

Assignment 4

Suryaansh Jain

May 20, 2022

Outline

- 1 Problem Statement
- 2 Definitions
- 3 Solution
- 4 Graphs

Problem Statement

13.5 Q12 [NCERT 12]

Find the probability of throwing at most 2 sixes in 6 throws of a single die.

Random Variable Definition

In this experiment, there are six consecutive Bernoulli trials. Let us define a Binomial Random Variable $X = \{0, 1, 2, 3, 4, 5, 6\}$ where the value of X is the number of sixes obtained

Probability Mass Function

The probability of success (assuming a fair die) is $p = \frac{1}{6}$.
Therefore, the probability that X maps to i is given by:

$$\Pr(X = i) = \binom{6}{i} (1 - p)^{6-i} p^i, \quad 0 \leq i \leq 6 \quad (1)$$

The values for i can be substituted in the above formula, and the graph of the PMF can be obtained.

Cumulative Distribution Function

The cumulative probability $\Pr(X \leq i)$ can be defined as under:

$$\Pr(X \leq i) = \sum_{k=0}^i \binom{6}{k} (1-p)^{6-k} p^k, \quad 0 \leq i \leq 6 \quad (2)$$

The values of i can be substituted in the above equation, and the obtained values can be used to plot the CDF graph.

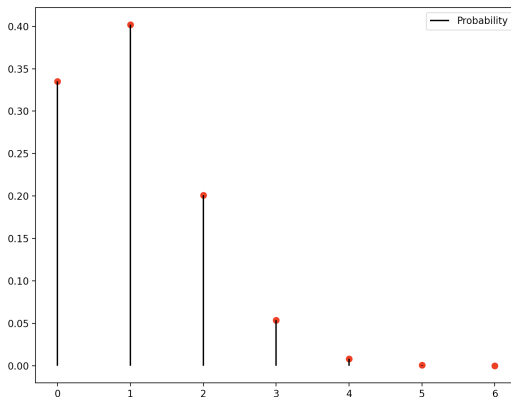
Solution

The probability to be found corresponds to the case $\Pr(X \leq 2)$.
Substituting i in Equation 1 and summing, we get

$$\Pr(X = 2) + \Pr(X = 1) + \Pr(X = 0) = \frac{5^4}{3^3 \times 2^6} \approx 0.36 \quad (3)$$

PMF Graph

The PMF graph is:



CDF Graph

The CDF graph is:

