

Practical Exercise 2

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Der Code ist zusätzlich als Datei einsehbar.

a)

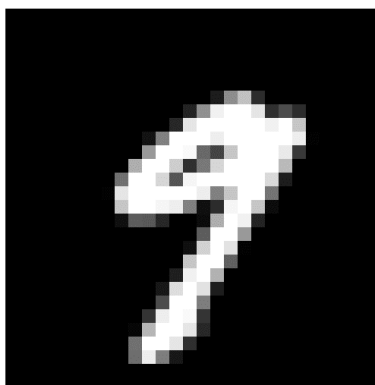
Code:

```
#Exercise 2
# Task a

load("digit0.mat")

% function to show a certain amount of images (im_num) for each digit
function show_data(im_num)
    for j= 0:9
        s=strcat("digit",int2str(j),".mat");
        load(s)
        for i = 1:im_num
            I = D(i,:);
            I = reshape(I, [28,28]); % converts I to size to 28 x 28
            I=imrotate(I,270); % rotates I by 270 degrees
            figure(1), imshow(flipplr(I),[]); % shows flipped I
            pause(0.1); % pauses for 0.1 seconds
        end
    end
endfunction
```

Die Funktion erzeugt wie gefordert im_num Beispielbilder für jede Ziffer. Ruft man die Funktion mit im_num = 5 auf und wartet bis das letzte Beispielbild angezeigt wird, wird folgendes angezeigt:



b)

Code:

```
load("digit2.mat")

# Task b, Calculating the mean

Sum= zeros(1,784);
s_D= size(D,1);
for im_num= 1: s_D
    for i=1:784
        I = D(im_num,:);
        Sum(i) = Sum(i) + I(i); % adds the value of the pixel i in picture im_num to the sum of values of pixel i
    end
end

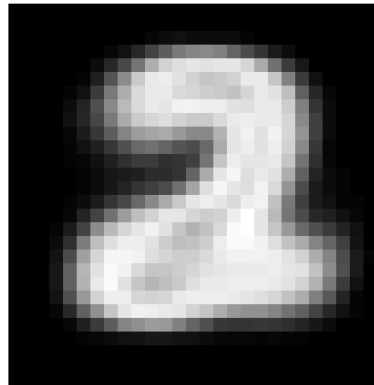
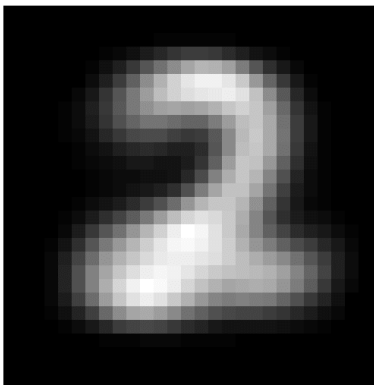
Avg=Sum/s_D; % divides the sums by the number of images
I = reshape(Avg, [28,28]); % converts I to size to 28 x 28
I = imrotate(I,270);
figure(1), imshow(fliplr(I),[]);

# Calculating the variance
SumDev= zeros(1,784);
for im_num= 1: s_D
    for i=1:784
        I = D(im_num,:);
        SumDev(i) = SumDev(i)+((I(i)-Avg(i))^2); % adds the square of the value of pixel i minus the mean to the sum
    end
end

Var=SumDev/s_D; % divides the sums by the number of pictures

I = reshape(Var, [28,28]); % converts I to size to 28 x 28
I=imrotate(I,270);
figure(2), imshow(fliplr(I),[]);
```

Es werden die folgenden Bilder ausgegeben (links Figure 1, rechts Figure 2):



c) und d)

Code:

```
#Task c and d

load("digit3.mat")
s_D = size(D,1); % number of images
k = 1; % index of the figures
m_x = 0:255;

Pixel = [297,155,203,210,217,399,410,595,605,715]; % 10 interesting pixel

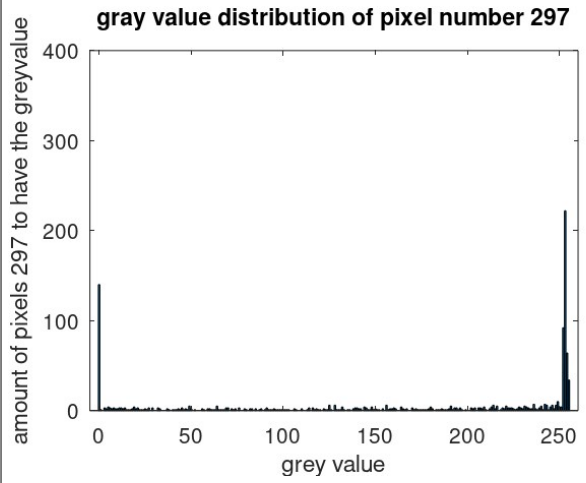
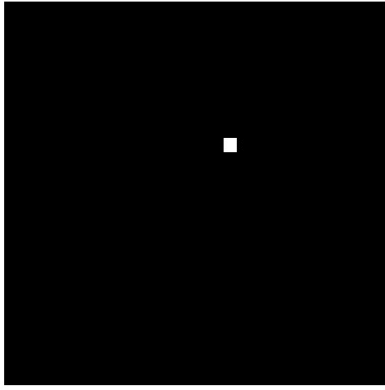
for j = 1:10
    p = Pixel(j);
    M = zeros(1,256);
    P = zeros(1,784);
    P(p) = 255; % changes the value at the given pixel p to 255

    for im_num= 1: s_D
        I = D(im_num,:);
        i=I(p)+1;
        M(i)=M(i)+1; % M(i) counts the number of images with value i-1 at pixel p
    end

    P = reshape(P, [28,28]); % converts P to size to 28 x 28
    P=imrotate(P,270);
    figure(k); imshow(flipplr(P),[]);

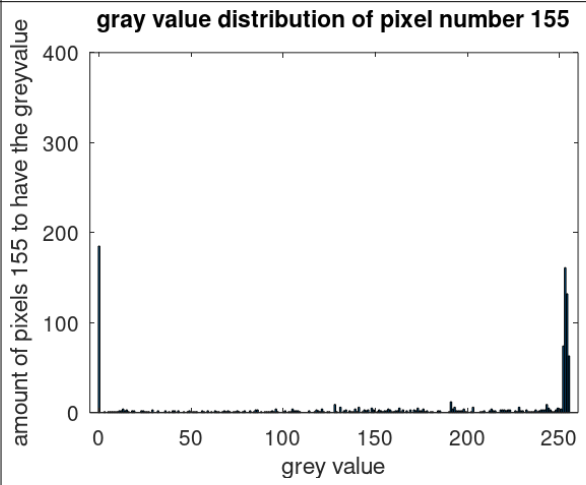
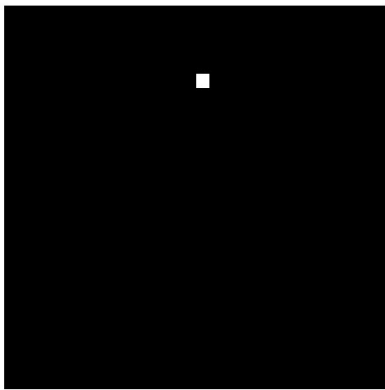
    figure(k+1);
    bar(m_x,M)
    t = strcat("gray value distribution of pixel number ", int2str(p));
    title(t);
    axis([-5, 260, 0, 400]);
    xlabel ('grey value');
    y = strcat("amount of pixels ", int2str(p) , " to have the greyvalue");
    ylabel(y);
    k = k+2
end
```

Es werden folgende Bilder ausgegeben:



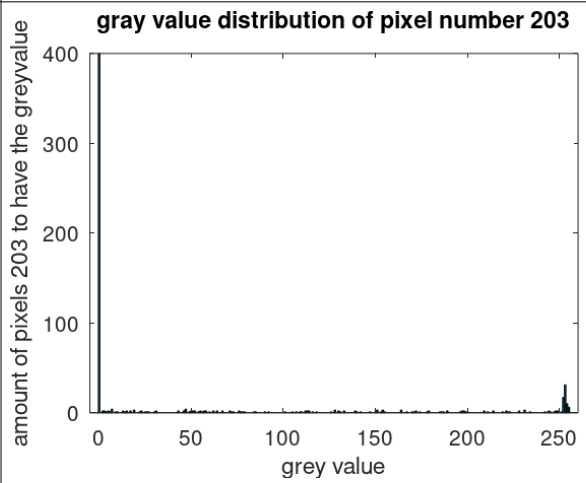
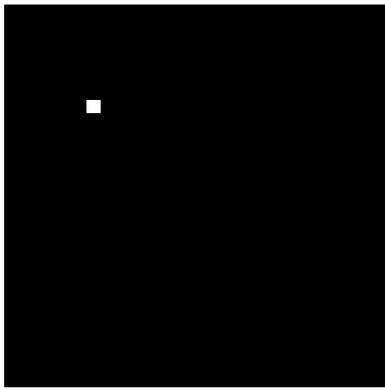
1

2



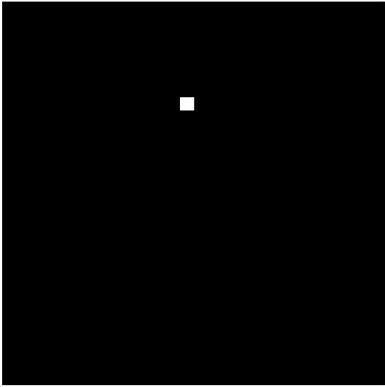
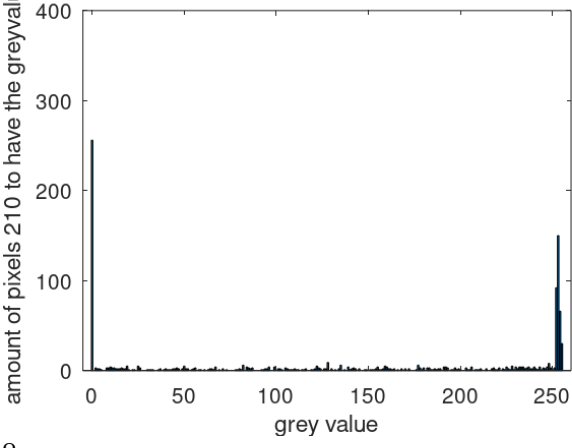
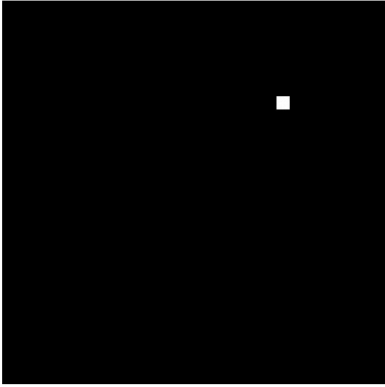
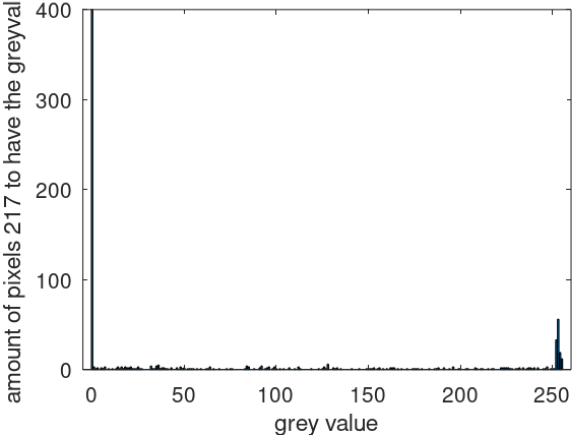
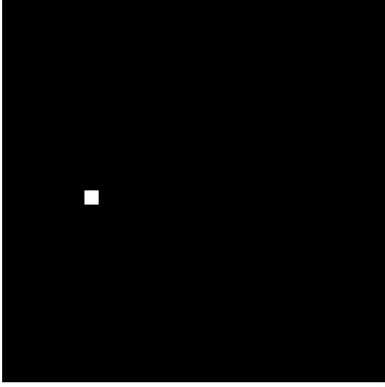
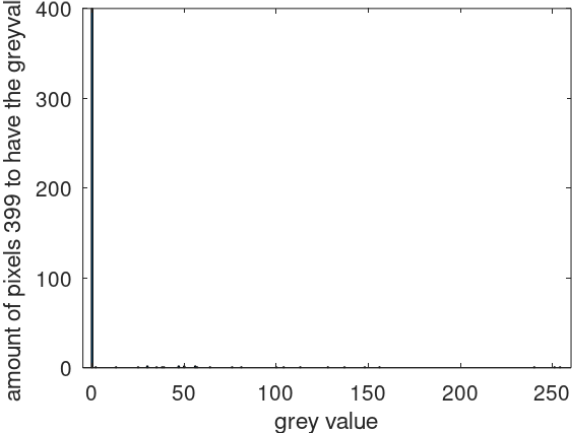
3

