

# Graph Interview Prepration

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## 1. Find the Shortest Path Between Two Nodes in a Graph

### Problem Statement

Given a graph represented as an adjacency list or adjacency matrix, find the shortest path between two nodes. The graph may be **unweighted** (use BFS) or **weighted** (use Dijkstra's algorithm).

### Algorithm (Dijkstra's Algorithm for Weighted Graph)

1. **Initialize a Min-Heap (Priority Queue):** Store (distance, node) pairs.
2. **Set Distances:** Create an array dist to store the shortest distance from the source to every node, initialized as Infinity, except dist[source] = 0.
3. **Process Nodes:**
  - Extract the node with the smallest distance from the priority queue.
  - Update the distances of its neighbors if a shorter path is found.
  - Push the updated (distance, neighbor) back into the queue.
4. **Continue Until All Nodes Are Processed.**
5. **Return the Shortest Distance to the Target Node.**

### Why This Algorithm?

We use **Dijkstra's Algorithm** because we are dealing with a **graph with weighted edges** and need the shortest path. BFS works only for unweighted graphs, but Dijkstra efficiently finds the shortest path in  $O((V + E) \log V)$  time using a priority queue. If negative weights exist, we use **Bellman-Ford Algorithm** instead.

### Time & Space Complexity

- **Time Complexity:**  $O((V + E) \log V)$ , where  $V$  = number of vertices and  $E$  = number of edges.
- **Space Complexity:**  $O(V)$  for distance array and  $O(E)$  for the adjacency list.

### Java Code

```
import java.util.*;
```

```
class ShortestPathGraph {
```

```
    static class Node {
```

```

int vertex, weight;

Node(int v, int w) { vertex = v; weight = w; }

}

```

```

public static int dijkstraShortestPath(int V, List<List<Node>> adj, int source, int target) {

    PriorityQueue<Node> pq = new PriorityQueue<>(Comparator.comparingInt(n ->
n.weight));

    int[] dist = new int[V];
    Arrays.fill(dist, Integer.MAX_VALUE);
    dist[source] = 0;
    pq.add(new Node(source, 0));

    while (!pq.isEmpty()) {
        Node curr = pq.poll();
        int u = curr.vertex;
        if (u == target) return dist[u];

        for (Node neighbor : adj.get(u)) {
            int v = neighbor.vertex, weight = neighbor.weight;
            if (dist[u] + weight < dist[v]) {
                dist[v] = dist[u] + weight;
                pq.add(new Node(v, dist[v]));
            }
        }
    }

    return -1; // Return -1 if no path exists
}

```

```

public static void main(String[] args) {

    int V = 5;

```

```

List<List<Node>> adj = new ArrayList<>();

for (int i = 0; i < V; i++) adj.add(new ArrayList<>());

adj.get(0).add(new Node(1, 2));
adj.get(0).add(new Node(3, 6));
adj.get(1).add(new Node(2, 3));
adj.get(3).add(new Node(2, 1));

int shortestPath = dijkstraShortestPath(V, adj, 0, 2);

System.out.println("Shortest Path: " + shortestPath);
}
}

```

**Leetcode Link:**

- [Dijkstra's Algorithm](#) (Similar Problem)

## 2. Determine Whether a Graph is Bipartite

### Problem Statement

A graph is **bipartite** if we can split its vertices into two independent sets such that no two adjacent nodes belong to the same set. Given a graph represented as an adjacency list, determine whether it is bipartite.

### Algorithm (BFS-Based Two-Coloring Approach)

1. **Initialize a Color Array:** Assign -1 to all nodes (uncolored).
2. **Use BFS to Color the Graph:**
  - Start from any uncolored node and color it 0.
  - For each neighbor, assign the opposite color (1 for 0 and vice versa).
  - If a conflict arises (a neighbor has the same color), return false.
3. **Repeat for all Components:** If the graph is disconnected, check each component.
4. **Return true if No Conflicts Found.**

**Why This Algorithm?**

We use **BFS two-coloring** because it efficiently checks whether a graph is bipartite in  **$O(V + E)$  time**. If any cycle of **odd length** exists, the graph is **not bipartite**. We can also use **DFS**, but BFS is preferred for shorter paths.

### Time & Space Complexity

- **Time Complexity:**  $O(V + E)$ , where  $V$  = number of vertices,  $E$  = number of edges.
- **Space Complexity:**  $O(V)$  for the color array and queue.

