

Sutiksh Verma – Sec 6

002122052

Program Structures and Algorithms

Fall 2021

Assignment No: 2

Task: To implement the class Timer.java and InsertionSort.java and also measure the running times of the sort using four different initial array ordering situations i.e. Random, Ordered, Partially-Ordered and Reverse ordered array.

Output:

The screenshot displays an IDE with a Java project. The main editor shows the `Benchmark_Timer.java` file, which contains a `main` method for benchmarking an insertion sort. The code includes comments and a `benchTimer` object to measure the time taken for different array sizes.

```
126 public static void main(String[] args) {
127
128     //Instantiate the insertion sort class
129     InsertionSort ins_sort = new InsertionSort();
130
131     //Instantiate Benchmark_Timer class to perform Benchmark Test
132     Benchmark_Timer<Integer> benchTimer = new Benchmark_Timer<>("description: \"Benchmark Test\", (Pre)null, (x) -> ins_sort.sort(x, (from) 0, x.length), (Post)null);
133
134     //Create a randomly ordered array and run benchmark test
```

The Run console shows the output of the benchmark test, displaying the time taken for different array sizes (N=800, 1600, 3200, 6400) and the time taken for different array sizes (N=800, 1600, 3200, 6400).

```
Run: Benchmark_Timer
Value of N: 800 Order Situation- Randomly Ordered Time Taken: 0.7
2021-09-24 15:47:08 INFO Benchmark_Timer - Begin run: Benchmark Test with 10 runs
Value of N: 1600 Order Situation- Randomly Ordered Time Taken: 2.6
2021-09-24 15:47:08 INFO Benchmark_Timer - Begin run: Benchmark Test with 10 runs
Value of N: 3200 Order Situation- Randomly Ordered Time Taken: 10.3
2021-09-24 15:47:08 INFO Benchmark_Timer - Begin run: Benchmark Test with 10 runs
Value of N: 6400 Order Situation- Randomly Ordered Time Taken: 40.2
-----
2021-09-24 15:47:08 INFO Benchmark_Timer - Begin run: Benchmark Test with 10 runs
Value of N: 800 Order Situation- Ordered Time Taken: 0.0
2021-09-24 15:47:08 INFO Benchmark_Timer - Begin run: Benchmark Test with 10 runs
Value of N: 1600 Order Situation- Ordered Time Taken: 0.0
2021-09-24 15:47:08 INFO Benchmark_Timer - Begin run: Benchmark Test with 10 runs
Value of N: 3200 Order Situation- Ordered Time Taken: 0.0
2021-09-24 15:47:08 INFO Benchmark_Timer - Begin run: Benchmark Test with 10 runs
Value of N: 6400 Order Situation- Ordered Time Taken: 0.1
2021-09-24 15:47:08 INFO Benchmark_Timer - Begin run: Benchmark Test with 10 runs
Value of N: 8000 Order Situation- Ordered Time Taken: 0.1
-----
2021-09-24 15:47:08 INFO Benchmark_Timer - Begin run: Benchmark Test with 10 runs
```

The bottom status bar shows the file encoding as UTF-8, 4 spaces, and the date and time as 15:47 on 24-09-2021.

Console Output:

2021-09-24 16:03:52 INFO Benchmark_Timer - Begin run: Benchmark Test with 10 runs

Value of N: 200 Order Situation- Randomly Ordered Time Taken: 0.3

2021-09-24 16:03:52 INFO Benchmark_Timer - Begin run: Benchmark Test with 10 runs

Value of N: 400 Order Situation- Randomly Ordered Time Taken: 0.6

2021-09-24 16:03:52 INFO Benchmark_Timer - Begin run: Benchmark Test with 10 runs

Value of N: 800 Order Situation- Randomly Ordered Time Taken: 0.9

2021-09-24 16:03:52 INFO Benchmark_Timer - Begin run: Benchmark Test with 10 runs

Value of N: 1600 Order Situation- Randomly Ordered Time Taken: 2.4

2021-09-24 16:03:52 INFO Benchmark_Timer - Begin run: Benchmark Test with 10 runs

