 3 ROC's

1.3 (iii) 121&1/3

There can be 3 ROC's

1.4 (iven ROC is 121=1)

There can be 3 ROC's

1.5 (iven ROC is 121=1)

There can be 3 ROC's

1.6 (iven ROC is 121=1)

There can be 3 ROC's

1.7 (iven ROC is 121=1)

There can be 3 ROC's

From Result -3: we know that $\frac{1}{1-dz^{1}} \longleftrightarrow -d^{n}u(-n-1) ; \text{ for } (z|c|d)$ $\frac{1}{1-dz^{1}} \longleftrightarrow -d^{n}u(-n-1) ; \text{ for } (z|c|d)$

Solu) * "For a Sinusoid signal, location of zeros affects only their phase?"

Forom the Result (3) proved: before: in prob: (1.2).

(oslwont \$\phi\$) 2-> zws\$ - 10 zws (wo-\$)

\[\frac{1}{x^2+1-2zws}(wo)
\]

Consider the zeros', here; $z^2\cos\phi - 2\cos(\omega\phi - \phi) = 0$ $\Rightarrow Z = 0, \left[\frac{1}{2} \cos(\omega\phi - \phi) \right]$

-Tor sin(won+φ) (> σχείη(ωο-φ) + z²είηφ
-2+1-27 cos(ωο)

Zeros; zzo, zz - sin(word)

+ Since both the denominator's of sinusoid's signal, z-transform does not have \$ term,

-) 'b' is present Buly in numerator, thus present in zeros of z-transform: while no affect on poles.

-> Thus, the statement is true

: By changing phase changes only roots not poles

2.2) ° A LII system is BIBO, Stable Iff, system function 801. includes unit virele" - The know that the system is stable iff I hande os, college han is impulse tresponse. H(2) = 5 h(n) 2 < 5 [h(n) | 2-n] : 14(21) < 2 1h(n) 12-n) It the ROC Include unit visule 171=1 (H(Z)) & I (h(n)) -> Thus, know that IHLEI < 00; Since, for System lies in ROC. .. 2 h(n) <00 > Stable System => Eq; $h(n) = \frac{1}{3} n u(n)$ => $\frac{2}{1} |h(n)| = \frac{2}{1-\frac{1}{2}} = \frac{2}{1-\frac{1}{2$ => : Bounded valued output => BIBO stable => g h(n)=(2)^nu(n) => Zh(n) = Z(3) = oo. => Not stable W(n) = (2) hin= (=) n H(t) = 1-2 2<1 =) [Z72] (2) <1 Since 1 1712 does not contain 27-1 121=1) => we can say that : Since 121=1 is included it's it's not stable

Stable

1

8 30)

31)

y(n) = 0.5 y(n-1) + x(n)

>((h) = 10 cos(
$$\frac{x_0}{y_0}$$
) u(n)

2-haughom: $y(z) = 0.5 t^{-1} y(z) + y(t)$

As proved earlier in prob.1.2; knut. 1.3:

(es(won) u(n) \longleftrightarrow $\frac{1}{2t^2} \frac{1}{2t^2} \frac{1}{2$

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$$|V(z)| = -1.86 + 6.78 - 29.01 + 6.78 - 29.09 - 20.09$$

. We got a sinusoid ise and and exponential term in olp.

transient: Which ever gets to zero as $t n + \infty$ $\frac{1}{3} + \frac{1.86(\frac{1}{2})^n}$

Steady state? - Which lasts at
$$4 n - 100$$

$$y_s(n) = 13.56 \cos(\frac{\pi n - 29.09}{4}) u(n)$$

3) (32)
$$y(n)$$
, as $y(n-1) - y(n-2) + x(n) - 5x(n-1) + 6x(n-2)$

Sol.

Converting into x - transform.

$$y(x) = 2 \cdot 5 \cdot \frac{1}{2} \cdot y(z) - 8 \cdot \frac{1}{2} \cdot y(z) + x(z) - (\frac{1}{2} \cdot x(z)) + (6\frac{1}{2} \cdot x(z))$$

$$y(x) = 2 \cdot 5 \cdot \frac{1}{2} \cdot y(z) - 8 \cdot \frac{1}{2} \cdot y(z) + x(z) - (\frac{1}{2} \cdot x(z)) + (6\frac{1}{2} \cdot x(z))$$

$$y(x) = 2 \cdot 5 \cdot \frac{1}{2} \cdot y(z) - 8 \cdot \frac{1}{2} \cdot y(z) + x(z) - (\frac{1}{2} \cdot x(z)) + (6\frac{1}{2} \cdot x(z)) + ($$