### Java Code

```
import java.util.*;

class BipartiteGraph {

    public static boolean isBipartite(int[][] graph) {

        int V = graph.length;

        int[] color = new int[V];

        Arrays.fill(color, -1); // Uncolored

        for (int i = 0; i < V; i++) {

            if (color[i] == -1) { // Check unvisited components

                Queue<Integer> queue = new LinkedList<>();

                queue.add(i);

                color[i] = 0;

                while (!queue.isEmpty()) {

                    int node = queue.poll();

                    for (int neighbor : graph[node]) {

                        if (color[neighbor] == -1) {

                            color[neighbor] = 1 - color[node];

                            queue.add(neighbor);

                        } else if (color[neighbor] == color[node]) {

                            return false; // Conflict found

                        }

                    }

                }

            }

        }

        return true;
    }
}
```

```

        }
    }
}
return true;
}

public static void main(String[] args) {
    int[][] graph = {
        {1, 3}, {0, 2}, {1, 3}, {0, 2}
    };
    System.out.println("Is Bipartite: " + isBipartite(graph));
}
}

```

**Leetcode Link:**

- [Is Graph Bipartite?](#)

### 3. Detect a Cycle in a Directed Graph

#### Problem Statement

Given a directed graph, determine whether it contains a cycle. A cycle exists if we can start from a node and reach the same node through a sequence of edges.

#### Algorithm (DFS-Based Cycle Detection)

1. **Use a Visited Array:** Track the state of each node:
  - 0 → Unvisited
  - 1 → Visiting (part of current recursion stack)
  - 2 → Visited (fully explored)
2. **Perform DFS:**
  - Mark a node as 1 when visiting.
  - If a neighbor is also 1, a **cycle exists**.

- After exploring all neighbors, mark the node as 2.

3. **Repeat for All Nodes:** If DFS completes without detecting a cycle, return false.

### Why This Algorithm?

DFS with recursion stack efficiently detects cycles in directed graphs in  **$O(V + E)$  time**. An alternative is **Kahn's Algorithm (Topological Sort)**, but it requires an in-degree array.

### Time & Space Complexity

- **Time Complexity:**  $O(V + E)$  (DFS traversal).
- **Space Complexity:**  $O(V)$  (recursion stack).

### Java Code

```
import java.util.*;
```

```
class DetectCycleDirected {  
    public static boolean hasCycle(int V, List<List<Integer>> adj) {  
        int[] state = new int[V];  
  
        for (int i = 0; i < V; i++) {  
            if (state[i] == 0 && dfs(i, adj, state)) {  
                return true;  
            }  
        }  
        return false;  
    }  
}
```

```
private static boolean dfs(int node, List<List<Integer>> adj, int[] state) {  
    state[node] = 1; // Mark as visiting  
    for (int neighbor : adj.get(node)) {  
        if (state[neighbor] == 1 || (state[neighbor] == 0 && dfs(neighbor, adj, state))) {  
            return true;  
        }  
    }  
}
```

```

        state[node] = 2; // Mark as visited
        return false;
    }

    public static void main(String[] args) {
        int V = 4;
        List<List<Integer>> adj = new ArrayList<>();
        for (int i = 0; i < V; i++) adj.add(new ArrayList<>());
        adj.get(0).add(1);
        adj.get(1).add(2);
        adj.get(2).add(3);
        adj.get(3).add(1); // Cycle

        System.out.println("Has Cycle: " + hasCycle(V, adj));
    }
}

```

**Leetcode Link:**

- [Detect Cycle in Directed Graph](#)

## 4. Count the Number of Connected Components in an Undirected Graph

### Problem Statement

Given an undirected graph, find the number of **connected components** (sets of nodes that are directly or indirectly connected).

### Algorithm (DFS Traversal)

1. **Use a Visited Array:** Track nodes that have been visited.
2. **Perform DFS/BFS for Each Component:**
  - If a node is unvisited, increase the count and perform DFS to mark all reachable nodes.
3. **Return the Count of Components.**

### Why This Algorithm?

DFS efficiently finds connected components in  **$O(V + E)$**  time. We could also use **BFS or Union-Find**, but DFS is simpler for adjacency lists.

### Time & Space Complexity

- **Time Complexity:**  $O(V + E)$  (DFS traversal).
- **Space Complexity:**  $O(V)$  (visited array).

