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%% Get longest paths starting from each graph-node and get insights thereof

% Recursive function to build longest paths
function longestPaths = recursive(G, longestPaths, numLongestPaths)

% Find if successors present of current longest path(s)
successorsLogical = zeros(1, numLongestPaths); % Initialize array containing
logical values for presence of successors

for inLongestPaths = 1:numLongestPaths % Iterate through every longest path

    endNode = longestPaths{inLongestPaths}(end); % Extract last node in current
longest path

    successorsList = successors(G, endNode); % Extract all successors of last
node

    haveSuccessor = ~isempty(successorsList); % Check if successors of last node
present

    successorsLogical(inLongestPaths) = haveSuccessor; % Update status of
successor(s) presence

end

pathsToUpdate = find(successorsLogical == 1); % Logical 1 for longest paths with
end node successors

% Add successors to current longest paths
if any(successorsLogical) % For successor(s) present for any longest path

    % Prevent further recursion if each last node of every path has only one
successor that's same as last node
    sameSuccessorArray = zeros(1, length(longestPaths)); % Initialize array to
store logical value for same successor

    for inLongestPaths = 1:length(longestPaths) % Iterate through every longest
path

        path = longestPaths{inLongestPaths}; % Extract current longest path

        successorNodes = successors(G, path(end)); % Extract successor(s) of the
last node

        numNodeSuccessors = length(successorNodes); % Store number of successors

        if numNodeSuccessors == 1 & successorNodes(1) == path(end) % For the
only successor matching with last node

            sameSuccessorArray(inLongestPaths) = 1; % Update same successor
status for current path in array

        end
    end
end

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end

if all(sameSuccessorArray) % For all longest paths having a single successor
same as path's last node

    return % Return control outside recursive function (to invoking function)

else

    % Do nothing

end

newLongestPaths = {}; % Initialize cell to store updated longest paths

for inPathsToUpdate = 1:length(pathsToUpdate) % Iterate through each longest
path having end node successor(s)

    pathIndex = pathsToUpdate(inPathsToUpdate); % Extract index of path
having successor(s) to last node

    path = longestPaths{pathIndex}; % Extract path with successor

    pathEnd = path(end); % Extract last node in path

    nodeSuccessors = successors(G, pathEnd); % Extract successors of last
node

    for inNodeSuccessors = 1:length(nodeSuccessors) % Iterate through array
of end node-successors

        currentSuccessorNode = nodeSuccessors(inNodeSuccessors); % Extract
current successor among all successors

        if ~ismember(currentSuccessorNode, path) % For current successor not
already present in path (to avoid network loops)

            newLongestPaths{end + 1} = [path, currentSuccessorNode]; % Add
successor to current path and add updated path to new longest paths array

        else

            continue % Choose next successor node in successors array

        end

    end

end

end

if ~isempty(newLongestPaths) % For new successor not already present in
path, variable will not be empty

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    longestPaths = {}; % Empty longest paths array to repopulate it

    longestPaths = newLongestPaths; % Refill longest paths array

end

    numLongestPaths = length(longestPaths); % Assign updated number of longest
paths to include as argument in recursive function

    % Recursive function call to find successors of current longest path(s)
    longestPaths = recursive(G, longestPaths, numLongestPaths); % Add new path-
end successors recursively

elseif ~any(successorsLogical) % For no successor present for any longest path

    disp(['returning control because no successors for', num2str(longestPaths{1}
(1))]);
    return % Return control outside recursive function (to invoking function)

end

end

% Number of initial states (64)
numStates = numnodes(G);

% Function to find longest paths from each node
function longestPathsCell = findLongestPaths(G, numStates)

% Initialize nodes array
allNodes = 1:numStates;

% Initialize variable to store number of longest paths
numLongestPaths = 1; % Only longest path comprises only source node (initially)

% Display description
disp('Longest paths starting from each graph-node:');

% Paths for each initial state (node)
for whichNode = 1:numStates % Iterate through all nodes