Value of N: 3200 Order Situation- Randomly Ordered Time Taken: 11.5

2021-09-24 16:03:52 INFO Benchmark_Timer - Begin run: Benchmark Test with 10 runs

Value of N: 6400 Order Situation- Randomly Ordered Time Taken: 40.0

2021-09-24 16:03:52 INFO Benchmark_Timer - Begin run: Benchmark Test with 10 runs

Value of N: 200 Order Situation- Ordered Time Taken: 0.0

2021-09-24 16:03:52 INFO Benchmark_Timer - Begin run: Benchmark Test with 10 runs

Value of N: 400 Order Situation- Ordered Time Taken: 0.0

2021-09-24 16:03:52 INFO Benchmark_Timer - Begin run: Benchmark Test with 10 runs

Value of N: 800 Order Situation- Ordered Time Taken: 0.0

2021-09-24 16:03:52 INFO Benchmark_Timer - Begin run: Benchmark Test with 10 runs

Value of N: 1600 Order Situation- Ordered Time Taken: 0.0

2021-09-24 16:03:52 INFO Benchmark_Timer - Begin run: Benchmark Test with 10 runs

Value of N: 3200 Order Situation- Ordered Time Taken: 0.0

2021-09-24 16:03:52 INFO Benchmark_Timer - Begin run: Benchmark Test with 10 runs

Value of N: 6400 Order Situation- Ordered Time Taken: 0.1

2021-09-24 16:03:52 INFO Benchmark_Timer - Begin run: Benchmark Test with 10 runs

Value of N: 200 Order Situation- Partially Ordered Time Taken: 0.0

2021-09-24 16:03:52 INFO Benchmark_Timer - Begin run: Benchmark Test with 10 runs

Value of N: 400 Order Situation- Partially Ordered Time Taken: 0.1

2021-09-24 16:03:52 INFO Benchmark_Timer - Begin run: Benchmark Test with 10 runs

Value of N: 800 Order Situation- Partially Ordered Time Taken: 0.4

2021-09-24 16:03:52 INFO Benchmark_Timer - Begin run: Benchmark Test with 10 runs

Value of N: 1600 Order Situation- Partially Ordered Time Taken: 2.0

2021-09-24 16:03:52 INFO Benchmark_Timer - Begin run: Benchmark Test with 10 runs

Value of N: 3200 Order Situation- Partially Ordered Time Taken: 8.6

2021-09-24 16:03:53 INFO Benchmark_Timer - Begin run: Benchmark Test with 10 runs

Value of N: 6400 Order Situation- Partially Ordered Time Taken: 18.0

2021-09-24 16:03:53 INFO Benchmark_Timer - Begin run: Benchmark Test with 10 runs

Value of N: 200 Order Situation- Reverse Ordered Time Taken: 0.1

2021-09-24 16:03:53 INFO Benchmark_Timer - Begin run: Benchmark Test with 10 runs

Value of N: 400 Order Situation- Reverse Ordered Time Taken: 0.3

2021-09-24 16:03:53 INFO Benchmark_Timer - Begin run: Benchmark Test with 10 runs

Value of N: 800 Order Situation- Reverse Ordered Time Taken: 1.2

2021-09-24 16:03:53 INFO Benchmark_Timer - Begin run: Benchmark Test with 10 runs

Value of N: 1600 Order Situation- Reverse Ordered Time Taken: 5.0

2021-09-24 16:03:53 INFO Benchmark_Timer - Begin run: Benchmark Test with 10 runs

Value of N: 3200 Order Situation- Reverse Ordered Time Taken: 19.0

2021-09-24 16:03:53 INFO Benchmark_Timer - Begin run: Benchmark Test with 10 runs

Value of N: 6400 Order Situation- Reverse Ordered Time Taken: 72.3

Process finished with exit code 0

Relationship Conclusion: It can be observed from the results of the benchmark test:

In best-case scenario, which happens when the array is sorted, the insertion sort runs in $O(n)$ time as it simply compares the elements with no swapping required

In the average-case, when the array is sorted in randomly-ordered or partially ordered manner the insertion sort runs in $O(n^2)$ time

Similarly, in the worst-case scenario, when the array is sorted in the reverse order manner the insertion sort takes $O(n^2)$ time because for inserting the last element, the algorithm will need $n-1$ comparisons and perform $n-1$ swaps and so on.

