

# Merge Sort Algorithm

**Divide the unsorted list into two roughly equal halves.**

Recursively sort each half:

- If the half contains more than one element, repeat the divide and sort steps.

Merge the sorted halves back together:

- Compare the elements from both halves one by one and arrange them in a sorted order.
- Continue this until both halves are completely merged into one sorted array.

**Repeat the process until the entire list is sorted.**

```
MergeSort(arr)
    if length of arr <= 1
        return
    mid = length of arr / 2
    left = arr[0 to mid-1]
    right = arr[mid to end]
    MergeSort(left)
    MergeSort(right)
    Merge(arr, left, right)

Merge(arr, left, right)
    i = 0, j = 0, k = 0
    while i < length of left and j < length of right
        if left[i] < right[j]
            arr[k] = left[i]
            i = i + 1
        else
            arr[k] = right[j]
            j = j + 1
        k = k + 1
    while i < length of left
        arr[k] = left[i]
        i = i + 1
        k = k + 1
    while j < length of right
        arr[k] = right[j]
        j = j + 1
        k = k + 1
```

# Quick Sort Algorithm

**Pick a Pivot:** Choose an element from the array as the pivot (usually the last element or a random one).

**Partition the Array:**

- Rearrange the elements such that elements smaller than the pivot are on its left.
- Elements greater than the pivot are on its right.
- Place the pivot in its correct sorted position in the array.

**Recursively Sort the Subarrays:**

- Apply Quick Sort to the subarray of elements on the left of the pivot.
- Apply Quick Sort to the subarray of elements on the right of the pivot.

**Repeat** the process until each subarray has one or no elements, at which point the entire array is sorted.

```
QuickSort(arr, low, high)
    if low < high
        pivotIndex = Partition(arr, low, high)
        QuickSort(arr, low, pivotIndex - 1)
        QuickSort(arr, pivotIndex + 1, high)
```

```
Partition(arr, low, high)
    pivot = arr[high]
    i = low - 1
    for j = low to high - 1
        if arr[j] < pivot
            i = i + 1
            swap(arr[i], arr[j])
    swap(arr[i + 1], arr[high])
    return i + 1
```

```
swap(arr, i, j)
    temp = arr[i]
    arr[i] = arr[j]
    arr[j] = temp
```

## Merge Sort Time Complexity

- Best Case:  $O(n \log n)$
- Average Case:  $O(n \log n)$
- Worst Case:  $O(n \log n)$
- Space Complexity:  $O(n)$

## Quick Sort Time Complexity

- Best Case:  $O(n \log n)$
- Average Case:  $O(n \log n)$
- Worst Case:  $O(n^2)$
- Space Complexity:  $O(\log n)$  (for the recursive call stack)