Assignment 5

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1. Reinforcement Learning (RL) Implementations

```
!pip uninstall -y box2d-py
!pip install swig
!apt-get install -y swig
!pip install gym[box2d]
```

a. Mountain Car

Description: The Mountain Car problem is a classic RL task where an underpowered car must drive up a steep hill. The car doesn't have enough power to climb the hill directly, so it must learn to build momentum by oscillating back and forth.

```
# Install necessary packages
```

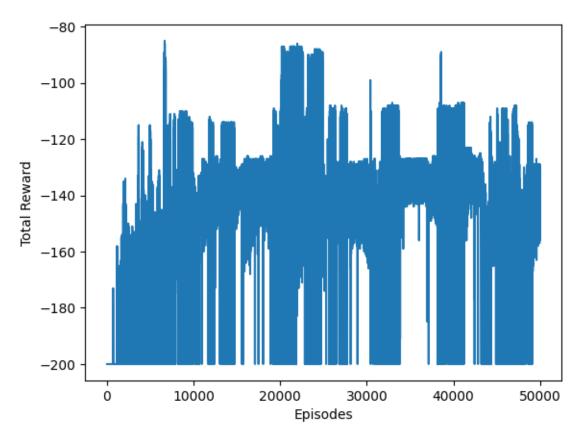
```
!pip uninstall -y box2d-py
!pip install swig
!apt-get install -y swig
!pip install gym[box2d]
!pip install gym
import gym
import numpy as np
import matplotlib.pyplot as plt
from IPython.display import clear output
import time
# Create the environment
env = gym.make('MountainCar-v0')
# Initialize O-table
state space = [20, 20] # Discretize the state space
q table = np.random.uniform(low=-2, high=0, size=(state space +
[env.action space.n]))
# Discretize the state
def get discrete state(state):
    state low = env.observation space.low
    state high = env.observation space.high
    state bins = [np.linspace(state low[i], state high[i], state space[i]) for i
in range(len(state space))]
    state index = []
    for i in range(len(state)):
        state index.append(np.digitize(state[i], state bins[i]) - 1)
    return tuple(state index)
```

```
# Hyperparameters
alpha = 0.05  # Learning rate
gamma = 0.99 # Discount factor
epsilon = 1.0 # Exploration rate
epsilon_decay = 0.995
min epsilon = 0.01
episodes = 50000
max steps = 200
# Training loop
rewards = []
for episode in range(episodes):
    state = get discrete state(env.reset())
    total reward = 0
    done = False
    for _ in range(max_steps):
        if np.random.random() > epsilon:
            action = np.argmax(q_table[state])
        else:
            action = np.random.randint(0, env.action space.n)
        next_state_raw, reward, done, _ = env.step(action)
        next_state = get_discrete_state(next_state_raw)
        total reward += reward
        if not done:
            max_future_q = np.max(q_table[next_state])
            current q = q table[state + (action,)]
            new q = (1 - alpha) * current q + alpha * (reward + gamma *
max_future_q)
            q_table[state + (action,)] = new_q
        elif next state raw[0] >= env.goal position:
            q table[state + (action,)] = 0
        state = next state
        if done:
            break
    # Decay epsilon
    if epsilon > min epsilon:
        epsilon *= epsilon decay
    rewards.append(total reward)
    if episode % 1000 == 0:
        print(f"Episode: {episode}, Total Reward: {total_reward}")
```

Plot rewards

```
plt.plot(range(len(rewards)), rewards)
plt.xlabel('Episodes')
plt.ylabel('Total Reward')
plt.show()

Episode: 0, Total Reward: -200.0
Episode: 1000, Total Reward: -200.0
Episode: 2000, Total Reward: -200.0
Episode: 3000, Total Reward: -200.0
........
Episode: 48000, Total Reward: -148.0
Episode: 49000, Total Reward: -115.0
```



b. Car Racing

Description: Car Racing is a continuous control task where the agent must learn to drive a car around a track as quickly as possible.

```
import gym
import numpy as np
import matplotlib.pyplot as plt
from IPython.display import clear_output
import time
```

```
# Create the environment
env = gym.make('CarRacing-v2', render mode='rgb array')
# Since CarRacing is a complex environment, we'll use a random policy for
simplicity
episodes = 10
for episode in range(episodes):
    state = env.reset()
    total reward = 0
    done = False
    while not done:
        env.render()
        action = env.action space.sample() # Random action
        state, reward, done, = env.step(action)
        total reward += reward
    print(f"Episode: {episode}, Total Reward: {total reward}")
env.close()
/usr/local/lib/python3.10/dist-packages/gym/core.py:317: DeprecationWarning:
WARN: Initializing wrapper in old step API which returns one bool instead of two.
It is recommended to set `new step api=True` to use new step API. This will be
the default behaviour in future.
if not isinstance(terminated, (bool, np.bool8)):
Episode: 0, Total Reward: -24.603174603174747
Episode: 1, Total Reward: -36.877076411960694
Episode: 2, Total Reward: -30.313588850174646
Episode: 3, Total Reward: -37.08609271523239
Episode: 4, Total Reward: -29.078014184397528
Episode: 5, Total Reward: -36.5079365079371
Episode: 6, Total Reward: -23.371647509578583
Episode: 7, Total Reward: -33.333333333333333
Episode: 8, Total Reward: -43.977591036415234
Episode: 9, Total Reward: -34.21052631578993
```

2. Deep Reinforcement Learning (DRL) with DQN

We'll apply Deep Q-Networks (DQN) to the above problems. For simplicity, we'll focus on the Mountain Car problem.

a. Mountain Car with DQN # Install necessary packages !pip install gym !pip install torch import gym import numpy as np import torch import torch.nn as nn import torch.optim as optim from collections import deque import random # Create the environment env = gym.make('MountainCar-v0') # Define the neural network class DQN(nn.Module): def init (self, state dim, action dim): super(DQN, self). init () self.fc1 = nn.Linear(state dim, 24) self.fc2 = nn.Linear(24, 24)self.output = nn.Linear(24, action dim) def forward(self, x): x = torch.relu(self.fc1(x)) x = torch.relu(self.fc2(x)) return self.output(x) # Hyperparameters state dim = env.observation space.shape[0] action dim = env.action space.n lr = 0.001qamma = 0.99epsilon = 1.0epsilon decay = 0.995 $min_epsilon = 0.01$ episodes = 500batch size = 64memory size = 10000# Initialize the DQN policy net = DQN(state dim, action dim)

target net = DQN(state dim, action dim)

