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# Assignment 1

# Sushma - CS20BTECH11051

## Download all python codes from

https://github.com/Sushma-AI1103/Assignment-1/blob/main/assingment\_1code.py

#### 1 Problem

( 4.12) Determine P(E|F), if a die is thrown three times,

E: 4 appears on third toss

F: 6 and 5 appears on respectively on first and second toss.

### 2 Solution

Throwing a die three times is similar to throw three die simultaneously as every trial is independent.

Let  $X_i = \{1, 2, 3, 4, 5, 6\}$  where i = 1, 2, 3Now, for a fair die, all events are equally likely. Therefore,

$$\Pr\left(X_{i} = n\right) = \begin{cases} \frac{1}{6} & 1 \le n \le 6\\ 0 & otherwise \end{cases} \tag{2.0.1}$$

Let us assume

$$p = \frac{1}{6},\tag{2.0.2}$$

probability of event E,

$$Pr(E) = Pr(X_3 = 4) = p$$
 (2.0.3)

similarly, Probability of event F would be,

$$Pr(F) = Pr(X_1 = 6, X_2 = 5) = Pr(X_1 = 6) Pr(X_2 = 5)$$

$$(2.0.4)$$

$$= p \cdot p = p^2$$

$$(2.0.5)$$

since events are independent.

Now, Probability of E and F would be

$$Pr(EF) = Pr(X_1 = 6, X_2 = 5, X_3 = 4)$$
 (2.0.6)

= 
$$Pr(X_1 = 6) Pr(X_2 = 5) Pr(X_3 = 4)$$
 (2.0.7)

$$= p \cdot p \cdot p \qquad (2.0.8)$$

$$= p^3$$
 (2.0.9)

Probability P(E|F),

$$P(E \mid F) = P(X_3 = 4 \mid X_1 = 6, X_2 = 5)$$
 (2.0.10)

$$= \frac{\Pr(EF)}{\Pr(F)} \quad (2.0.11)$$

$$= \frac{\Pr(X_1 = 6, X_2 = 5, X_3 = 4)}{\Pr(X_1 = 6, X_2 = 5)}$$
 (2.0.12)

$$=\frac{p^3}{p^2}=p \qquad (2.0.13)$$

$$=\frac{1}{6}$$
 (2.0.14)