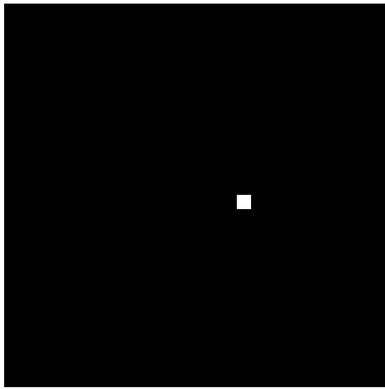
4



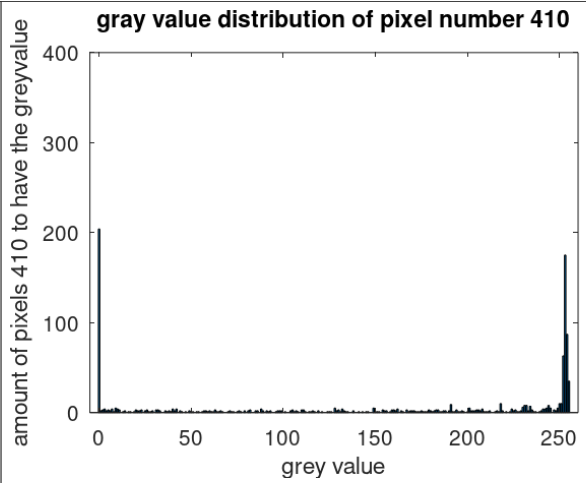
5

6

<p>7</p> 	<p>gray value distribution of pixel number 210</p> 
<p>9</p> 	<p>gray value distribution of pixel number 217</p> 
<p>11</p> 	<p>gray value distribution of pixel number 399</p> 



