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Assignment 1

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Download all python codes from

https://github.com/Sushma-AI1103/Assignment-1/blob/main/assingment 1code.py

1 Problem

(4.12) Determine P(E|F), if a die is thrown three times,

E: 4 appears on third toss

F: 6 and 5 appears on respectively on first and second toss.

2 Solution

Throwing a die three times is similar to throw three die simultaneously as every trial is independent.

Let $X_i = \{1, 2, 3, 4, 5, 6\}$ where i = 1, 2, 3Now , for a fair die , all events are equally likely. Therefore ,

$$Pr(X_i = n) = \frac{1}{6} \qquad 1 \le n \le 6$$

$$= 0 \qquad otherwise \qquad (2.0.1)$$

probability of event E,

$$Pr(E) = Pr(X_3 = 4) = \frac{1}{6}$$

(2.0.2)

similarly, Probability of event F would be,

$$Pr(F) = Pr(X_1 = 6, X_2 = 5)$$

$$= Pr(X_1 = 6) Pr(X_2 = 5)$$

$$= \frac{1}{6} \cdot \frac{1}{6} = \frac{1}{36}$$

since events are independent.

Now, Probability of E and F would be

$$Pr(EF) = Pr(X_1 = 6, X_2 = 5, X_3 = 4)$$

$$= Pr(X_1 = 6) Pr(X_2 = 5) Pr(X_3 = 4)$$

$$= \frac{1}{6} \cdot \frac{1}{6} \cdot \frac{1}{6}$$

$$= \frac{1}{216}$$
(2.0.3)

Probability P(E|F),

$$P(E \mid F) = \frac{\Pr EF}{\Pr F}$$
$$= \frac{\frac{1}{216}}{\frac{1}{36}}$$
$$= \frac{1}{6}$$