### Java Code

```
import java.util.*;
```

```
class ConnectedComponents {  
    public static int countComponents(int V, List<List<Integer>> adj) {  
        boolean[] visited = new boolean[V];  
        int count = 0;  
  
        for (int i = 0; i < V; i++) {  
            if (!visited[i]) {  
                dfs(i, adj, visited);  
                count++;  
            }  
        }  
        return count;  
    }  
  
    private static void dfs(int node, List<List<Integer>> adj, boolean[] visited) {  
        visited[node] = true;  
        for (int neighbor : adj.get(node)) {  
            if (!visited[neighbor]) {  
                dfs(neighbor, adj, visited);  
            }  
        }  
    }  
}
```



```

public static void main(String[] args) {

    int V = 5;

    List<List<Integer>> adj = new ArrayList<>();

    for (int i = 0; i < V; i++) adj.add(new ArrayList<>());

    adj.get(0).add(1);
    adj.get(1).add(0);
    adj.get(2).add(3);
    adj.get(3).add(2);
    adj.get(4).add(4); // Isolated node

    System.out.println("Number of Components: " + countComponents(V, adj));

}
}

```

**Leetcode Link:**

- [Number of Connected Components](#)

## 5. Find the Minimum Spanning Tree of a Graph

### Problem Statement

Given a weighted, connected, and undirected graph, find its Minimum Spanning Tree (MST). A Minimum Spanning Tree is a subset of edges that connects all vertices with the minimum possible total edge weight and no cycles.

### Algorithm (Kruskal's Algorithm)

1. **Sort** all edges of the graph in increasing order based on their weights.
2. **Initialize** an empty MST and use a Disjoint Set Union (DSU) to manage connected components.
3. **Iterate** through the sorted edges:
  - If adding the edge does not create a cycle, include it in the MST.
  - Use the **Union-Find** data structure to keep track of connected components.

4. Stop when we have exactly  $V-1$  edges in the MST (where  $V$  is the number of vertices).

### Why This Algorithm?

We use **Kruskal's Algorithm** because:

- It **greedily selects** the smallest edge, ensuring a globally optimal solution.
- It efficiently detects cycles using **Disjoint Set Union (DSU)**.
- Kruskal's works best for **sparse graphs** ( $E=O(V)$ ), unlike Prim's Algorithm, which is better for dense graphs.
- If we need an alternative, **Prim's Algorithm** would work, but it processes vertices one by one, making it slower for graphs with fewer edges.

### Time & Space Complexity

- **Sorting Edges**  $\rightarrow O(E \log E)$
- **DSU Operations**  $\rightarrow O(E \alpha(V))$  (almost constant time using path compression)
- **Overall Complexity**  $\rightarrow O(E \log E)$
- **Space Complexity**  $\rightarrow O(V + E)$  (for storing edges and DSU)

### Java Code (Using Kruskal's Algorithm)

```
import java.util.*;
```

```
class Edge implements Comparable<Edge> {
```

```
    int src, dest, weight;
```

```
    public Edge(int src, int dest, int weight) {
```

```
        this.src = src;
```

```
        this.dest = dest;
```

```
        this.weight = weight;
```

```
    }
```

```
    public int compareTo(Edge compareEdge) {
```

```
        return this.weight - compareEdge.weight;
```

```
    }
```

```
}
```

```
class DisjointSet {
```

```
    int[] parent, rank;
```

```
    public DisjointSet(int n) {
```

```
        parent = new int[n];
```

```
        rank = new int[n];
```

```
        for (int i = 0; i < n; i++) parent[i] = i;
```

```
    }
```

```
    public int find(int x) {
```

```
        if (parent[x] != x) parent[x] = find(parent[x]); // Path compression
```

```
        return parent[x];
```

```
    }
```

```
    public void union(int x, int y) {
```

```
        int rootX = find(x), rootY = find(y);
```

```
        if (rootX != rootY) {
```

```
            if (rank[rootX] > rank[rootY]) parent[rootY] = rootX;
```

```
            else if (rank[rootX] < rank[rootY]) parent[rootX] = rootY;
```

```
            else {
```

```
                parent[rootY] = rootX;
```

```
                rank[rootX]++;
```

```
            }
```

```
        }
```

```
    }
```

```
}
```

```

public class KruskalMST {

    public static List<Edge> kruskalMST(int V, List<Edge> edges) {

        Collections.sort(edges); // Sort edges by weight

        DisjointSet ds = new DisjointSet(V);

        List<Edge> mst = new ArrayList<>();

        for (Edge edge : edges) {

            if (ds.find(edge.src) != ds.find(edge.dest)) { // No cycle

                mst.add(edge);

                ds.union(edge.src, edge.dest);

            }

            if (mst.size() == V - 1) break; // Stop when MST is complete

        }

        return mst;

    }

    public static void main(String[] args) {

        int V = 4;

        List<Edge> edges = Arrays.asList(

            new Edge(0, 1, 10), new Edge(0, 2, 6), new Edge(0, 3, 5),

            new Edge(1, 3, 15), new Edge(2, 3, 4)

        );

        List<Edge> mst = kruskalMST(V, edges);

        System.out.println("Edges in MST:");

        for (Edge edge : mst) {

            System.out.println(edge.src + " - " + edge.dest + " (" + edge.weight + ")");

        }

    }

}

