

**RV COLLEGE OF ENGINEERING®**

(An Autonomous Institution affiliated to VTU, Belagavi)

**I Semester Master of Technology (Computer Science and Engineering)****ADVANCES IN ALGORITHMS AND APPLICATIONS****Time: 03 Hours****Maximum Marks: 100****Instructions to candidates:**

1. Each unit consists of two questions of 20 marks each.
2. Answer FIVE full questions selecting one from each unit.

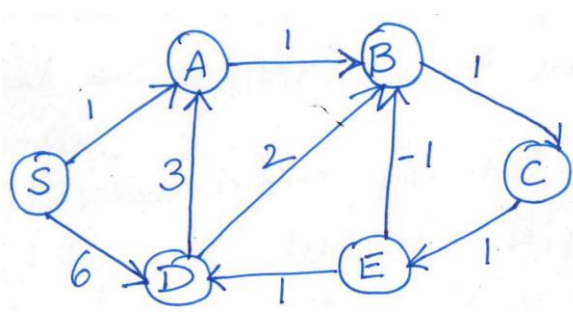
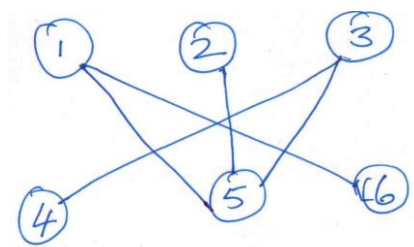
**UNIT-1**

1	a	Solve the equation $\left[T(n) = T\left(\frac{n}{3}\right) + T\left(\frac{2n}{3}\right) + C_n\right]$ using recurrence method.	08
	b	What is the running time of insertion sort on an array $A$ of length $n$ that is already sorted in increasing order? Given example.	08
	c	Solve the following using Master's theorem. i) $T(n) = 7T\left(\frac{n}{3}\right) + n^2$ ii) $T(n) = 4T\left(\frac{n}{2}\right) + n^2$	04
<b>OR</b>			
2	a	Illustrate the counting sort on the array $A = \langle 6, 0, 2, 0, 1, 3, 4, 6, 1, 3, 2 \rangle$ and mention time complexity.	10
	b	Prove that $T(n) = 2T\left(\frac{n}{2}\right) + n = O(n \log n)$ using substitution method.	10

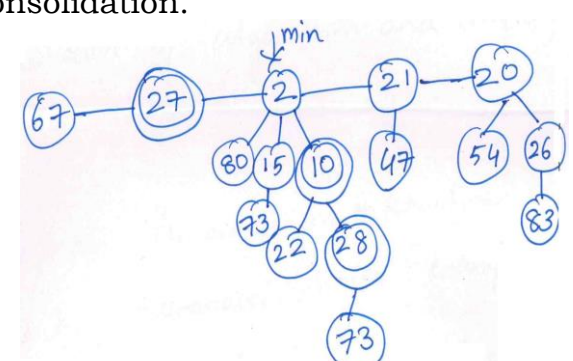
**UNIT-2**

3	a	Find the longest common sub-sequence for the given strings and trace back the solution. $X = abcaabcb$ $Y = acbabcb$ Calculate time complexity.	08																					
	b	What is Activity Selection Problem? Find the solution of Activity Selection problem for the following set of activities. What is the time complexity?																						
		<table><tr><td><math>i</math></td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td></tr><tr><td><math>S_i</math></td><td>1</td><td>3</td><td>0</td><td>5</td><td>8</td><td>5</td></tr><tr><td><math>F_i</math></td><td>2</td><td>4</td><td>6</td><td>7</td><td>9</td><td>9</td></tr></table>	$i$	1	2	3	4	5	6	$S_i$	1	3	0	5	8	5	$F_i$	2	4	6	7	9	9	08
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$F_i$	2	4	6	7	9	9																		
	c	Explain potential method of amortized analysis.	04																					
		<b>OR</b>																						
4	a	What is matrix chain multiplication problem? Write the algorithm for matrix chain multiplication. Find 'm' and 's' table computed by the algorithm for the following matrix dimension. <table><tr><td><math>A_1</math></td><td><math>30 \times 35</math></td></tr><tr><td><math>A_2</math></td><td><math>35 \times 15</math></td></tr><tr><td><math>A_3</math></td><td><math>15 \times 5</math></td></tr><tr><td><math>A_4</math></td><td><math>5 \times 10</math></td></tr><tr><td><math>A_5</math></td><td><math>10 \times 20</math></td></tr><tr><td><math>A_6</math></td><td><math>20 \times 25</math></td></tr></table>	$A_1$	$30 \times 35$	$A_2$	$35 \times 15$	$A_3$	$15 \times 5$	$A_4$	$5 \times 10$	$A_5$	$10 \times 20$	$A_6$	$20 \times 25$	10									
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	b	Explain Accounting method for stack operations.	05																					
	c	Discuss elements of greedy strategy with example.	05																					

### UNIT-3

5	<p>a Apply Bellmanford algorithm on the given graph in Fig. 5.a with source vertex <math>S</math> with all the iterations. What is the complexity of the algorithm?</p>	
	<p style="text-align: center;">  </p> <p style="text-align: center;">Fig. 5.a</p> <p>b Write Ford-Fulkerson algorithm and its complexity.</p> <p>c Apply maximum matching algorithm to the following bipartite graph in Fig. 5.c.</p> <p style="text-align: center;">  </p> <p style="text-align: center;">Fig. 5.c</p>	08 08
	<p style="text-align: center;"><b>OR</b></p> <p>a Write Johnson algorithm and discuss its complexity. Write the importance of Dijkstra algorithm in Johnson method.</p> <p>b Draw finite automata table and diagram for the pattern ACACAGA. Write the complexity.</p>	04  10 10

### UNIT-4

7	<p>a Consider the Fibonacci heap given in Fig. 7.a. Nodes that are double circled are marked nodes.</p> <ol style="list-style-type: none"> <li>What is the potential of the heap?</li> <li>Suppose delete_min is performed, show the resulting heap after consolidation.</li> </ol> <p style="text-align: center;">  </p> <p style="text-align: center;">Fig. 7.a</p>	
	<p>b Explain Knuth-Morris-Pratt (KMP) string matching algorithm and show its complexity.</p> <p style="text-align: center;"><b>OR</b></p>	10 10

8	a	Explain operation on disjoint_sets and its union find problem.	10
	b	Write algorithm and give complexity of finite automata string matcher.	07
	c	Generate prefix table for pattern $P = ababaca$ .	03

### UNIT-5

9	a	Explain the working of the following keywords with respect to parallel programming: i) Parallel ii) Spawn iii) Sync.	08
	b	Compare merge sort algorithm with parallel merge sort algorithm with illustration of algorithm and complexity.	12
<b>OR</b>			
10	a	Explain dynamic multithreading with Fibonacci series example.	10
	b	Illustrate working of multithreaded matrix multiplication with an example.	10