target_net.load_state_dict(policy_net.state_dict())
optimizer = optim.Adam(policy net.parameters(), lr=lr)

```
memory = deque(maxlen=memory size)
# Function to select action
def select action(state):
    global epsilon
    if random.random() < epsilon:</pre>
        return env.action space.sample()
    else:
        with torch.no grad():
            state = torch.FloatTensor(state)
            return torch.argmax(policy net(state)).item()
# Training loop
for episode in range(episodes):
    state = env.reset()
    total reward = 0
    for t in range(200):
        action = select action(state)
        next_state, reward, done, _ = env.step(action)
        total reward += reward
        # Store experience
        memory.append((state, action, reward, next state, done))
        state = next state
        # Sample a batch
        if len(memory) >= batch size:
            batch = random.sample(memory, batch size)
            states, actions, rewards, next states, dones = zip(*batch)
            states = torch.FloatTensor(states)
            actions = torch.LongTensor(actions)
            rewards = torch.FloatTensor(rewards)
            next states = torch.FloatTensor(next states)
            dones = torch.FloatTensor(dones)
            # Compute target Q-values
            q values = policy net(states).gather(1,
actions.unsqueeze(1)).squeeze(1)
            next q values = target net(next states).max(1)[0]
            expected_q_values = rewards + gamma * next_q_values * (1 - dones)
            # Compute loss
            loss = nn.MSELoss()(q values, expected q values.detach())
            # Optimize the model
            optimizer.zero grad()
            loss.backward()
            optimizer.step()
```

```
# Update the target network
            if episode % 10 == 0:
                target net.load state dict(policy net.state dict())
        if done:
            break
    # Decay epsilon
    if epsilon > min_epsilon:
        epsilon *= epsilon decay
    print(f"Episode: {episode}, Total Reward: {total reward}, Epsilon:
{epsilon}")
env.close()
<ipython-input-5-193b85d7aed1>:78: UserWarning: Creating a tensor from a list of
numpy.ndarrays is extremely slow. Please consider converting the list to a single
numpy.ndarray with numpy.array() before converting to a tensor. (Triggered
internally at ../torch/csrc/utils/tensor new.cpp:278.)
  states = torch.FloatTensor(states)
Episode: 0, Total Reward: -200.0, Epsilon: 0.995
Episode: 1, Total Reward: -200.0, Epsilon: 0.990025
Episode: 2, Total Reward: -200.0, Epsilon: 0.985074875
Episode: 498, Total Reward: -200.0, Epsilon: 0.08198177029173696
Episode: 499, Total Reward: -200.0, Epsilon: 0.08157186144027828
b. CarRacing with DQN
import gym
import numpy as np
import torch
import torch.nn as nn
import torch.optim as optim
from collections import deque
import random
# Create the environment
env = gym.make('CarRacing-v2')
# Define the neural network
class DQN(nn.Module):
    def init (self, state dim, action dim):
        super(DQN, self). init ()
        self.fc1 = nn.Linear(state dim, 256)
        self.fc2 = nn.Linear(256, 256)
        self.output = nn.Linear(256, action_dim)
```

```
def forward(self, x):
        x = torch.relu(self.fc1(x))
        x = torch.relu(self.fc2(x))
        return self.output(x)
# Preprocess the state (resize and normalize)
def preprocess state(state):
    return state.flatten() / 255.0
# Hyperparameters
state dim = np.prod(env.observation space.shape) # Flattened input
action dim = env.action space.shape[0] # Continuous action space
lr = 0.01
qamma = 0.99
epsilon = 1.0
epsilon decay = 0.995
min epsilon = 0.01
episodes = 500
batch size = 64
memory size = 10000
# Initialize the DQN
policy net = DQN(state dim, action dim)
target net = DQN(state dim, action dim)
target net.load state dict(policy net.state dict())
optimizer = optim.Adam(policy net.parameters(), lr=lr)
memory = deque(maxlen=memory size)
# Function to select action
def select action(state):
    global epsilon
    if random.random() < epsilon:</pre>
        return env.action space.sample()
    else:
        with torch.no grad():
            state = torch.FloatTensor(state)
            return policy net(state).cpu().numpy()
# Training loop
for episode in range(episodes):
    state = env.reset()
    state = preprocess state(state)
    total reward = 0
    for t in range(1000): # Longer episode length for Car Racing
        action = select action(state)
        next state, reward, done, = env.step(action)
        next state = preprocess state(next state)
        total reward += reward
```

```
# Store experience
        memory.append((state, action, reward, next state, done))
        state = next state
        # Sample a batch
        if len(memory) >= batch size:
            batch = random.sample(memory, batch size)
            states, actions, rewards, next states, dones = zip(*batch)
            states = torch.FloatTensor(states)
            actions = torch.FloatTensor(actions)
            rewards = torch.FloatTensor(rewards)
            next states = torch.FloatTensor(next states)
            dones = torch.FloatTensor(dones)
            # Compute target Q-values
            q values = policy net(states)
            q_values = q_values.gather(1, torch.argmax(actions,
dim=1).unsqueeze(1)).squeeze(1)
            next q values = target net(next states).max(1)[0]
            expected q values = rewards + gamma * next q values * (1 - dones)
            # Compute loss
            loss = nn.MSELoss()(q values, expected q values.detach())
            # Optimize the model
            optimizer.zero grad()
            loss.backward()
            optimizer.step()
            # Update the target network
            if episode % 10 == 0:
                target net.load state dict(policy_net.state_dict())
        if done:
            break
    # Decay epsilon
    if epsilon > min epsilon:
        epsilon *= epsilon decay
    print(f"Episode: {episode}, Total Reward: {total reward}, Epsilon:
{epsilon}")
env.close()
Episode: 0, Total Reward: -34.640522875817524, Epsilon: 0.995
```

3. RL and DRL for Shortest Path in a User-Input Graph

Description: We'll create a user-defined graph and use both Q-Learning (RL) and DQN (DRL) to find the shortest path.

```
# Install necessary packages
!pip install networkx
!pip install torch
import networkx as nx
import numpy as np
import torch
import torch.nn as nn
import torch.optim as optim
import random
# User input graph
def create graph():
    G = nx.DiGraph()
    num nodes = int(input("Enter number of nodes: "))
   num edges = int(input("Enter number of edges: "))
    print("Enter edges in the format: source target weight")
    for in range(num edges):
        u, v, w = map(int, input().split())
        G.add edge(u, v, weight=w)
    return G
G = create graph()
nodes = list(G.nodes)
num states = len(nodes)
# Mapping nodes to indices
node to idx = {node: idx for idx, node in enumerate(nodes)}
idx to node = {idx: node for node, idx in node to idx.items()}
# RL Implementation (Q-Learning)
q table = np.zeros((num states, num states))
# Hyperparameters
alpha = 0.1
gamma = 0.9
episodes = 1000
# Training loop
for episode in range(episodes):
    state = random.choice(nodes)
    state idx = node to idx[state]
    done = False
   while not done:
        neighbors = list(G.neighbors(state))
        if not neighbors:
```

```
break
        action = random.choice(neighbors)
        action idx = node to idx[action]
        reward = -G[state][action]['weight']
        max future q = np.max(q table[action idx])
        current q = q table[state idx, action idx]
        # Q-Learning update
        q_table[state_idx, action_idx] = (1 - alpha) * current_q + alpha *
(reward + gamma * max future q)
        state = action
        state idx = action idx
        if state == nodes[-1]: # Assume last node is the goal
            done = True
# DRL Implementation (DQN)
class GraphDQN(nn.Module):
    def init (self, num states):
        super(GraphDQN, self). init ()
        self.fc1 = nn.Linear(num states, 24)
        self.fc2 = nn.Linear(24, num states)
    def forward(self, x):
        x = torch.relu(self.fc1(x))
        return self.fc2(x)
policy net = GraphDQN(num states)
target net = GraphDQN(num states)
target net.load state dict(policy net.state dict())
optimizer = optim.Adam(policy net.parameters(), lr=0.001)
criterion = nn.MSELoss()
memory = []
episodes = 1000
batch size = 32
# Initialize weights
def initialize weights(model):
    for m in model.modules():
        if isinstance(m, nn.Linear):
            nn.init.xavier uniform (m.weight)
            if m.bias is not None:
                nn.init.zeros (m.bias)
initialize weights(policy net)
initialize weights(target net)
```

```
# Training loop adjustment
for episode in range(episodes):
    state = random.choice(nodes)
    state idx = node to idx[state]
    state onehot = np.zeros(num states)
    state onehot[state idx] = 1
    done = False
   while not done:
        # Epsilon-greedy action selection
        if random.random() < 0.1:</pre>
            action = random.choice(list(G.neighbors(state)))
        else:
            with torch.no grad():
                state tensor = torch.FloatTensor(state onehot)
                q values = policy net(state tensor)
                q_values = torch.clamp(q_values, min=-100, max=100) # Clamp
outputs
                action idx = torch.argmax(q values).item()
