

LMB = 

4	4	4	6	6	6	6
0	1	2	3	4	5	6

 → Left Max Boundary

RMB = 

6	6	6	6	5	5	5
0	1	2	3	4	5	6

 → Right Max Boundary

Trapped water at index  $i$  =  $\underbrace{\min(LMB[i], RMB[i])}_{\text{Water level}} - \text{height}[i]$

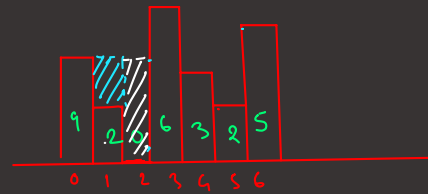
Potential water =  $\sum tw$

$LMB[i] = \max(LMB[i-1], \text{height}[i])$  if  $i \neq 0$

for  $i=0$ ,  $LMB[0] = \text{height}[0]$

$RMB[i] = \max(RMB[i+1], \text{height}[i])$  if  $i \neq n-1$

if  $i = n-1$ ,  $RMB[i] = \text{height}[i]$



$$tw[0] = \min(LMB[0], RMB[0]) - \text{height}[0] \\ = \min(4, 6) - 4 = 4 - 4 = 0$$

$$tw[1] = \min(4, 6) - 2 = 4 - 2 = 2$$

$$tw[2] = \min(4, 6) - 0 = 4 - 0 = 4$$

⋮

## Sorting

① Bubble Sort: large elements come to the end of array by swapping with the adjacent element.

A → 

8	5	7	3	2
---	---	---	---	---

$i=0$   
1<sup>st</sup> pass

8	5	5	5	5
5	8	7	7	7
7	7	8	3	3
3	3	3	8	2
2	2	2	2	8

Comp = 4  
max swap = 4

result for pass 1  
2<sup>nd</sup> pass  $i=1$

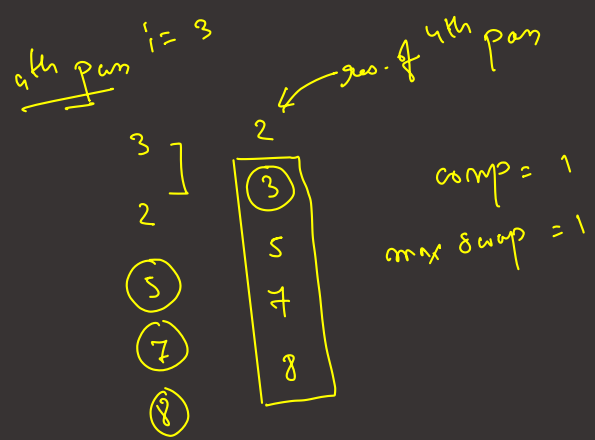
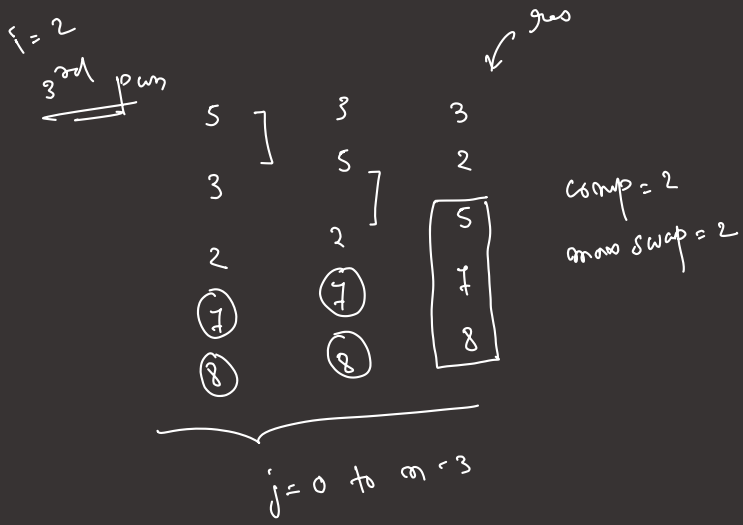
5	5	5	5
7	7	3	3
3	3	7	2
2	2	2	7
8	8	8	8