```

}

#### Leetcode Link

- No direct problem for Kruskal's MST, but a similar one:  
[Connecting Cities With Minimum Cost](#)
  - Prim's Algorithm alternative:  
[Minimum Cost to Connect All Points](#)
- 

## 6. Topological Sorting of a Directed Acyclic Graph (DAG)

### Problem Statement

Given a Directed Acyclic Graph (DAG), find a valid **topological ordering** of its vertices, meaning an order in which for every directed edge  $u \rightarrow v$ , vertex  $u$  comes before  $v$ .

### Algorithm (Kahn's Algorithm - BFS Approach)

1. **Compute in-degree** of all vertices.
2. **Push all vertices** with in-degree **0** into a queue.
3. **Process the queue:**
  - Remove a node and add it to the result list.
  - Decrease the in-degree of its neighbors.
  - If a neighbor's in-degree becomes **0**, push it into the queue.
4. **Repeat until all nodes are processed.**

### Why This Algorithm?

- We use **Kahn's Algorithm (BFS-based)** because it ensures that we always process nodes with zero dependencies first.
- **DFS-based Topological Sort** is an alternative where we use a stack to store nodes after DFS completion.
- **Time Complexity:**  $O(V+E)$  ( $O(V + E)$ ) (same for both BFS and DFS approaches).
- **Space Complexity:**  $O(V)$  for storing the result.

### Code (Java - BFS Approach)

```
import java.util.*;
```

```
public class TopologicalSort {  
    public static List<Integer> topoSort(int V, List<List<Integer>> adj) {
```

```

int[] inDegree = new int[V];
for (List<Integer> neighbors : adj)
    for (int neighbor : neighbors) inDegree[neighbor]++;

Queue<Integer> queue = new LinkedList<>();
for (int i = 0; i < V; i++)
    if (inDegree[i] == 0) queue.add(i);

List<Integer> result = new ArrayList<>();
while (!queue.isEmpty()) {
    int node = queue.poll();
    result.add(node);
    for (int neighbor : adj.get(node))
        if (--inDegree[neighbor] == 0) queue.add(neighbor);
}
return result;
}
}

```

**Leetcode Link**

[Course Schedule II \(Leetcode 210\)](#)

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## 7. Shortest Path Between All Pairs of Nodes in a Weighted Graph (Floyd-Warshall Algorithm)

### Problem Statement

Given a weighted graph, find the shortest paths between all pairs of nodes.

### Algorithm (Floyd-Warshall Algorithm)

1. Create a **distance matrix**, initialized with graph weights.
2. Iterate over **each node  $k$  as an intermediate node**:
  - Update  $\text{dist}[i][j] = \min(\text{dist}[i][j], \text{dist}[i][k] + \text{dist}[k][j])$   $\text{dist}[i][j] = \min(\text{dist}[i][j], \text{dist}[i][k] + \text{dist}[k][j])$ .

3. If  $\text{dist}[i][i]$  is negative, there's a **negative cycle**.

### Why This Algorithm?

- **Floyd-Warshall** is best for small graphs as it runs in  $O(V^3)$ .
- For sparse graphs, **Dijkstra's Algorithm** is better ( $O(V + E \log V)$ ).
- **Space Complexity:**  $O(V^2)$  for the distance matrix.

### Code (Java - Floyd-Warshall)

```
public class FloydWarshall {  
  
    static final int INF = 1000000;  
  
    public static void floydWarshall(int[][] graph) {  
  
        int V = graph.length;  
        int[][] dist = new int[V][V];  
  
        for (int i = 0; i < V; i++)  
            for (int j = 0; j < V; j++) dist[i][j] = graph[i][j];  
  
        for (int k = 0; k < V; k++)  
            for (int i = 0; i < V; i++)  
                for (int j = 0; j < V; j++)  
                    if (dist[i][k] + dist[k][j] < dist[i][j])  
                        dist[i][j] = dist[i][k] + dist[k][j];  
    }  
}
```

### Leetcode Link

[Find the City With the Smallest Number of Neighbors \(Leetcode 1334\)](#)

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## 8. Clone a Directed Graph

### Problem Statement

Given a directed graph, create a **deep copy** of the graph.

### Algorithm (DFS Approach)

1. Use a **hash map** to store visited nodes.
2. Perform **DFS traversal**:
  - Copy each node and its neighbors recursively.

### Why This Algorithm?

- DFS is used because we need to explore and copy all neighbors before returning the node.
- **Time Complexity:**  $O(V+E)O(V + E)$
- **Space Complexity:**  $O(V)O(V)$  for storing nodes.

### Code (Java - DFS Approach)

```
import java.util.*;
```

```
class Node {  
    int val;  
    List<Node> neighbors;  
    public Node(int val) {  
        this.val = val;  
        neighbors = new ArrayList<>();  
    }  
}
```

```
public class CloneGraph {  
    private Map<Node, Node> map = new HashMap<>();  
  
    public Node cloneGraph(Node node) {  
        if (node == null) return null;  
        if (map.containsKey(node)) return map.get(node);  
  
        Node clone = new Node(node.val);  
        map.put(node, clone);
```



```

        for (Node neighbor : node.neighbors)
            clone.neighbors.add(cloneGraph(neighbor));

    return clone;
}
}

```

#### Leetcode Link

[Clone Graph \(Leetcode 133\)](#)

---

## 9. Check if There is a Path Between Two Nodes in a Graph

### Problem Statement

Given a graph and two nodes, check if there exists a path between them.

### Algorithm (DFS or BFS)

1. Use **DFS** (or BFS) to traverse from the source node.
2. If the destination node is reached, return **true**.
3. If all paths are explored and the destination is not found, return **false**.

### Why This Algorithm?

- **DFS** is used when we need a recursive approach and a **single path search**.
- **BFS** is better if we need the **shortest path** in an **unweighted graph**.

### Code (Java - DFS Approach)

```

import java.util.*;

public class GraphPath {

    public static boolean hasPath(Map<Integer, List<Integer>> graph, int src, int dest,
    Set<Integer> visited) {

        if (src == dest) return true;

        if (visited.contains(src)) return false;

        visited.add(src);
    }
}

```

```

        for (int neighbor : graph.getOrDefault(src, new ArrayList<>()))
            if (hasPath(graph, neighbor, dest, visited)) return true;

        return false;
    }
}

```

#### Leetcode Link

[Find If Path Exists in Graph \(Leetcode 1971\)](#)

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## 10. Find the Diameter of a Tree or Graph

### Problem Statement

Find the **longest path** between any two nodes in a tree or graph.

### Algorithm (Two BFS or DFS Traversals)

1. **First BFS/DFS** from any node to find the farthest node XX.
2. **Second BFS/DFS** from XX to find the farthest node YY, which gives the diameter.

### Why This Algorithm?

- Works in  $O(V+E)$  time using **two DFS or BFS traversals**.
- **Greedy approach** ensures the longest path is found efficiently.

### Code (Java - DFS Approach)

```

public class TreeDiameter {

    static int maxDiameter = 0;

    public static int dfs(Map<Integer, List<Integer>> graph, int node, Set<Integer> visited) {
        visited.add(node);

        int max1 = 0, max2 = 0;

        for (int neighbor : graph.get(node)) {
            if (!visited.contains(neighbor)) {
                int depth = dfs(graph, neighbor, visited);

                if (depth > max1) { max2 = max1; max1 = depth; }
            }
        }

        return max1 + max2;
    }
}

```

```

        else if (depth > max2) max2 = depth;
    }
}

maxDiameter = Math.max(maxDiameter, max1 + max2);
return max1 + 1;
}
}

```

**Leetcode Link**

[Diameter of Binary Tree \(Leetcode 543\)](#)

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## 11. Find the Strongly Connected Components (SCCs) of a Directed Graph (Kosaraju's Algorithm)

### Problem Statement

Find all **Strongly Connected Components (SCCs)** in a directed graph, where each SCC is a maximal set of nodes such that every node can reach every other node in the component.

### Algorithm (Kosaraju's Algorithm - Two DFS Traversals)

1. **Perform DFS** and store the finish order in a stack.
2. **Transpose the graph** (reverse all edges).
3. **Perform DFS** in the stack order on the transposed graph.
4. **Each DFS traversal identifies an SCC.**

### Why This Algorithm?

Kosaraju's Algorithm efficiently finds SCCs in a directed graph using two depth-first search (DFS) traversals. The first DFS stores nodes in a finish-time order, and the second DFS on the transposed graph extracts SCCs. This approach ensures linear time complexity  $O(V+E)O(V + E)O(V+E)$ , making it optimal for large graphs.

### Code (Java - Kosaraju's Algorithm)

```

import java.util.*;

public class StronglyConnectedComponents {
    public static void findSCCs(int V, List<List<Integer>> adj) {

```

```

Stack<Integer> stack = new Stack<>();
boolean[] visited = new boolean[V];

for (int i = 0; i < V; i++)
    if (!visited[i]) dfs(adj, i, visited, stack);

List<List<Integer>> transposedGraph = transposeGraph(V, adj);
Arrays.fill(visited, false);

while (!stack.isEmpty()) {
    int node = stack.pop();
    if (!visited[node]) {
        List<Integer> scc = new ArrayList<>();
        dfs(transposedGraph, node, visited, scc);
        System.out.println("SCC: " + scc);
    }
}

private static void dfs(List<List<Integer>> adj, int node, boolean[] visited, Stack<Integer>
stack) {
    visited[node] = true;
    for (int neighbor : adj.get(node))
        if (!visited[neighbor]) dfs(adj, neighbor, visited, stack);
    stack.push(node);
}

private static List<List<Integer>> transposeGraph(int V, List<List<Integer>> adj) {
    List<List<Integer>> transposed = new ArrayList<>();
    for (int i = 0; i < V; i++) transposed.add(new ArrayList<>());

```

```

    for (int i = 0; i < V; i++)
        for (int neighbor : adj.get(i)) transposed.get(neighbor).add(i);
    return transposed;
}
}

```

**Leetcode Link**

[Strongly Connected Components \(Leetcode - Hard\)](#)

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## 12. Convert a Graph to Its Complement

### Problem Statement

The **complement of a graph** is a graph with the same vertices but contains all edges **not** present in the original graph.

### Algorithm

1. **Create an adjacency matrix** of the original graph.
2. **Invert the adjacency matrix** to obtain the complement graph.

### Why This Algorithm?

Using an **adjacency matrix** allows easy inversion of edges in  $O(V^2)$  time. If using an adjacency list, an **efficient set-based lookup** prevents redundant edges, improving performance. The approach guarantees correctness while handling **sparse and dense graphs efficiently**.

### Code (Java - Adjacency Matrix Approach)

```

public class GraphComplement {

    public static int[][] complementGraph(int[][] graph) {

        int V = graph.length;

        int[][] complement = new int[V][V];

        for (int i = 0; i < V; i++) {
            for (int j = 0; j < V; j++) {
                if (i != j) complement[i][j] = (graph[i][j] == 1) ? 0 : 1;
            }
        }
    }
}

```

```

        }
    }
    return complement;
}
}

```

#### Leetcode Link

[Graph Complement Problem](#) (Custom Implementation)

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## 13. Find the Maximum Flow in a Network Flow Graph (Ford-Fulkerson Algorithm)

### Problem Statement

Find the **maximum flow** from the **source (s)** to the **sink (t)** in a flow network.

### Algorithm (Edmonds-Karp Implementation - BFS)

1. Use **BFS** to find an **augmenting path**.
2. Find the **bottleneck capacity** of that path.
3. **Update the residual graph**.
4. Repeat until no more augmenting paths exist.

### Why This Algorithm?

Ford-Fulkerson finds the **maximum flow** by augmenting flow paths iteratively, while the **Edmonds-Karp variation** ensures  $O(VE^2)$  worst-case time complexity using **BFS for shortest augmenting paths**. This method efficiently handles real-world network constraints like **pipeline optimization and traffic routing**.