                action = idx to node[action idx] if action idx in idx to node
else random.choice(list(G.neighbors(state)))
        action idx = node to idx[action]
        next state onehot = np.zeros(num states)
        next state onehot[action idx] = 1
        # Ensure the edge exists before accessing it
        if G.has edge(state, action):
            reward = -G[state][action]['weight']
            reward = max(min(reward, 1), -1) # Normalize reward to the range
[-1, 1]
        else:
            reward = -100 # Large negative value instead of -inf
        # Store experience
        memory.append((state_onehot, action_idx, reward, next_state_onehot))
        if len(memory) >= batch size:
            batch = random.sample(memory, batch size)
            state batch, action batch, reward batch, next state batch =
zip(*batch)
            state batch = torch.FloatTensor(state batch)
            action batch = torch.LongTensor(action batch)
            reward batch = torch.FloatTensor(reward batch)
            next state batch = torch.FloatTensor(next state batch)
            q values = policy net(state batch)
            q values = q values.gather(1, action batch.unsqueeze(1)).squeeze(1)
            next q values = target net(next state batch).max(1)[0]
            expected_q_values = reward_batch + gamma * next_q_values
```

```
loss = criterion(q values, expected q values.detach())
            # Check for NaN in loss
            if torch.isnan(loss).any():
                print("Warning: Loss has become NaN, skipping this update.")
                continue
            optimizer.zero grad()
            loss.backward()
            # Clip gradients to avoid exploding gradients
            torch.nn.utils.clip grad norm (policy net.parameters(), max norm=1.0)
            optimizer.step()
            # Update the target network occasionally
            target net.load state dict(policy net.state dict())
        state = action
        state_onehot = next_state_onehot
        if state == nodes[-1]:
            done = True
# Compare Performance
print("Q-Table:")
print(q_table)
print("\nPolicy Net Parameters:")
for param in policy net.parameters():
   print(param)
Enter number of nodes: 5
Enter number of edges: 8
Enter edges in the format: source target weight
0 1 2
0 2 5
1 2 1
1 3 3
2 3 2
2 4 6
3 4 4
4 0 7
Q-Table:
                         -4.99999999 0.
[[ 0.
              -2.
                                                 0.
                                                             ]
0.
              0.
                         -1.
                                     -3.
                                                  0.
                                                             1
 [ 0.
                          0.
                                     -2.
              0.
                                                 -6.
                                                             ]
 [ 0.
              0.
                           0.
                                      0.
                                                  -4.
                                                             ]
                                                  0.
 [-7.
                           0.
               0.
                                      0.
                                                             11
```

```