2<sup>nd</sup> pass

Comp = 3  
swap = 2  
max swap = 3

$j=0$  to  $n-2$

$j=0$  to  $n-1$



$\therefore$  total no of comp =  $(n-1) + \dots + 3 + 2 + 1$

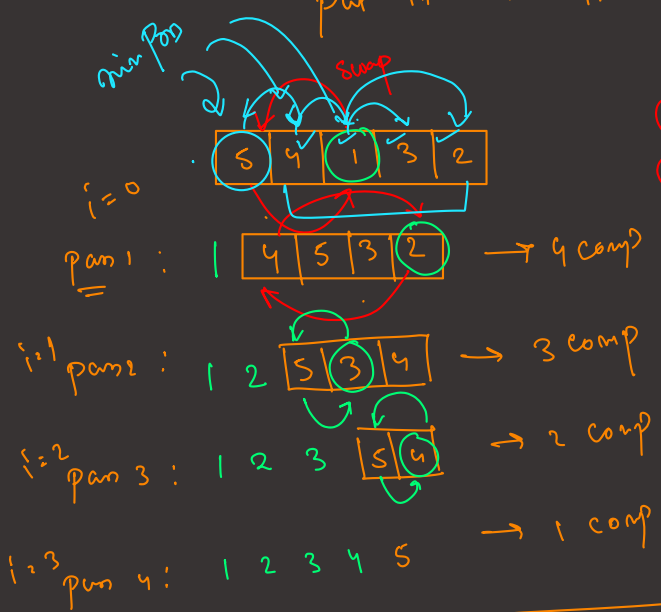
Note Bubble sort  $\rightarrow$  adaptive  
(not by default)  
 $\downarrow$   
stable (HW)

time complexity =  $O(n^2)$   $\leftarrow$  max swap

for (int i = 0; i < n-1; i++)  
for (int j = 0; j < n-1-i; j++)  
// start & end.  
 $\downarrow$   
comp or swap

$O\left(\frac{n^2}{2} - \frac{n}{2}\right)$   
 $= O(n^2/2) = O(n^2)$

Selection sort pick the smallest (from unsorted part),  
put it at the beginning.



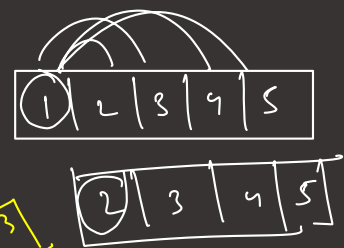
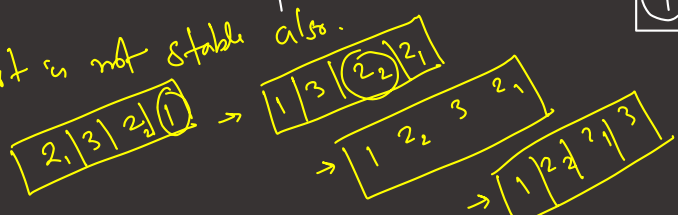
- check for the min of unsorted array.
- ele [1<sup>st</sup> index]  $\leftrightarrow$  ele [position]

total no. of swap =  $n-1$   
 $= O(n)$

total comp =  $\frac{n(n-1)}{2} = O(n^2) \leftarrow$  time complexity

② Selection sort is not adaptive

③ Selection sort is not stable also.



1 2 4 3 6 5

1  
2  
4  
3  
6  
5

1  
2  
4  
3  
6  
5

1  
2  
4  
3  
6  
5

1  
2  
3  
4  
6  
5

1  
2  
3  
4  
6  
5



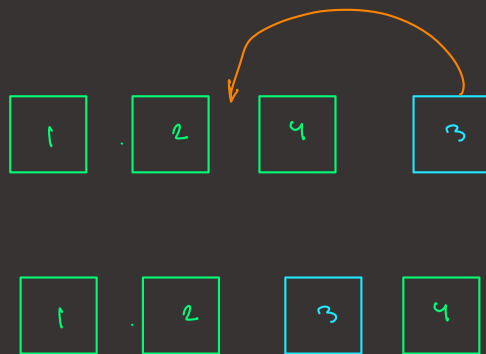
4 1 2 5 3

4  
1  
2  
5  
3

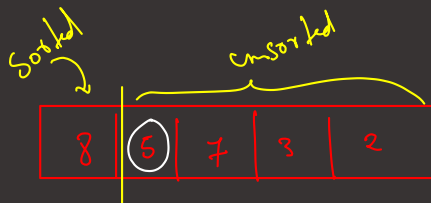
4  
1  
2  
5  
3

4  
1  
2  
5  
3

## Insertion Sort



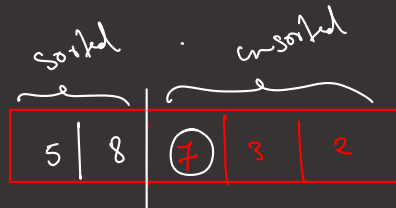
pick an element from unsorted part and place it at the right position of the sorted array.



comp  $\rightarrow$  5  $\leftarrow$  temp = arr[1]

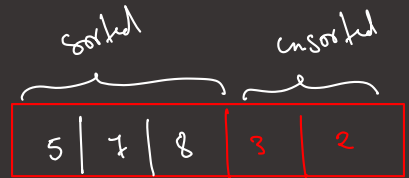


comp  $\rightarrow$  7  $\leftarrow$  temp = arr[2]



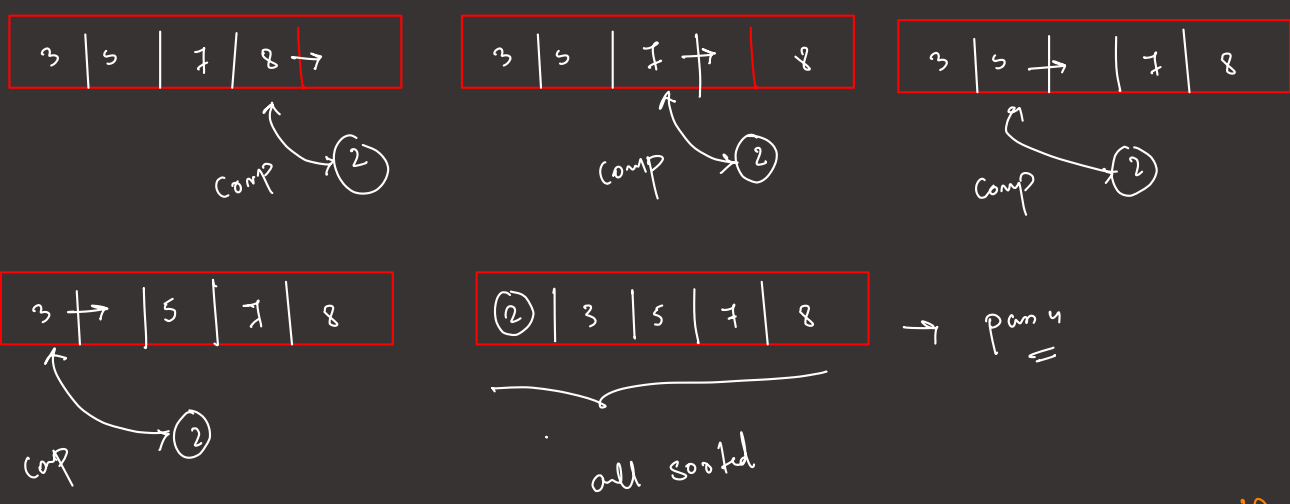
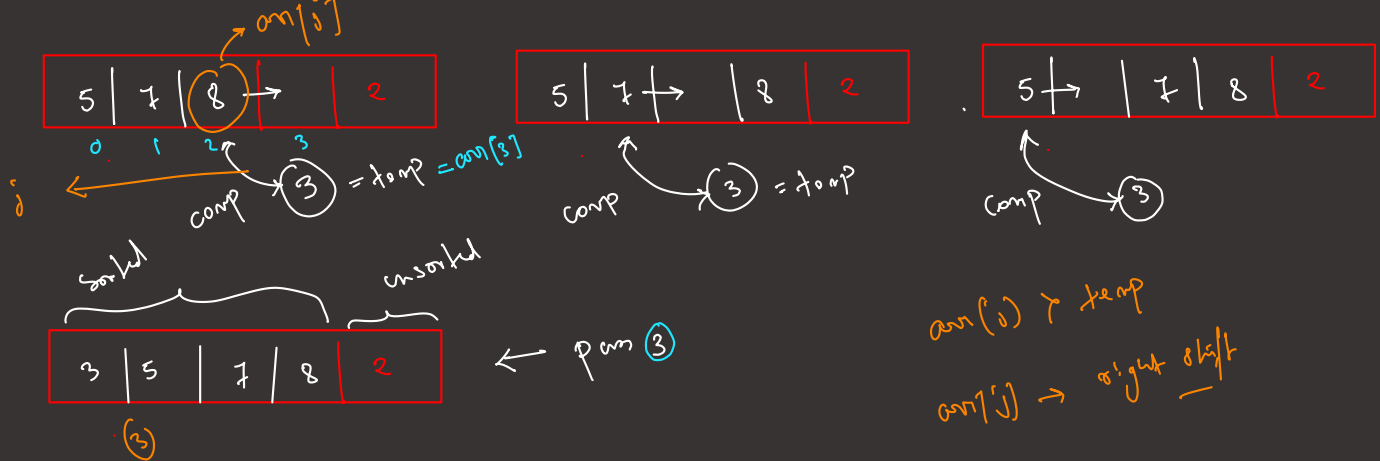
comp  $\rightarrow$  7