Therefore, we get: $2(1+2+3+\dots+n-2+n-1)$

$$= n(n-1) \quad \text{[Using Sum of n formula]}$$

$$= n^2 - n$$

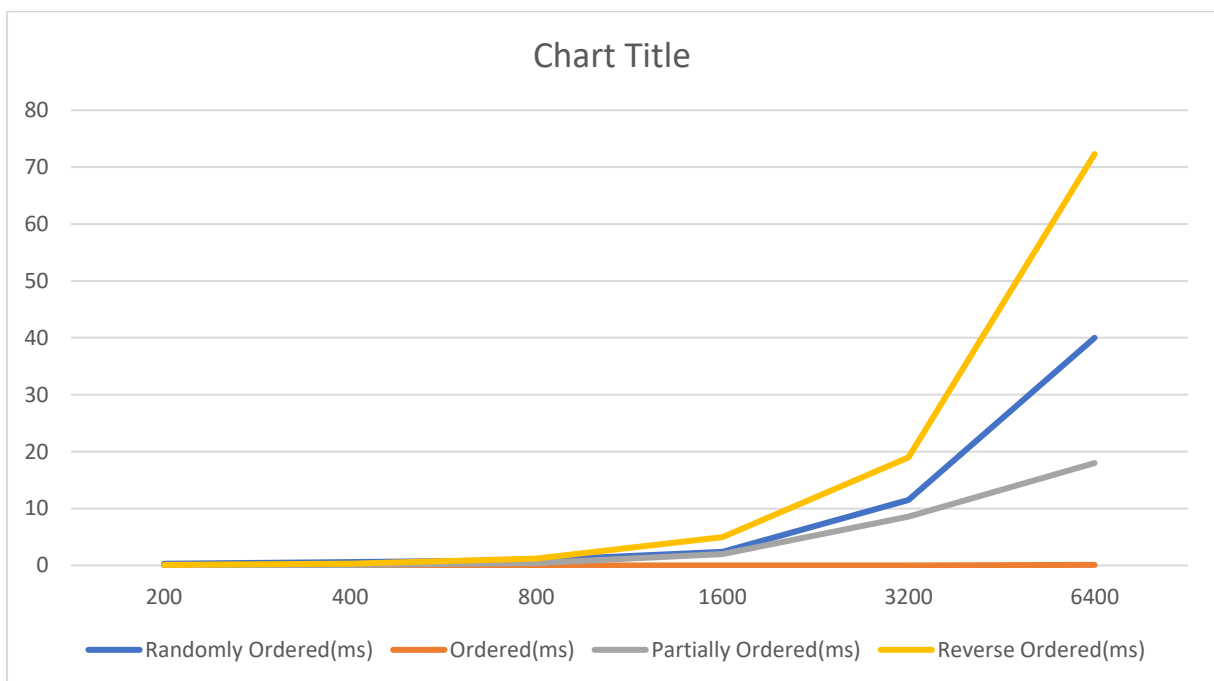
$$\sim n^2$$

Thus, it can be derived that the following pattern is followed by the run time of insertion sort for different order situation in arrays

Ordered < Partially Ordered < Randomly Ordered < Reverse Ordered
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Evidence: I have attached a chart and a table to show the data of the different outputs observed conducting different experiments with different values of n . As a result, We can see the proportionate increase of the time with respect to the increased value of n using different sorted situations-

Value of N	Randomly Ordered(ms)	Ordered(ms)	Partially Ordered(ms)	Reverse Ordered(ms)
200	0.3	0.0	0.0	0.1
400	0.6	0.0	0.1	0.3
800	0.9	0.0	0.4	1.2
1600	2.4	0.0	2.0	5.0
3200	11.5	0.0	8.6	19.0
6400	40.0	0.1	18.0	72.3



The horizontal axis is N: size of the input array.

Passed Unit Tests: Following are the images of passes unit tests which are TimerTest.java, BenchmarkTimer.java, InsertionSortTest.java.

