

Find Max. or Min Subarray Sum

MaxSum = $-\infty$

brute force Approach
 $O.C = O(n^3)$
 MaxSum = $-\infty$

for (int i = 0 to n) {
 for (int j = i to n) {

sum = 0;

for (k = i to j) {

sum \rightarrow (i, j)

}

MaxSum = max (MaxSum, sum);

}

}

return MaxSum;

for (i = 0 to n)
 for (j = i to n) {
 sum = 0

for (k = i to j) {

sum = sum + arr[k] (i to j)

MaxSum = max (MaxSum, sum)

$-\infty = \text{Integer.MIN_VALUE}$

Approach 2 : Prefix Sum Method, $O.C = O(n^2)$

arr =

1	-2	6	-1	3
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if i = 0
 $\text{sum}(i, i) = \text{sum}(0, 0) = \text{prefix}[0]$

$\text{sum}(i, i) = \text{prefix}[i] - \text{prefix}[i-1]$

$\text{sum}(1, 3) = \text{prefix}[3] - \text{prefix}[0]$
 $= 9 - 1 = 8$

$\left[\text{sum}(2, 4) = \text{sum}(0, 4) - \text{sum}(0, 1) \right]$
 \downarrow
 $\text{prefix}[4]$

sum(0, 2) \downarrow
 sum(0, 4) = prefix[4]
 \downarrow
 prefix =

1	-1	5	4	7
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 0 1 2 3 4
 \downarrow
 $\text{prefix}[i] = \text{sum up to } i^{\text{th}} \text{ element of arr}$
 $= \text{sum}(0, i) \leftarrow \text{sum of element 0 to } i$

① calculate prefix Array.

② for (int i = 0 to n)
 for (j = i to n)

$\text{sum}(i, j) = \text{prefix}[j] - \text{prefix}[i-1]$

H.W find for min sub-array sum

Approach 3

Kadane's Algo $O(n) = O(n)$

-2	-3	4	-1	-2	1	5	-3
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CS	0	0	4	3	1	2	7	4
MS	0	0	4	4	4	4	7	7

CS	-2	-3	4	3	1	2	7	4
MS	-2	-2	4	4	4	4	7	7

$$CS = \max(arr[i], CS + arr[i])$$

i=1 $CS = \max(-3, -2 + -3) = -3$

i=2 $CS = \max(4, -3 + 4) = 4$
 $CS = \max(4, 1) = 4$

i=3 $CS = \max(-1, -1 + 4) = 3$
 $CS = \max(-1, 3) = 3$

min + Max
 $-ve + +ve = +ve$
 $+ve + -ve = +ve \downarrow \uparrow +ve$

$$\left\{ \begin{array}{l} \text{sum} < 0 \\ CS = 0 \\ MS = \max(MS, CS) \end{array} \right\}$$

Qs Buy and sell stocks

prices = [7, 1, 5, 3, 6, 4]

buy at index 1, sell at index 4

profit = 6 - 1 = 5

profit = prices[i] - buying price

> 0 ↑
 < 0 ↓

buy price = ∞, profit = 0

for (int i = 0 to n)?

if (BP < prices[i])

profit = prices[i] - B.P. // day's profit.

max profit = max(max profit, today's profit);

i=2, 3 - 1 = 2
 today's profit = 2
 profit(2, 4)

BP = ∞, P = 0

i=0, Today's profit = 7 - ∞ = -∞
 buy price = 7

i=1, 1 - 7 = -6
 buy price = 1, P = 0

i=2, 5 - 1 = 4
 today's profit = 4
 max profit(0, 4) = 4

else {
 buying price = prices[i];
}

max profit = 4

