

2)

a) The decision variable should represent the number of units shipped from well to each transshipment point(pump) to each destination (refinery points), The decision variable shipped from location i to j

Where i = 1,2,3,4

j=4,5,6,7,8,9,10,11,12

	R1	R2	R3	R4	R5	Dummy
Pump A	5.15	5.69	6.13	5.63	5.80	0
Pump A	5.12	5.12	5.47	6.05	6.12	0
Pump A	5.32	6.16	6.25	6.17	5.87	0
Demand	30	57	48	91	48	2

Minimize total cost:

$$1.52x_{14} + 1.60x_{15} + 1.40x_{16} + 1.70x_{24} + 1.63x_{25} + 1.55x_{26} + 1.45x_{34} + 1.57x_{35} + 1.30x_{36} + 5.15x_{47} + 5.69x_{48} + 6.13x_{49} + 5.63x_{4,10} + 5.80x_{4,11} + x_{4,12} + 5.12x_{57} + 5.47x_{58} + 6.05x_{59} + 6.12x_{5,10} + 5.71x_{5,11} + x_{5,12} + 5.32x_{67} + 6.16x_{68} + 6.25x_{69} + 6.17x_{6,10} + 5.87x_{6,11} + x_{6,12}$$

s.t.

$$x_{14} + x_{15} + x_{16} \leq 93 \text{ Supply at Well 1 [node 1]}$$

$$x_{24} + x_{25} + x_{26} \leq 88 \text{ Supply at Well 2 [node 2]}$$

$$x_{34} + x_{35} + x_{36} \leq 95 \text{ Supply at Well 3 [node 3]}$$

$$x_{47} + x_{57} + x_{67} = 30 \text{ (Demand at Refinery 1 [node 7])}$$

$$x_{48} + x_{58} + x_{68} = 57 \text{ (Demand at Refinery 2 [node 8])}$$

$$x_{49} + x_{59} + x_{69} = 48 \text{ (Demand at Refinery 3 [node 9])}$$

$$x_{4,10} + x_{5,10} + x_{6,10} = 91 \text{ (Demand at Refinery 4 [node 10])}$$

$$x_{4,11} + x_{5,11} + x_{6,11} = 48 \text{ (Demand at Refinery 5 [node 11])}$$

$$x_{4,12} + x_{5,12} + x_{6,12} = 2 \text{ (Dummy Variable [node 12])}$$

$$x_{14} + x_{24} + x_{34} = x_{47} + x_{49} + x_{4,10} + x_{4,11} + x_{4,12} \text{ ((Shipping through Pump 1 [node 4])}$$

$$x_{15} + x_{25} + x_{35} = x_{57} + x_{58} + x_{59} + x_{5,10} + x_{5,11} + x_{5,12} \text{ (Shipping through Pump 2 [node 5])}$$

$$x_{16} + x_{26} + x_{36} = x_{67} + x_{68} + x_{69} + x_{6,10} + x_{6,11} + x_{6,12} \text{ (Shipping through Pump 3 [node 6])}$$

$$x_{ij} \geq 0 \text{ for all } i \text{ and } j \text{ (Non negativity constraint)}$$

b) The network diagram for this problem: -
Where W = well, P = pump and R = refinery