### Code (Java - BFS Approach)

```

import java.util.*;

public class MaxFlow {
    static final int INF = Integer.MAX_VALUE;

    public static int fordFulkerson(int[][] capacity, int s, int t) {

```

```

int V = capacity.length;

int[][] residual = new int[V][V];

for (int i = 0; i < V; i++)
    System.arraycopy(capacity[i], 0, residual[i], 0, V);

int maxFlow = 0;

int[] parent = new int[V];

while (bfs(residual, s, t, parent)) {
    int flow = INF;

    for (int v = t; v != s; v = parent[v])
        flow = Math.min(flow, residual[parent[v]][v]);

    for (int v = t; v != s; v = parent[v]) {
        residual[parent[v]][v] -= flow;
        residual[v][parent[v]] += flow;
    }

    maxFlow += flow;
}

return maxFlow;
}

private static boolean bfs(int[][] residual, int s, int t, int[] parent) {
    Arrays.fill(parent, -1);

    Queue<Integer> queue = new LinkedList<>();

    queue.add(s);

    parent[s] = s;

    while (!queue.isEmpty()) {

```

```

int u = queue.poll();
for (int v = 0; v < residual.length; v++) {
    if (parent[v] == -1 && residual[u][v] > 0) {
        parent[v] = u;
        queue.add(v);
        if (v == t) return true;
    }
}
}
return false;
}
}

```

**Leetcode Link**

[Maximum Flow Problem](#)

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## 14. Implement Dijkstra's Algorithm

### Why This Algorithm?

Dijkstra's Algorithm is optimal for single-source shortest path problems in weighted graphs. Using a min-heap priority queue, it efficiently finds the shortest path in  $O((V+E)\log V)$  or  $O((V+E) \log V)$ , making it well-suited for navigation systems and network routing.

### Code:

```

import java.util.*;

public class Dijkstra {

    public static int[] dijkstra(int V, List<List<int[]>> adj, int src) {
        PriorityQueue<int[]> pq = new PriorityQueue<>(Comparator.comparingInt(a -> a[1]));
        int[] dist = new int[V];
        Arrays.fill(dist, Integer.MAX_VALUE);
        dist[src] = 0;
        pq.offer(new int[]{src, 0});
    }
}

```



```

while (!pq.isEmpty()) {
    int[] curr = pq.poll();
    int u = curr[0], d = curr[1];

    if (d > dist[u]) continue;

    for (int[] neighbor : adj.get(u)) {
        int v = neighbor[0], weight = neighbor[1];
        if (dist[u] + weight < dist[v]) {
            dist[v] = dist[u] + weight;
            pq.offer(new int[]{v, dist[v]});
        }
    }
}
return dist;
}
}

```

---

## 15. Implement Kruskal's Algorithm

### Why This Algorithm?

Kruskal's Algorithm is efficient for **finding the Minimum Spanning Tree (MST)** by **sorting edges and using Union-Find for cycle detection**. With  $O(E \log V)$  complexity, it performs well in **sparse graphs**, making it ideal for **network design and clustering**.

### Code:

```

import java.util.*;

public class Kruskal {

    public static int kruskal(int V, int[][] edges) {

```

```

Arrays.sort(edges, Comparator.comparingInt(a -> a[2]));
UnionFind uf = new UnionFind(V);
int minCost = 0;

for (int[] edge : edges) {
    if (uf.union(edge[0], edge[1])) minCost += edge[2];
}
return minCost;
}
}

```

---

## 16. Implement Breadth-First Search (BFS)

### Why This Algorithm?

BFS is optimal for **finding the shortest path in an unweighted graph**. Its **level-order traversal** ensures **all nodes at depth  $d$  are visited before depth  $d+1$** . With  $O(V+E)$  complexity, it's widely used in **maze solving, AI, and network traversal**.

### Code:

```

public static void bfs(Map<Integer, List<Integer>> graph, int start) {
    Queue<Integer> queue = new LinkedList<>();
    Set<Integer> visited = new HashSet<>();
    queue.add(start);
    visited.add(start);

    while (!queue.isEmpty()) {
        int node = queue.poll();
        System.out.print(node + " ");
        for (int neighbor : graph.get(node)) {
            if (!visited.contains(neighbor)) {
                queue.add(neighbor);
                visited.add(neighbor);
            }
        }
    }
}

```

```
    }  
  }  
}  
  
}
```

---