

optimazation Assignment-1

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Problem Statement The maximum distance from $(0,0)$ to a point on the curve $x=asint-bsin(\frac{at}{b})$ and $y=acost-bcos(\frac{at}{b})$ for both $a,b>0$ is

Solution

The distance from origin to the point is given by

$$P(t)^2 = (x^2 - 0) + (y^2 - 0) \quad (0.0.1)$$

$$P(t)^2 = a^2 + b^2 - 2ab[\cos(t - \frac{at}{b})] \quad (0.0.2)$$

$$p'(t)^2 = -2ab \sin(t - \frac{at}{b})(1 - \frac{a}{b}) \quad (0.0.3)$$

Using gradient descent method we can find its maxima ,

$$x_{n+1} = x_n + \alpha \nabla f(x_n) \quad (0.0.4)$$

$$\Rightarrow x_{n+1} = x_n + \alpha(a^2 + b^2 - 2ab[\cos(t - \frac{at}{b})]) \quad (0.0.5)$$

Taking $a = 5, b = 2, \alpha = 0.001$ and precision = 0.00000001, values obtained using python are:

$$\boxed{\text{Maximum Distance} = 3.00000} \quad (0.0.6)$$

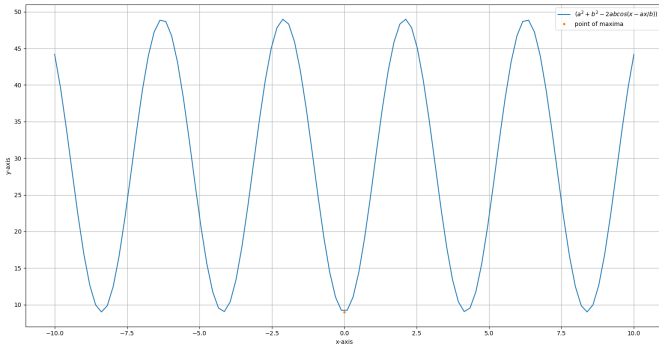


Figure 0: Figure of construction