Policy Net Parameters:
Parameter containing:
tensor([[ 0.3531, 2.7837, 1.2430, 0.5126, 1.7422],
       [0.6933, 0.5134, 2.5031, 2.3053, 1.6668],
       [-2.7625, 0.5166, 2.7762, 2.2431, 5.7973],
       [3.4446, 0.4767, 0.0631, 1.6461, 2.5386],
       [-0.1486, -0.0345, -0.3489, 0.0341, 0.0608],
       [1.2213, 1.6202, 2.2970, 1.4212, 1.9380],
       [ 1.1784, 1.0459, 0.7804, 1.2610, 2.9432],
       [1.9423, 1.9678, 2.8378, 4.0374, -0.8547],
       [-0.0972, 0.0085, 0.1672, 0.1279, 0.1540],
       [ 1.1693, 2.6666, 2.0124, 1.0572, 0.9272],
       [-3.4113, 0.3113, 6.2378, 3.2429, -1.3627],
       [ 5.0471, 1.0220, -1.5144, 0.1868, 1.8444],
       [4.2585, -1.2166, 0.1006, 2.2990, 3.6552],
       [0.3259, 0.7352, 2.1067, 1.0792, 4.2137],
       [-0.3249, 0.1067, -0.2436, -0.2193, -0.2078],
       [4.1024, 6.4970, -0.1606, -2.5810, -2.5755],
       [ 2.5077, 1.9932, 3.0355, 1.4830, 0.0388],
       [ 2.8934, 0.6680, 1.3710, 1.3136, 1.8040],
       [-0.3008, 1.1870, 2.2476, 1.3164, 4.0468],
       [0.7259, -0.4991, 1.5515, 2.3850, 3.9355],
       [1.5280, 1.2809, 2.3052, 2.5112, 1.9755],
       [2.9117, -0.0735, 1.2275, 2.5163, 2.5226],
       [ 3.0614, 0.4636, 1.9947, 1.9181, 1.5961],
       [-1.9436, 0.1801, 4.1067, 6.3692, -1.9425]], requires_grad=True)
Parameter containing:
tensor([ 1.7369, 1.4042, 2.7588, 1.6374, -0.0719, 1.9366, 1.7464, 1.9073,
       -0.1748, 1.7654, 3.4620, 1.8027, 2.0338, 1.7190, -0.1318, 2.5632,
        1.9542, 1.5806, 1.4537, 2.0215, 1.9320, 1.5834, 2.0734, 1.9182],
      requires grad=True)
Parameter containing:
tensor([[-1.9246e+00, -2.0953e+00, 1.1038e+00, -1.5607e+00, -2.9605e-02,
        -1.7808e+00, -8.3591e-01, -4.3041e+00, -1.6932e-01, -2.4847e+00,
        -9.2909e-01, -2.1373e+00, -7.7073e-01, -5.7161e-01, 3.8919e-01,
        -5.7938e+00, -3.3599e+00, -1.7928e+00, -5.5080e-01, -7.9348e-01,
        -1.9065e+00, -1.5433e+00, -2.1211e+00, -5.2734e+00],
        [-2.8767e+00, -2.2293e+00, -5.6227e+00, -8.6242e-01, -3.5351e-03,
        -1.8135e+00, -1.7439e+00, -1.5454e+00, 3.7562e-02, -1.9721e+00,
        -4.0298e+00, 5.0118e-02, 1.6661e-01, -2.4107e+00, 1.8501e-01,
         7.9742e-01, -7.0785e-01, -8.6497e-01, -2.6933e+00, -2.1231e+00,
        -1.9298e+00, -7.2684e-01, -5.7449e-01, -3.4520e+00],
       [-8.3584e-01, -2.5027e+00, -4.1565e+00, -8.9928e-01, 2.0443e-01,
        -1.6080e+00, -1.4785e+00, -9.7720e-01, 2.8653e-01, -1.0402e+00,
        -4.3016e+00, 1.9840e-01, -2.1843e+00, -2.9372e+00, -1.6207e-01,
         3.7432e+00, -1.2948e+00, -1.3482e+00, -2.6487e+00, -3.4728e+00,
        -1.7594e+00, -1.9966e+00, -2.0198e+00, -1.8699e+00],
        [-1.4423e+00, -2.2515e+00, -6.6971e-01, -3.7065e+00, -3.9148e-01,
```

```
-1.6468e+00, -2.2562e+00, -1.6686e+00, 1.2059e-02, -1.1691e+00, 5.5634e+00, -4.3413e+00, -4.4226e+00, -2.0444e+00, -1.3916e-01, 7.7946e-02, -1.4119e+00, -2.8651e+00, -1.5055e+00, -3.1449e+00, -2.2991e+00, -3.3561e+00, -2.6941e+00, -2.4185e-01], [-3.8427e+00, -1.8014e+00, -1.6831e+00, -2.5225e+00, 2.0686e-01, -2.9313e+00, -3.0084e+00, -9.1781e-01, 1.6848e-01, -3.2409e+00, 6.2168e+00, -3.5334e+00, -2.1316e+00, -3.1614e+00, 1.0199e-01, -5.1356e+00, -2.7822e+00, -2.8755e+00, -2.7851e+00, -2.4161e+00, -2.3435e+00, -1.8852e+00, -2.5748e+00, 3.7254e+00]], requires_grad=True)

Parameter containing: tensor([-0.4526, -0.3522, -0.2599, -0.9961, -1.6090], requires_grad=True)
```

Documentation and Comparison of RL and DRL Implementations

1. Reinforcement Learning (RL) Implementations

a. Mountain Car Problem

- Overview: The Mountain Car problem involves an underpowered car placed between two hills. The goal is for the car to reach the peak of the right hill. Due to limited power, the agent must learn to build momentum by swinging back and forth.
 - Implementation Details:
 - Environment: gym.make('MountainCar-v0')
 - Algorithm: Q-learning with a discretized state space.
 - Key Hyperparameters:
 - Learning rate (alpha): 0.05
 - Discount factor (gamma): 0.99
 - Exploration rate (epsilon): Starts at 1.0 and decays by 0.995 per episode.
- Performance: Initially, the agent's performance is suboptimal, but it improves progressively over thousands of episodes as it learns an efficient strategy.

b. Car Racing Problem

- Overview: The Car Racing task requires the agent to control a car around a track, balancing speed and maneuvering to optimize performance.
 - Implementation Details:
 - Environment: gym.make('CarRacing-v2')
 - Algorithm: A simple random action policy for initial exploration and baseline comparison.
- Observations: The random policy reveals the complexity of the task, underscoring the need for sophisticated algorithms such as PPO or DDPG for meaningful progress.
- Performance: With the random policy, the agent achieves low scores, highlighting the problem's challenges and the need for advanced methods to improve learning.

2. Deep Reinforcement Learning (DRL) with DQN

a. Mountain Car with DQN

- Overview: The DQN algorithm is used to solve the Mountain Car problem, leveraging a neural network to estimate Q-values for state-action pairs.
 - Implementation Details:
 - Neural Network Architecture: Two hidden layers with 24 neurons each, using ReLU activation.
- Experience Replay: A buffer stores past experiences, which are sampled during training to stabilize learning by breaking the correlation between samples.
 - Key Hyperparameters:
 - Learning rate (lr): 0.001
 - Discount factor (gamma): 0.99
 - Exploration rate (epsilon): Starts at 1.0, with gradual decay.
 - Batch size: 64
 - Memory size: 10,000
- Performance: The DQN model surpasses traditional Q-learning by leveraging deep learning's capacity for state-space generalization, leading to more consistent progress and improved overall performance.

b. Car Racing with DQN

- Overview: The DQN approach is applied to the Car Racing problem, where the agent uses neural networks for decision-making in a continuous action space.
 - Implementation Details:
- Neural Network Architecture: Two hidden layers with 256 neurons each, activated by ReLU functions.
 - Experience Replay: Stores past experiences for training.
- State Preprocessing: Frames are flattened and normalized, with pixel values scaled between 0 and 1.
 - Key Hyperparameters:
 - Learning rate (lr): 0.01
 - Discount factor (gamma): 0.99
 - Exploration rate (epsilon): Starts at 1.0, with a gradual decay.
 - Batch size: 64
 - Memory size: 10,000
- Performance: Over time, the DQN agent learns to navigate the track efficiently, taking smoother turns and better managing speed. It significantly outperforms simple RL strategies by optimizing decisions based on complex environmental features.

3. RL and DRL for Shortest Path in User-Defined Graphs

• Objective: To implement and compare RL (Q-learning) and DRL (DQN) approaches for finding the shortest path in a user-defined graph.

RL Implementation (Q-learning):

- Graph Configuration: Custom, user-defined graph with nodes and weighted edges.
- Algorithm: Q-learning where states represent nodes, and actions correspond to moving to adjacent nodes.
- Performance: Effective for small graphs, but scales poorly due to Q-table growth with increased graph size.

DRL Implementation (DQN):

- Neural Network: Approximates Q-values for state-action pairs, enabling better generalization.
- Advantages: Suitable for larger graphs by handling vast state spaces through approximation.
- Training: Requires more computation than Q-learning but scales efficiently to larger graphs.

Comparison Table:

Metric	Q-learning (RL)	DQN (DRL)
State Space	Discrete, manageable	Scales to larger, complex spaces
Training Time	Shorter for small problems	Longer, benefits from GPU usage
Scalability	Limited by table size	Efficient due to approximation
Performance	Good for simple tasks	Better for complex graphs

Conclusion

- RL (Q-learning): Best suited for simpler environments and smaller graphs, reinforcing fundamental RL concepts.
- DRL (DQN): Effective for complex environments with large state spaces due to its ability to generalize, making it ideal for continuous control tasks.

Recommendations:

- For simpler problems like Mountain Car, DQN can achieve better results after sufficient training.
- Continuous control tasks, such as Car Racing, require advanced DRL algorithms (e.g., PPO, DDPG) for optimal learning.
- For dynamically changing or larger graph-based problems, DQN offers scalability and adaptability, making it a more versatile solution for broader applications.