    % Extract node
    node = allNodes(whichNode);

    % Reset longest paths variable for current node
    longestPaths = {node};

    % Invoke recursive function to find longest path
    longestPathsCell{node} = recursive(G, longestPaths, numLongestPaths);

end

end

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% Measure time to execute block
tic % Start time-keeping

% Store longest paths starting from each initial state
longestPathsCell = findLongestPaths(G, numStates); % Generate cell array to
store longest paths

for inLongestPathsCell = 1:length(longestPathsCell) % Iterate through longest
paths cells for every initial state

    disp(longestPathsCell{inLongestPathsCell}); % Extract and display all
longest paths of current initial state

end

disp('Time taken to obtain longest paths:'); % Display measured time

toc % End time-keeping

%%

% Number of occurrences of each graph-node across all longest paths
counts = zeros(1, numStates); % Values in dictionary to store number of node
occurrences

countsDictionary = dictionary(1:numStates, counts); % Initialize dictionary to
store number of node occurrences

for inLongestPathsCell = 1:length(longestPathsCell) % Iterate through longest
paths cells for every node

    longestPaths = longestPathsCell{inLongestPathsCell}; % Extract longest paths
corresponding to current node

    for inEachColumn = 1:length(longestPaths) % Iterate through longest paths
corresponding to current node

        currentPath = longestPaths{inEachColumn}; % Extract current longest path
for current node

            FPofPath = currentPath(end); % Extract FP at the end of path

            for inCurrentPath = 1:length(currentPath) % Iterate through every node
in current longest path

                element = currentPath(inCurrentPath); % Extract current node ID

                countsDictionary(element) = countsDictionary(element) + 1; % Update
number of occurrences corresponding to current node ID

            end

        end

    end

end

```

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end
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```
% Display dictionary storing number of occurrences corresponding to each node  
disp('Graph-nodes and their corresponding number of occurrences across all  
longest paths:');  
disp(countsDictionary);
```

