

**Problem 1 (1.9) Score:** \_\_\_\_\_.

Assume for arithmetic, load/store, and branch instructions, a processor has CPIs of 1, 12, and 5, respectively. Also assume that on a single processor a program requires the execution of  $2.56 \times 10^9$  arithmetic instructions,  $1.28 \times 10^9$  load/store instructions, and 256 million branch instructions. Assume that each processor has a 2 GHz clock frequency.

Assume that, as the program is parallelized to run over multiple cores, the number of arithmetic and load/ store instructions per processor is divided by  $0.7 \times p$  (where  $p$  is the number of processors) but the number of branch instructions per processor remains the same.

- (1) Find the total execution time for this program on 1, 2, 4, and 8 processors, and show the relative speedup of the 2, 4, and 8 processor result relative to the single processor result.
- (2) If the CPI of the arithmetic instructions was doubled, what would the impact be on the execution time of the program on 1, 2, 4, or 8 processors?
- (3) To what should the CPI of load/store instructions be reduced in order for a single processor to match the performance of four processors using the original CPI values?

**Solution:** (1) Consider the program on one processor, the total cycle count is  $1 \times 2.56 \times 10^9 + 12 \times 1.28 \times 10^9 + 5 \times 2.56 \times 10^8 = 1.92 \times 10^{10}$ . Then consider the total execution time, that is, the *cycle count/cycle frequency*:

$$\text{Execution time for one processor is } 1.92 \times 10^{10} / (2 \times 10^9) = 9.6 \times 10^9$$

By the same way, the total execution time for this program on 2, 4, and 8 processors are shown in the following table.

processor count	arithmetic inst.	L/S inst.	branch inst.	cycles	execution time	speed up rate
1	2.56E9	1.28E9	2.56E8	1.92E10	9.60E9	1.00
2	1.83E9	9.14E8	2.56E8	1.41E10	7.05E9	1.36
4	9.14E8	4.57E8	2.56E8	7.68E9	3.84E9	2.50
8	4.57E8	2.29E8	2.56E8	3.46E9	1.73E9	5.55

Table 1: Execution time and speed-up rate

- (2) The answer is shown in following table.

processor count	execution time
1	9.84E9
2	7.95E9
4	4.30E9
8	2.47E9

Table 2: Execution after double the CPI of arithmetic instructions

- (3) Assume the  $CPI_{L/S\_inst.}$  is reduce to  $x$ . Then the execution time (Hint: the performance is measured by the execution time) of one processor is

$$2.56 \times 10^9 + 1.28 \times 10^9 x + 2.56 \times 10^8 \times 5 = 3.84 \times 10^9 + 1.28 \times 10^8 x$$

With original CPI values, the execution time of four processors is

$$2.56 \times 10^9 / (0.7 \times 4) + 1.28 \times 10^9 \times 12 / (0.7 \times 4) + 2.56 \times 10^8 \times 5 = 7.68 \times 10^9$$

To minimize the difference of performance, that is to reduce the *abs* difference of the two result above:

$$|(3.84 \times 10^9 + 1.28 \times 10^8 x) - (7.68 \times 10^9)| \quad \text{Then } x = 3. \text{ That is the answer.}$$

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**Problem 2 (1.11) Score: \_\_\_\_\_.**

The results of the SPEC CPU2006 bzip2 benchmark running on an AMD Barcelona has an instruction count of 2.389E12, an execution time of 750 s, and a reference time of 9650 s.

- (1) Find the CPI if the clock cycle time is 0.333 ns.
- (2) Find the SPECratio.
- (3) Find the increase in CPU time if the number of instructions of the benchmark is increased by 10% without affecting the CPI.
- (4) Find the increase in CPU time if the number of instructions of the benchmark is increased by 10% and the CPI is increased by 5%.
- (5) Find the change in the SPECratio for this change.
- (6) Suppose that we are developing a new version of the AMD Barcelona processor with a 4 GHz clock rate. We have added some additional instructions to the instruction set in such a way that the number of instructions has been reduced by 15%. The execution time is reduced to 700 s and the new SPECratio is 13.7. Find the new CPI.
- (7) This CPI value is larger than obtained in 1.11.1 as the clock rate was increased from 3 GHz to 4 GHz. Determine whether the increase in the CPI is similar to that of the clock rate. If they are dissimilar, why?
- (8) By how much has the CPU time been reduced?
- (9) For a second benchmark, libquantum, assume an execution time of 960 ns, CPI of 1.61, and clock rate of 3 GHz. If the execution time is reduced by an additional 10% without affecting the CPI and with a clock rate of 4 GHz, determine the number of instructions.
- (10) Determine the clock rate required to give a further 10% reduction in CPU time while maintaining the number of instructions and with the CPI unchanged.
- (11) Determine the clock rate if the CPI is reduced by 15% and the CPU time by 20% while the number of instructions is unchanged.

**Solution:** (1) CPU time = Instruction count × CPI × clock cycle time, then  $CPI = \frac{750s}{2.389 \times 10^{12} \times 0.333 \times 10^{-9}s} \approx 0.943$ .

- (2) The SPECratio is  $\frac{T_{ref}}{T_{actual}} = \frac{9650s}{750s} \approx 12.87$ .
- (3) From CPU time = Instruction count × CPI × clock cycle time, hence if number of instructions of the benchmark is increased by 10% then the CPU time is increased by 10%.
- (4) From (3) we can obtain that  $\frac{T_{new}}{T_{old}} = 1.1 \times 1.05 = 1.155$  ( $T_{old}$  represents the CPU time before change, and  $T_{new}$  represents the CPU time after change). That is, the CPU time is increased by 15.5%.
- (5) The change of SPECratio can extract from the change of execution time because:

$$\frac{SPECratio_{new}}{SPECratio_{old}} = \frac{\frac{T_{ref}}{T_{actual_{new}}}}{\frac{T_{ref}}{T_{actual_{old}}}} = \frac{T_{actual_{old}}}{T_{actual_{new}}} = \frac{1}{1.155} \approx 0.866$$

That is, the SPECratio is decreased by 13.4%.

- (6) CPU time = Instruction count × CPI × clock cycle time, then  $CPI = \frac{700 \times 4 \times 10^9}{0.85 \times 2.389 \times 10^{12}} \approx 1.38$
- (7) Clock rate ratio is  $\frac{4GHz}{3GHz} \approx 1.33$ . CPI ratio is  $\frac{1.38}{0.94} \approx 1.47$ . So they are dissimilar. The reason is when the number of instructions has been reduced by 15%, the CPU time is decreased from 750s to 700s at the same time, then there is a difference between clock rate ratio and CPI ratio.
- (8)  $\frac{700s}{750s} \approx 0.933$ , so the CPU time has been reduced by 6.7%.
- (9) Number of instructions = CPU time ×  $\frac{CPI}{CPU\ time}$  =  $960 \times 0.9 \times 4 \times 10^9 / 1.61 \approx 2.147 \times 10^{12}$
- (10) Only change clock rate to reduce the CPU time. Clock rate = Number of instructions × CPI / CPU time. The new clock is  $3GHz \times \frac{1}{0.9} \approx 3.33GHz$ .
- (11) Change clock rate and CPI to reduce the CPU time. Clock rate = Number of instructions × CPI / CPU time. The new clock is  $3GHz \times 0.85 \times \frac{1}{0.8} \approx 3.19GHz$ .

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