

## Practice Questions – Functions

Q.1 Show that  $f: R - \{1\} \rightarrow R - \{2\}$  such that  $f(x) = \frac{2x-3}{x-1}$  is bijective and hence find  $f^{-1}$ .

Q.2 Show that  $f: R - \{3\} \rightarrow R - \{0\}$  such that  $f(x) = \frac{1}{x-3}$  is bijective and hence find  $f^{-1}$ .

Q.3 Show that  $f: R - \{5\} \rightarrow R - \{0\}$  such that  $f(x) = \frac{1}{x-5}$  is bijective and hence find  $f^{-1}$ .

Q.4 Check whether the function  $f: Z \rightarrow Z$  defined as  $f(x) = x^2 + x + 1$  is bijective .

Q.5 If the functions  $f$  and  $g$  are defined as  $f: R \rightarrow R, f(x) = 2 + 3x$  and  $g: R \rightarrow R, g(x) = 4 - 3x$ . Find  $f \circ g(x)$  and  $g \circ f(x)$

Q.6 If the functions  $f$  and  $g$  are defined as  $f: R \rightarrow R, f(x) = 2x + 3$  and  $g: R \rightarrow R, g(x) = 3x + 4$ . Find  $f^{-1} \circ g^{-1}(x)$  and  $g^{-1} \circ f^{-1}(x)$

Q.7 If the functions  $f$  and  $g$  are defined as  $f: R \rightarrow R, f(x) = 2x - 3$  and  $g: R \rightarrow R, g(x) = 4 - 3x$ . Solve  $g^{-1} \circ f^{-1}(x) = 2$

Q.8 Functions  $f: R \rightarrow R, g: R \rightarrow R$  are defined as  $f(x) = 5x + 3$  and  $g(x) = 1 + 3x$  then find  $f \circ g, f \circ f, g \circ f$  &  $g \circ g \circ f$

Q.9 Functions  $f: R \rightarrow R, g: R \rightarrow R$  are defined as  $f(x) = 2x - 3, g(x) = 3x + 2$  Then show that  $f(x), g(x)$  are bijective and hence find  $f^{-1}(x), g^{-1}(x), g \circ f^{-1}$  and  $g^{-1} \circ f$

Q.10 Functions  $f: R \rightarrow R, g: R \rightarrow R$  are defined as  $f(x) = x - 4, g(x) = 6 - 7x$  Then show that  $f(x), g(x)$  are bijective and hence find  $f^{-1}(x), g^{-1}(x), g \circ f^{-1}$  and  $g^{-1} \circ f$

Q.11 Functions  $f: R \rightarrow R, g: R \rightarrow R$  are defined as  $f(x) = 2x, g(x) = x - 2$  Then show that  $f(x), g(x)$  are bijective and hence find  $f^{-1}(x), g^{-1}(x), g \circ f^{-1}$  and  $g^{-1} \circ f$

Q.12 Functions  $f: R \rightarrow R, g: N \rightarrow N$  are defined as  $f(x) = x^2, g(x) = x^2$  . check whether  $f, g$  are injective