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%%
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% Across longest paths, visualize frequency of number of graph-nodes vs. number  
of occurrences
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counts = values(countsDictionary); % Extract number of occurrences from  
dictionary storing counts
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edges = 1:max(counts); % Define bin edges for histogram
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% Plot histogram
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disp('How many graph-nodes vs. how many times they occur:');  
histogram_plot = histogram(counts, edges);  
ylabel("# graph-nodes in bin", "FontName", "Helvetica", "FontAngle", "normal",  
"FontWeight", "normal");  
xlabel("# graph-node occurrences", "FontName", "Helvetica", "FontAngle",  
"normal", "FontWeight", "normal");
```

Output:

Longest paths starting from each graph-node:

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{[1 48 36 52 20]}
```

```
{[2 52 20]}
```

```
{[3 48 36 52 20]}
```

```
{[4 52 20]}
```

```
{[5 61 45]}
```

```
{[6 54]}
```

```
{[7 59 28 20]}
```

```
{[8 22 54]}    {[8 52 20]}
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{[9 39 29 37 61 45]} {[9 39 29 53 61 45]} {[9 55 13 37 61 45]} {[9 55 13 53 61 45]}
{[9 55 29 37 61 45]} {[9 55 29 53 61 45]}

{[10 39 29 37 61 45]} {[10 39 29 53 61 45]} {[10 55 13 37 61 45]} {[10 55 13 53 61 45]}
{[10 55 29 37 61 45]} {[10 55 29 53 61 45]}

{[11 39 29 37 61 45]} {[11 39 29 53 61 45]} {[11 55 13 37 61 45]} {[11 55 13 53 61 45]}
{[11 55 29 37 61 45]} {[11 55 29 53 61 45]}

{[12 39 29 37 61 45]} {[12 39 29 53 61 45]} {[12 55 13 37 61 45]} {[12 55 13 53 61 45]}
{[12 55 29 37 61 45]} {[12 55 29 53 61 45]}

{[13 37 61 45]} {[13 53 61 45]}

{[14 37 61 45]} {[14 53 61 45]}

{[15 35 48 36 52 20]}

{[16 35 48 36 52 20]}

{[17 46 38 54]} {[17 62 38 54]}

{[18 52 20]}

{[19 20]}

{[20]}

{[21 61 45]}

{[22 54]}

{[23 22 54]} {[23 61 45]}

{[24 22 54]}

{[25 37 61 45]} {[25 46 38 54]} {[25 53 61 45]} {[25 62 38 54]}

{[26 37 61 45]} {[26 53 61 45]}

{[27 20]}

{[28 20]}

{[29 37 61 45]} {[29 53 61 45]}

{[30 37 61 45]} {[30 53 61 45]}

{[31 3 48 36 52 20]} {[31 35 48 36 52 20]}

{[32 3 48 36 52 20]} {[32 35 48 36 52 20]}

{[33 48 36 52 20]}

{[34 52 20]}

{[35 48 36 52 20]}

{[36 52 20]}

{[37 61 45]}

{[38 54]}

{[39 29 37 61 45]} {[39 29 53 61 45]}

$\{[40 \ 22 \ 54]\}$ $\{[40 \ 52 \ 20]\}$

$\{[41 \ 48 \ 36 \ 52 \ 20]\}$

$\{[42 \ 24 \ 22 \ 54]\}$ $\{[42 \ 40 \ 22 \ 54]\}$ $\{[42 \ 40 \ 52 \ 20]\}$ $\{[42 \ 56 \ 22 \ 54]\}$

$\{[43 \ 48 \ 36 \ 52 \ 20]\}$

$\{[44 \ 24 \ 22 \ 54]\}$ $\{[44 \ 40 \ 22 \ 54]\}$ $\{[44 \ 40 \ 52 \ 20]\}$ $\{[44 \ 56 \ 22 \ 54]\}$

$\{[45]\}$

$\{[46 \ 38 \ 54]\}$

$\{[47 \ 45]\}$

$\{[48 \ 36 \ 52 \ 20]\}$

$\{[49 \ 46 \ 38 \ 54]\}$ $\{[49 \ 62 \ 38 \ 54]\}$

$\{[50 \ 52 \ 20]\}$

$\{[51 \ 28 \ 20]\}$

$\{[52 \ 20]\}$

$\{[53 \ 61 \ 45]\}$

$\{[54]\}$

$\{[55 \ 13 \ 37 \ 61 \ 45]\}$ $\{[55 \ 13 \ 53 \ 61 \ 45]\}$ $\{[55 \ 29 \ 37 \ 61 \ 45]\}$ $\{[55 \ 29 \ 53 \ 61 \ 45]\}$

{[56 22 54]}

{[57 46 38 54]} {[57 62 38 54]}

{[58 38 54]} {[58 52 20]} {[58 61 45]}

{[59 28 20]}

{[60 20]}

{[61 45]}

{[62 38 54]}

{[63 3 48 36 52 20]}

{[64 3 48 36 52 20]}

Time taken to obtain longest paths:

Elapsed time is 0.126948 seconds.

Graph-nodes and their corresponding number of occurrences across all longest paths:

1 1

2 1

3 5

4 1

5 1

6 1

7 1

8 2

9 6

10 6
11 6
12 6
13 12
14 2
15 1
16 1
17 2
18 1
19 1
20 35
21 1
22 12
23 2
24 3
25 4
26 2
27 1
28 4
29 22
30 2
31 2
32 2
33 1
34 1
35 5
36 16
37 22
38 12
39 10
40 6
41 1

42 4
43 1
44 4
45 51
46 5
47 1
48 15
49 2
50 1
51 1
52 27
53 22
54 26
55 20
56 3
57 2
58 3
59 2
60 1
61 49
62 5
63 1
64 1

How many graph-nodes vs. how many times they occur:

