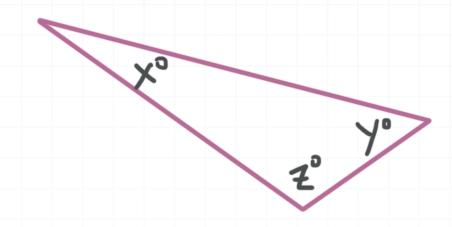
Interior angles of triangles

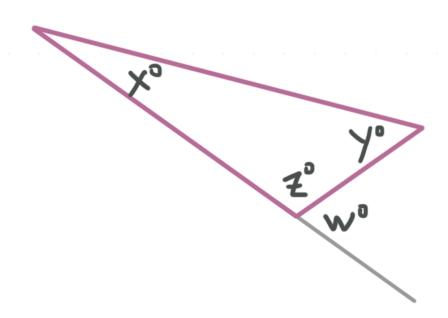
The interior angles of a triangle are the three angles on the inside of a triangle. The measures of these three angles always sum to 180° .



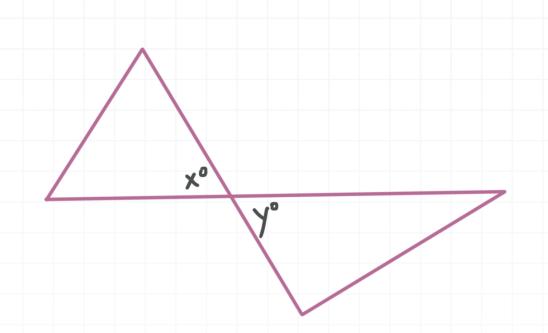
$$x^{\circ} + y^{\circ} + z^{\circ} = 180^{\circ}$$

There are a few other angle relationships we need to remember:

The measures of a pair of adjacent angles that (together) form a straight line add to 180° , so $z^{\circ} + w^{\circ} = 180^{\circ}$.



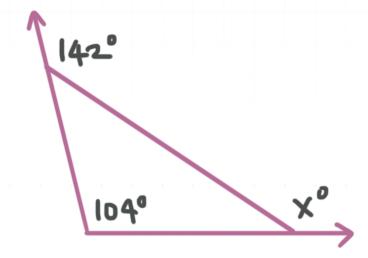
Vertical angles are congruent, so $x^{\circ} = y^{\circ}$.



Let's start by working through an example.

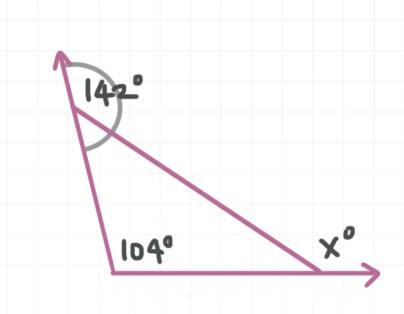
Example

What is the value of x?



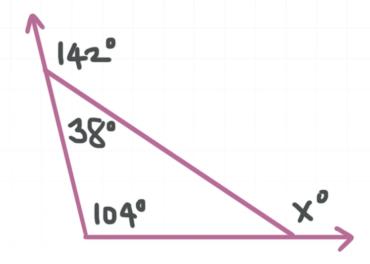
We know that the angle of measure 142° and the interior angle adjacent to it, together, form a straight line:





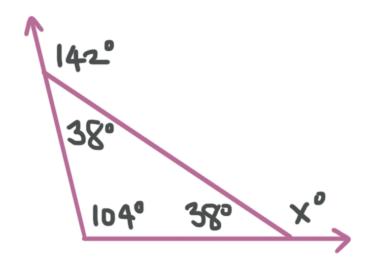
We can find the measure of that interior angle by subtraction:

$$180^{\circ} - 142^{\circ} = 38^{\circ}$$
.



The measures of the three angles inside a triangle sum to 180° , so the measure of the third interior angle is

$$180^{\circ} - 104^{\circ} - 38^{\circ} = 38^{\circ}$$



We can see that the adjacent angles of measure x° and 38° , together, form a straight line, so

$$x^{\circ} + 38^{\circ} = 180^{\circ}$$

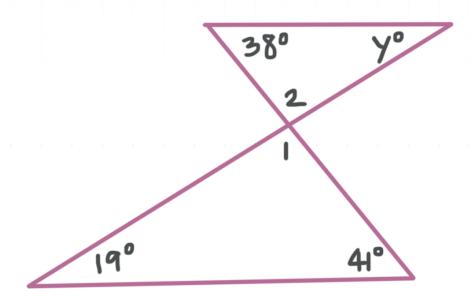
$$x^{\circ} = 142^{\circ}$$

$$x = 142$$

Let's try another one.

Example

What is the value of *y*?



The measures of the three interior angles of a triangle sum to 180° , so

$$m \angle 1 + 19^{\circ} + 41^{\circ} = 180^{\circ}$$

$$m \angle 1 = 120^{\circ}$$



Angle 1 and angle 2 are a pair of vertical angles, and vertical angles are congruent, so

$$m \angle 1 = m \angle 2 = 120^{\circ}$$

Again, the measures of the three interior angles of a triangle sum to 180° , so we see that

$$m \angle 2 + 38^{\circ} + y^{\circ} = 180^{\circ}$$

$$120^{\circ} + 38^{\circ} + y^{\circ} = 180^{\circ}$$

$$y^{\circ} = 22^{\circ}$$

$$y = 22$$