← pass 1



pass 2

$O(n \log n)$   
 $\downarrow$   
 $\approx O(n^2)$   
 $\downarrow$   
 $\uparrow$  bc =  $O(n^2)$  (count sort)

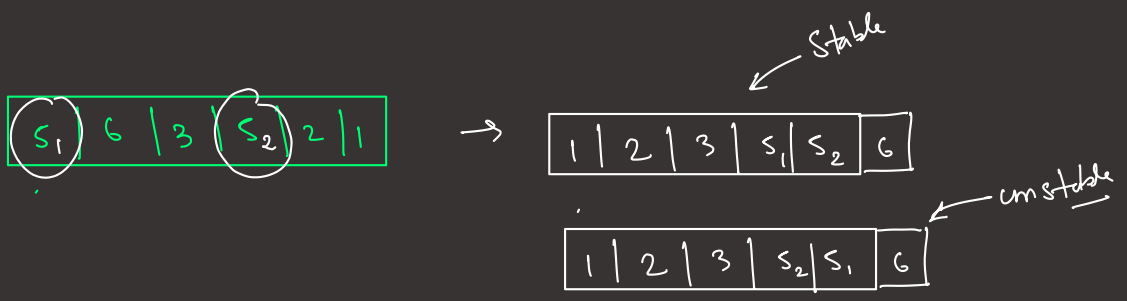


$\# \text{ pass} = (n-1)$   
 $\# \text{ comp} = 1 + 2 + 3 + \dots + (n-1) = \frac{n(n-1)}{2}$   
 $\text{max } \# \text{ swap} = \frac{n(n-1)}{2}$

time comp  $\propto O(n^2)$

Selection sort  $\rightarrow$  Adaptive  $\rightarrow O(n)$

Stability  
[Relative position will be maintained]



Selection sort is also stable.