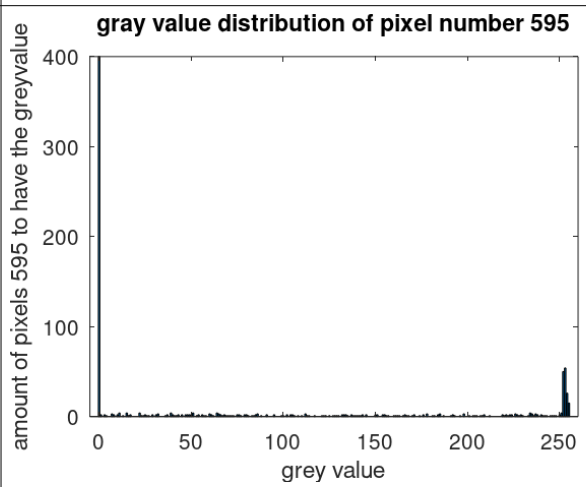
13



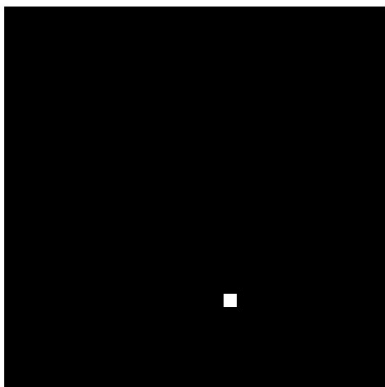
14



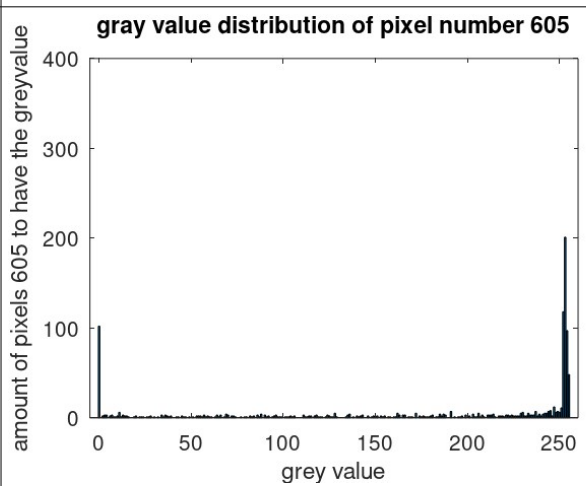
15



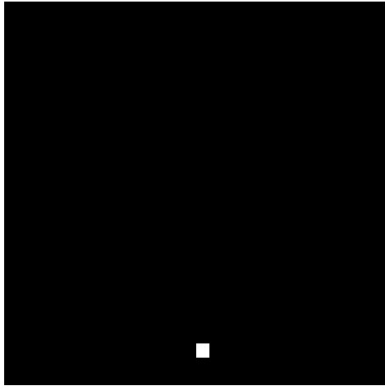
16



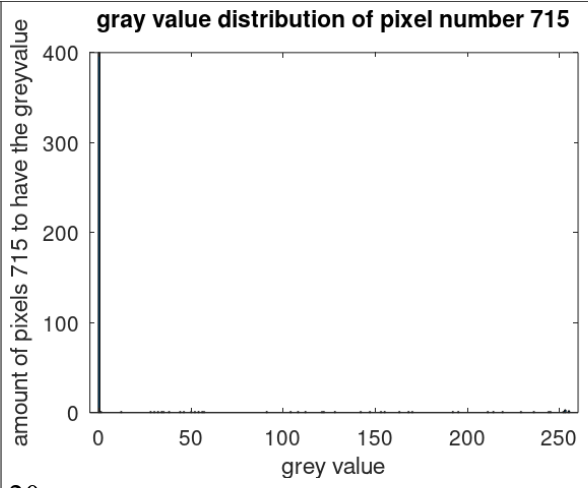
17



18



19



20

e)

Code:

```
#Task e

C=[];
function show_correlation (dig, xb, yb)

    s = strcat("digit", int2str(dig), ".mat");
    load(s)

    b_value= 28*(yb-1)+xb;
    base= rot90(D(:,b_value)); % extracting the grey values of each image for base pixel

    C=[];

    for i=1: 784
        pixel = rot90(D(:,i)); % extracting the grey values of each image for pixel i
        c = corr(pixel,base); % correlation between pixel i and base pixel
        c=(c+1)*255/2; % converting correlation to grey value
        C=[C,c]; % building vector of grey values for correlation image
    end

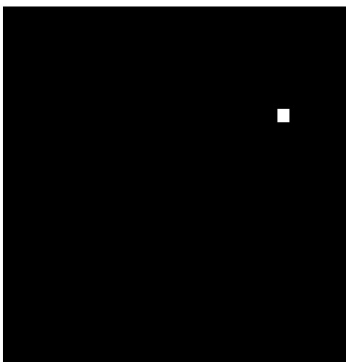
    P = zeros(1,784);
    P(b_value)=255;

    P = reshape(P, [28,28]); % converts P to size 28 x 28
    P=imrotate(P,270);
    figure(1); imshow(flipplr(P),[]);

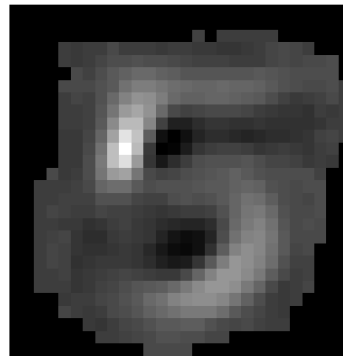
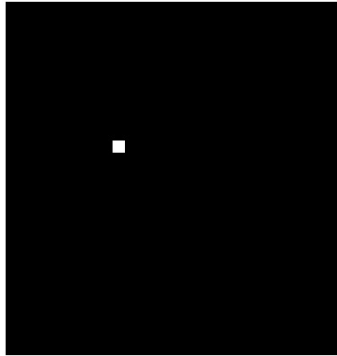
    C=reshape(C, [28,28]); % converts C to size to 28 x 28
    C = imrotate(C,270);
    figure(2), imshow(flipplr(C),[]);

endfunction
```

Der Aufruf show_correlation (2, 23, 9) erzeugt:



Für `show_correlation (5, 10, 12)` erhalten wir:



f)

Code:

```
#Task f

a=1;

function show_joint_probs(v_min, v_max, digit)
    s = strcat("digit",int2str(digit),".mat");
    load(s)
    size_D = size(D,1);
    P=[];

    for i=1:784
        pixel = rotdim(D(:,i));           % extracting the grey values of each image for pixel i
        pixel_max = pixel < v_max;
        pixel_min = pixel >=v_min;
        pixel_count = pixel_max & pixel_min;
        sum_p = sum(pixel_count);
        p = sum_p / size_D;               % the probabilite of pixel i having a grey value in the interval [v_min,v_max]
        P=[P,p];
    endfor

    P;
    p_min= min(P);
    p_max= max(P);
    range= p_max - p_min;
    G=[];

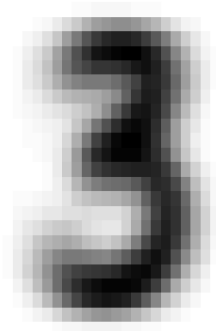
    % transforming the probabilities into grey values
    for i=1:784
        g=P(i);
        g=(g-p_min)*255/range;
        G=[G,g];
    endfor

    G = reshape(G, [28,28]); % converts G to size to 28 x 28
    G = imrotate(G,270);
    figure; imshow(flipplr(G),[]);

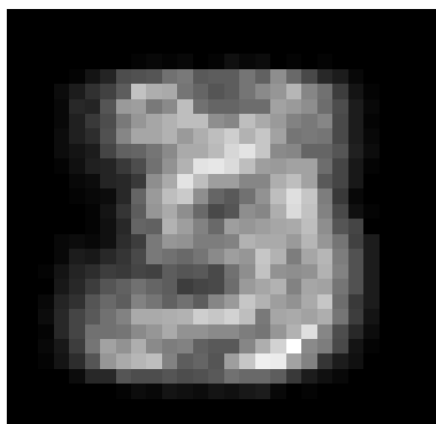
endfunction

show_joint_probs(0, 1,3)
show_joint_probs(1, 50,3)
show_joint_probs(50, 150,3)
show_joint_probs(250, 255,3)
```

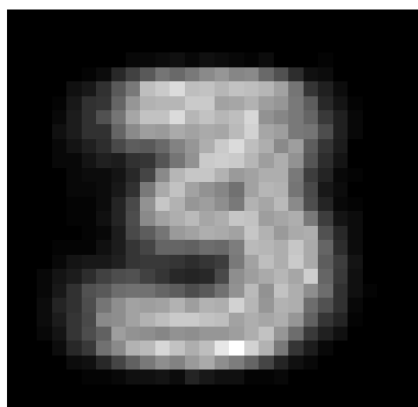
Wir erhalten für das Intervall $[0, 1[$ das Bild:



Wir erhalten für das Intervall $[1, 50]$ das Bild:



Wir erhalten für das Intervall $[50, 150]$ das Bild:



Wir erhalten für das Intervall $[250, 255]$ das Bild:

