



## Part 2.3: Visualization

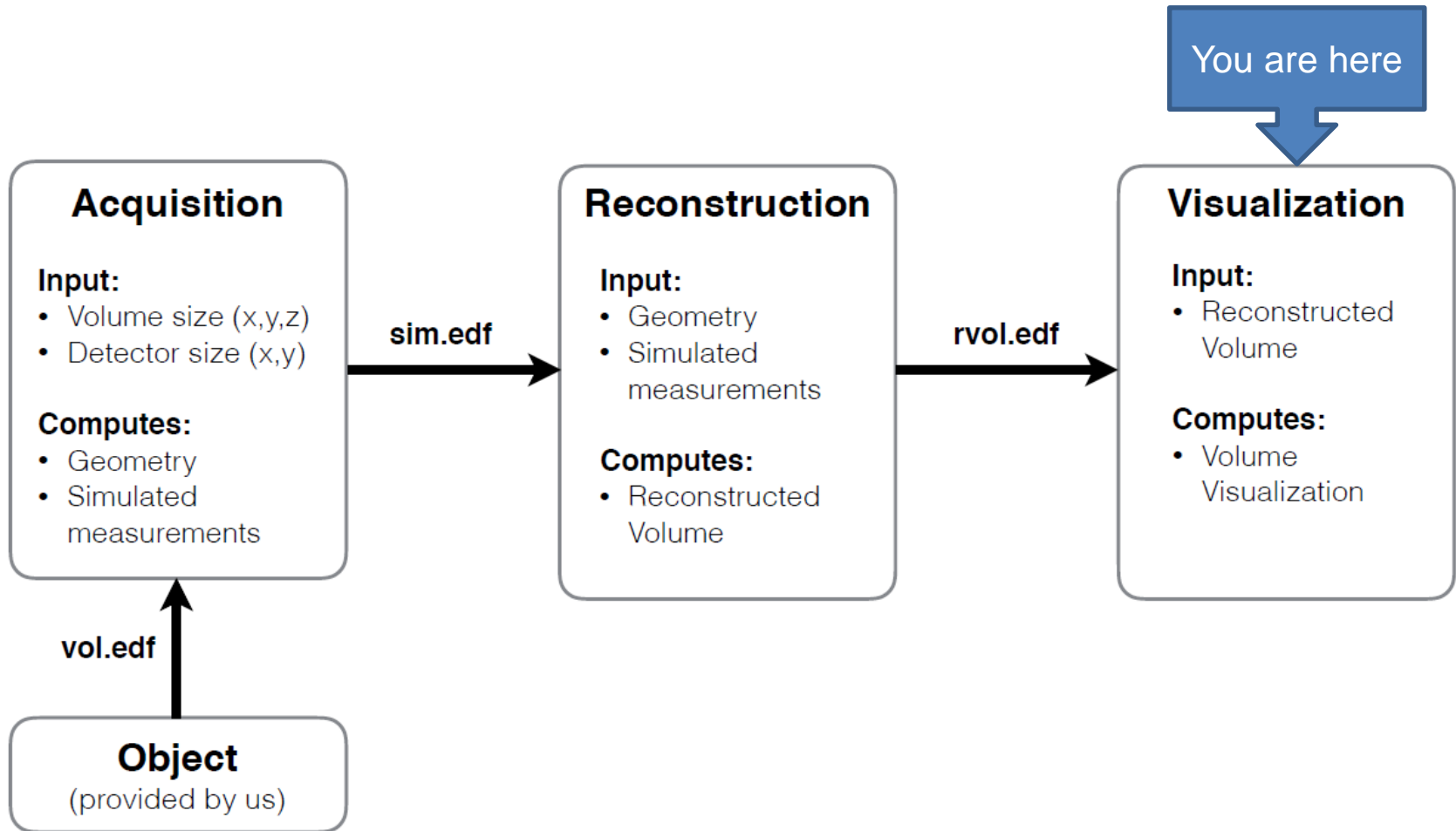
Jakob Weiss

Slides based on material by Christian Schulte zu Berge



# OVERVIEW

## Part 2 - Overview



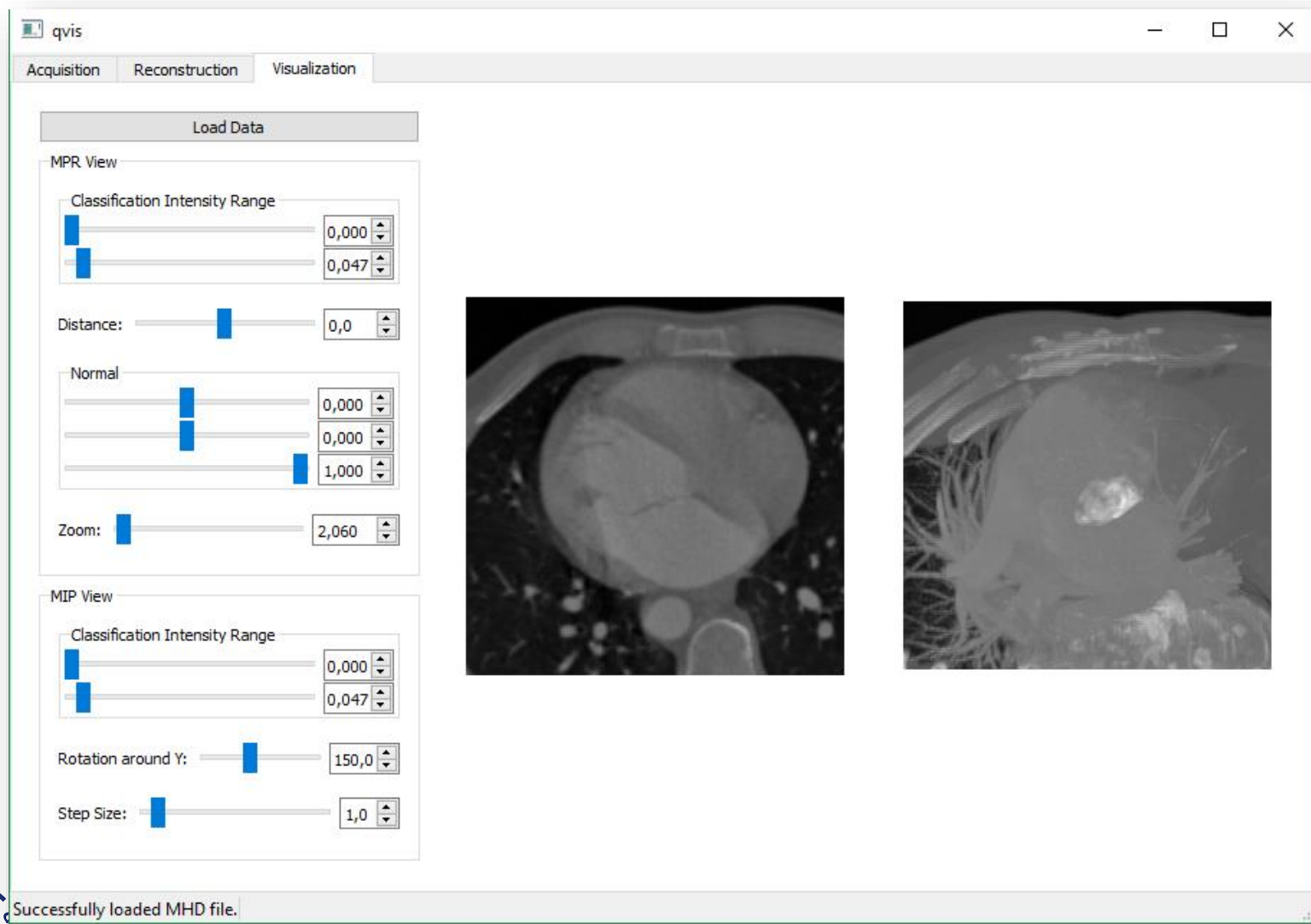
# Visualization Part

You will:

- Gain some background knowledge on Medical Visualization
- Learn some essential techniques:
  - Trilinear interpolation
  - Classification (transfer functions)
  - Slice visualization
  - Simple raycasting-based volume visualization
- Create your own volume visualization tool



# Example Application



# Disclaimer

- Today, most visualization techniques are implemented entirely on the GPU (e.g. OpenGL, DirectX, ...)
- However:
  - This is a C++ course, not a Computer Graphics course.
  - Everything will be implemented on the CPU.
  - ( ☹ )





# INTRODUCTION INTO VISUALIZATION

# Definition

## vi·su·al·ize<sup>1</sup>

- To form a mental image of; envisage
- To make visible

## McCormick et al.<sup>2</sup>

- „Visualization is a method of computing. It transforms the symbolic into the geometric, enabling researchers to observe their simulations and computations. Visualization offers a method for seeing the unseen.“



1. The American Heritage Dictionary of the English Language
2. Visualization in Scientific Computing, Computer Graphics 21(6), Nov 1987



# Disambiguation

## Computer Graphics $\leftrightarrow$ Visualization

- Both transform data into graphics/pictures
- CG: Focus on rendering, shading, texturing
- Vis: Focus on data abstraction and representation

## Further Differentiations

- Efficient algorithms (CG)  $\leftrightarrow$  Effective to use (Vis)
- Mapping image to abstract information (CV)  $\leftrightarrow$  Mapping information to image (Vis)
- Mapping data to data (IP)  $\leftrightarrow$  Mapping data to image (Vis)
- Perception Science  $\leftrightarrow$  Use this knowledge for better visualization (Vis)



# Data Characteristics

## Source

- Real world (measuring)  $\leftrightarrow$  Theory (simulation)  $\leftrightarrow$  Art (design, modelling)

## Domain

- Nominal  $\leftrightarrow$  Ordinal  $\leftrightarrow$  Discrete metric  $\leftrightarrow$  Continuous metric

## Dimensionality

- Scalar  $\leftrightarrow$  Vector  $\leftrightarrow$  Tensor  $\leftrightarrow$  Multivariate

## Structure

- Regular grid  $\leftrightarrow$  Scattered data



# Data Characteristics in our Application

## Source

- Real world (measuring) ↔ Theory (simulation) ↔ Art (design, modelling)

## Domain

- Nominal ↔ Ordinal ↔ Discrete metric ↔ Continuous metric

## Dimensionality

- Scalar ↔ Vector ↔ Tensor ↔ Multivariate

## Structure

- Regular grid ↔ Scattered data



# Visualization Techniques for Scalar Data

- Dimensionality matters:
    - 1D scalar field:  $\Omega \in \mathbb{R} \rightarrow \mathbb{R}$
    - 2D scalar field:  $\Omega \in \mathbb{R}^2 \rightarrow \mathbb{R}$
    - 3D scalar field:  $\Omega \in \mathbb{R}^3 \rightarrow \mathbb{R}$
  - Additional time domain?
    - E.g. 2D+t scalar field:  $\Omega \in \mathbb{R}^2 \times \mathbb{R} \rightarrow \mathbb{R}$
  - Basic strategies:
    - Mapping to geometry (Function plots, height fields, ...)
    - Mapping to color (Slice rendering, volume rendering)
- Visualization method depends heavily on data and application



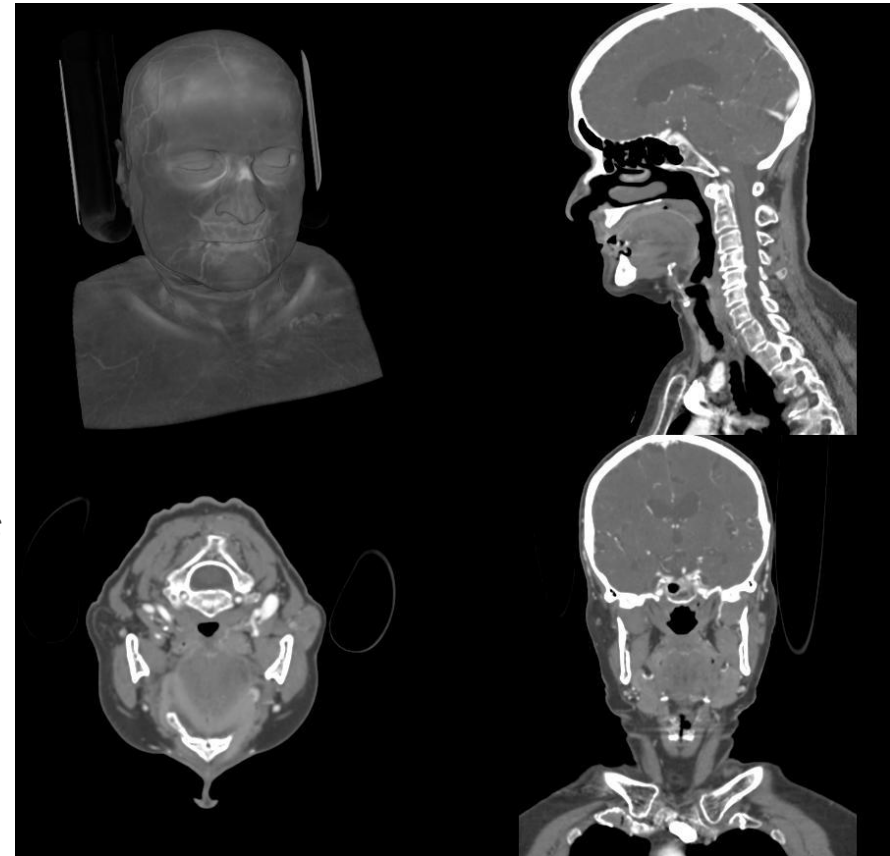
# Slice and Volume Visualization

Most medical data (CT, MRI, US, ...) has:

- Discrete metric data
- Scalar values
- Regular 2D/3D grid

Standard visualization techniques:

- 2D: Slice rendering
  - Axis aligned slice
  - Multi-planar reconstruction (MPR)
    - *Natively supported by today's GPUs*
- 3D: Volume rendering
  - Indirect Volume Rendering
    - *First, extract geometry, then, render geometry*
  - Direct Volume Rendering
    - *Directly project volume onto 2D screen by simulating physics of light transport*





# ESSENTIAL TECHNIQUE #1: TRILINEAR INTERPOLATION

# Interpolation

- Why do we need interpolation?
  - Image data has discrete representation: Voxel grid
  - Ray samples may lie between the voxels
- Nearest neighbor
  - Poor quality
- (Bi-/Tri-)Linear interpolation
  - Acceptable quality, fast implementation



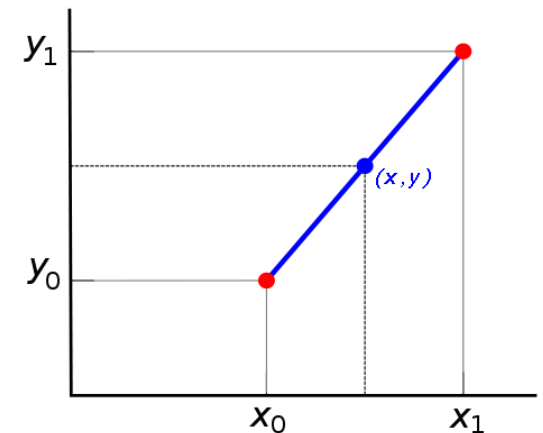
# Linear Interpolation

- Given two points  $(x_0, y_0)$ ,  $(x_1, y_1)$ , the following equation holds for any  $(x, y)$  on the straight line in between:

$$\frac{y - y_0}{x - x_0} = \frac{y_1 - y_0}{x_1 - x_0}$$

- Solving for  $y$  yields:

$$y = y_0 + (y_1 - y_0) \frac{x - x_0}{x_1 - x_0}$$



- We can generalize for any 1D function  $f$ :

$$f(x) \approx (1 - t)f(x_0) + tf(x_1), \quad t = \frac{x - x_0}{x_1 - x_0} \in [0, 1]$$



Image courtesy of: wikipedia.org



# Bilinear Interpolation

Extending this to 2D functions yields bilinear interpolation:

- First, perform two linear interpolations in  $x$  direction

$$f(R_1) \approx (1 - t_x)f(Q_{11}) + t_x f(Q_{21})$$

$$f(R_2) \approx (1 - t_x)f(Q_{12}) + t_x f(Q_{22})$$

- Then, perform interpolation in  $y$  direction

$$f(P) \approx (1 - t_y)f(R_1) + t_y f(R_2)$$

→ Three linear interpolations in total

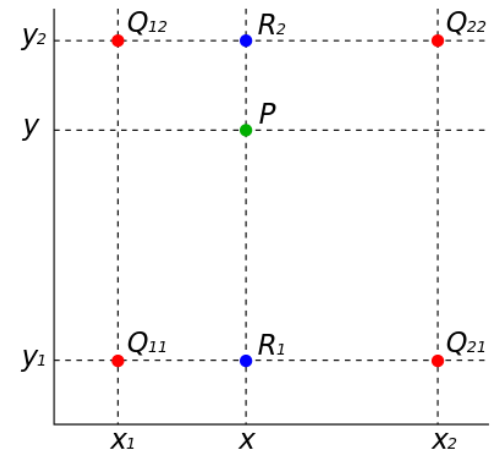


Image courtesy of: wikipedia.org

# Trilinear Interpolation

Extension to 3D functions yields trilinear interpolation:

- First, perform two bilinear interpolations in the  $xy$  plane to yield  $f(C_0)$  and  $f(C_1)$
- Then, perform interpolation in  $z$  direction

$$f(C) \approx (1 - t_z)f(C_0) + t_zf(C_1)$$

→ Seven linear interpolations in total

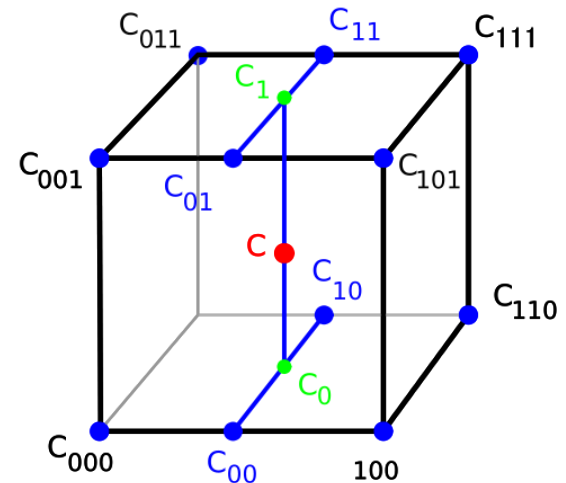


Image courtesy of: wikipedia.org



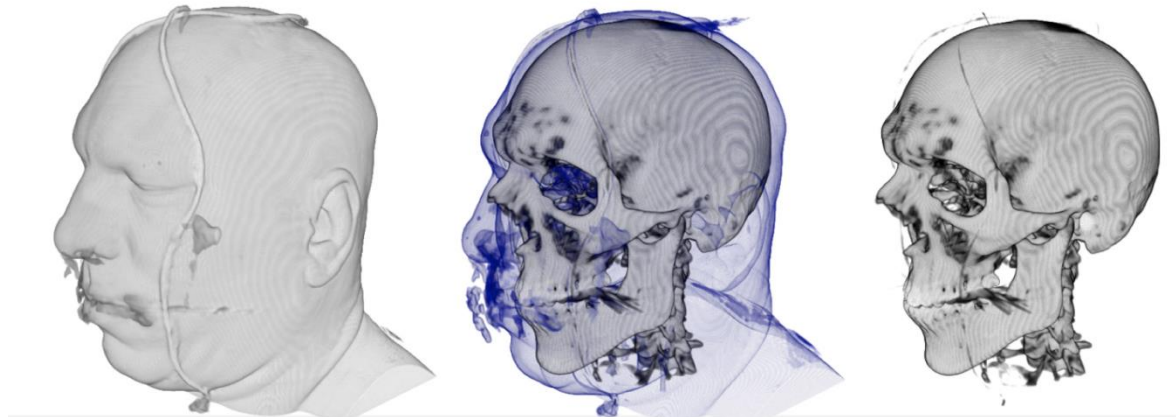
# ESSENTIAL TECHNIQUE #2: CLASSIFICATION / TRANSFER FUNCTIONS

# Slice and Volume Visualization: Classification

- Medical images usually only have scalar intensities as domain

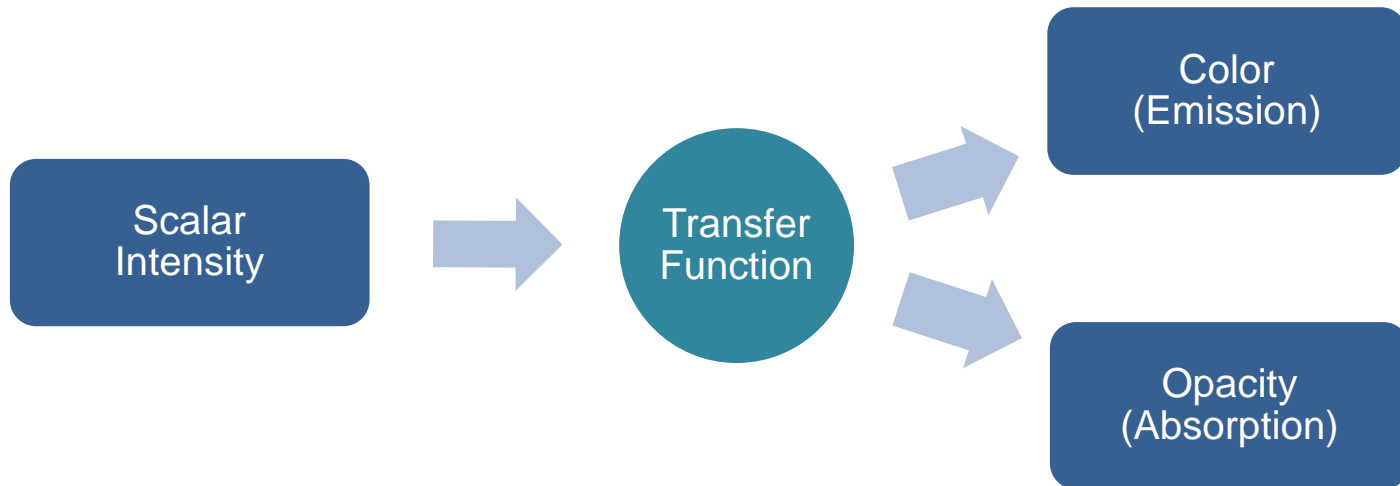


- How can we define the look of the data?

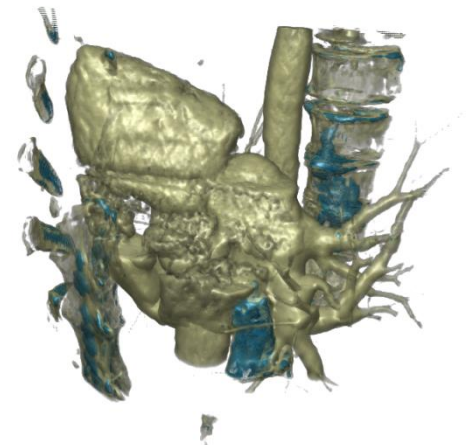
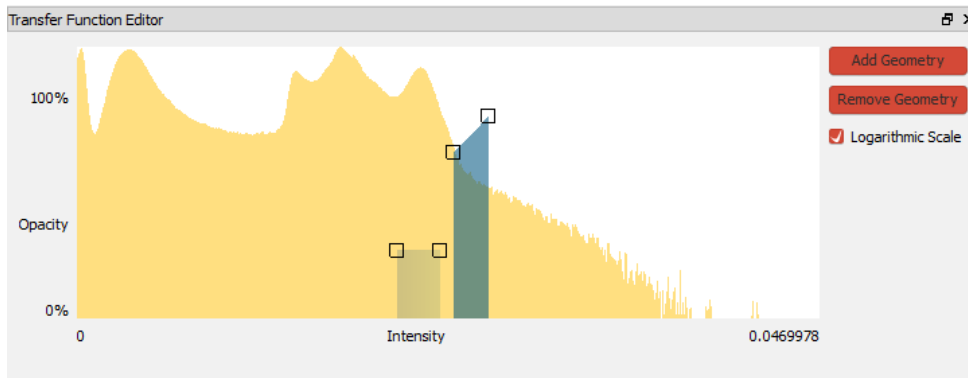
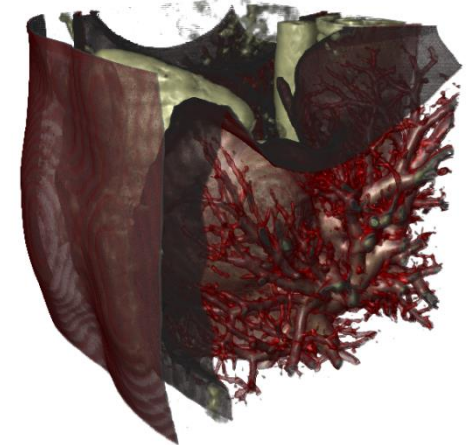
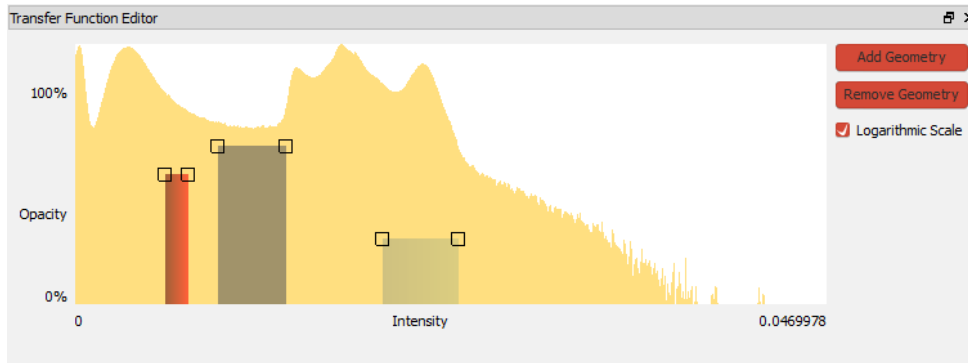


# Classification: Transfer Functions

- Simple concept:  
**Transfer functions** map scalar intensities to optical properties



# Classification: Transfer Function Examples

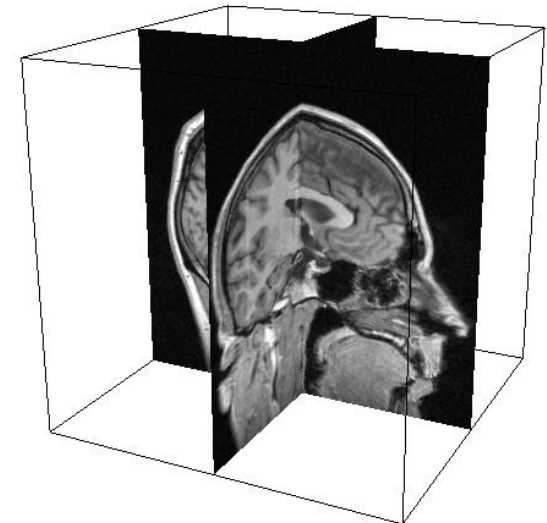
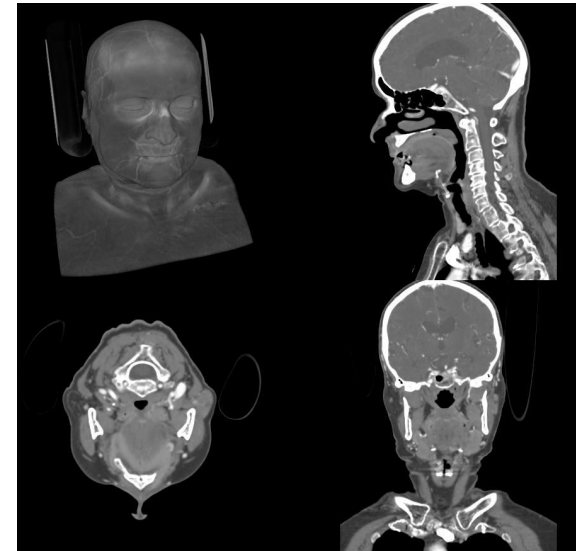




# ESSENTIAL TECHNIQUE #3: MULTI-PLANAR REFORMATION (MPR)

# 2D Visualization of 3D Volumes

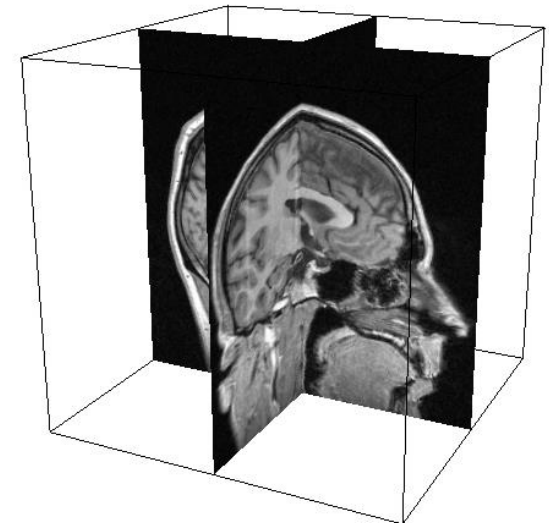
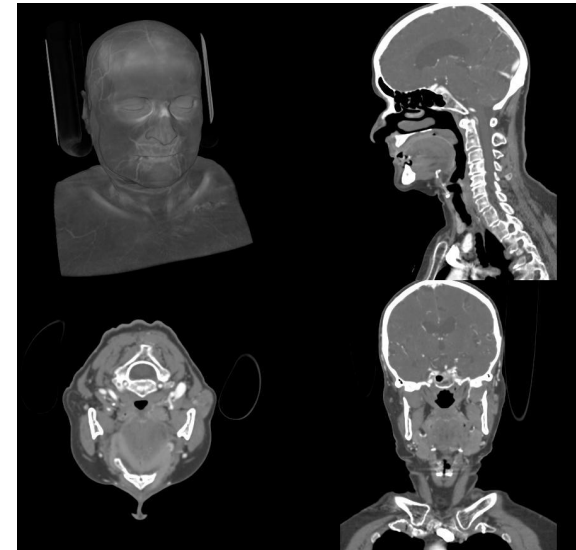
- A 2D view shows only a subset of the 3D data
- Show a cut plane through the volume
- Simplest case:
  - Axis-aligned slice in original resolution
  - → can use voxel intensities directly
- Generic case:
  - Arbitrary slice orientation
  - Slice resolution  $\neq$  volume resolution
  - → need interpolation





# 2D Visualization of 3D Volumes

- Multi-planar Reformation (MPR)
  - Define a cut plane through volume (e.g. use Hesse Normal Form)
  - Find transformation from 2D pixel space to voxel space
  - For each pixel:
    - Compute corresponding voxel
    - Acquire voxel intensity (interpolation!)
    - Apply transfer function
    - Color pixel accordingly

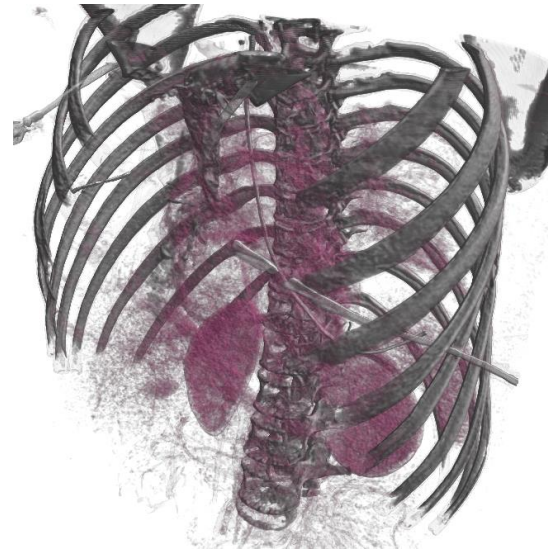
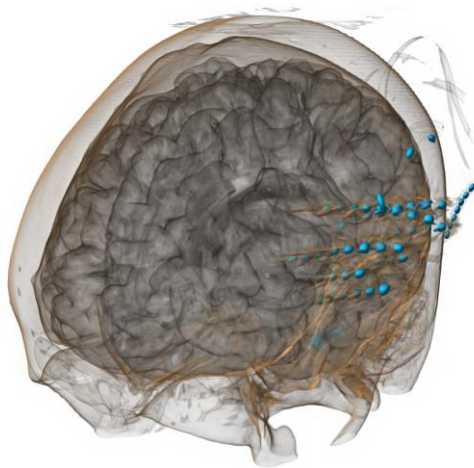




# ESSENTIAL TECHNIQUE #4: DIRECT VOLUME RENDERING (RAY CASTING)

# Direct Volume Rendering

- How do we get a photo-realistic rendering of the data?



Sampling



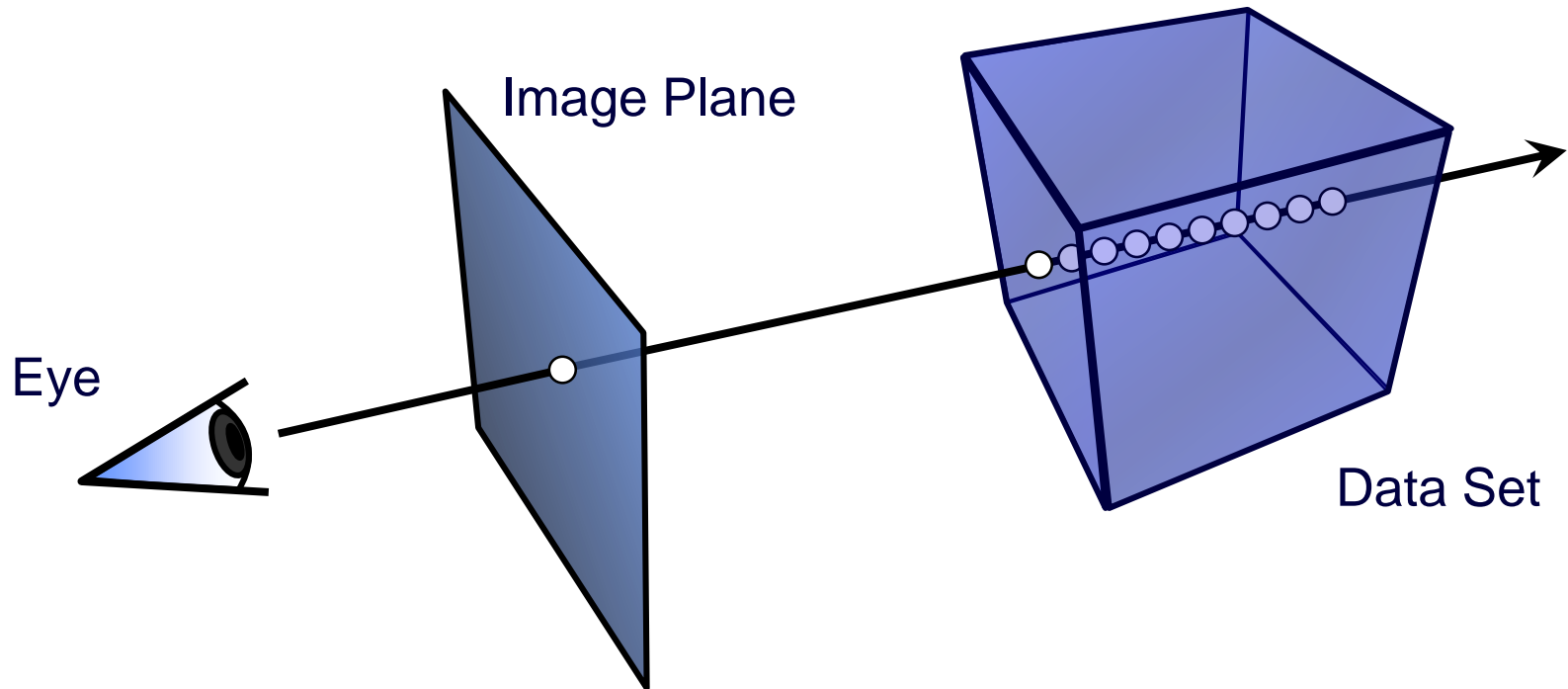
Classification



Compositing



# The Direct Volume Rendering Pipeline



- Direct Volume Rendering
  - Setup a scene with a virtual camera and image plane
  - Simulate physics of light transport through ray casting
  - Sample voxel intensities along rays (interpolation)
  - Integrate voxel intensities along rays (compositing)

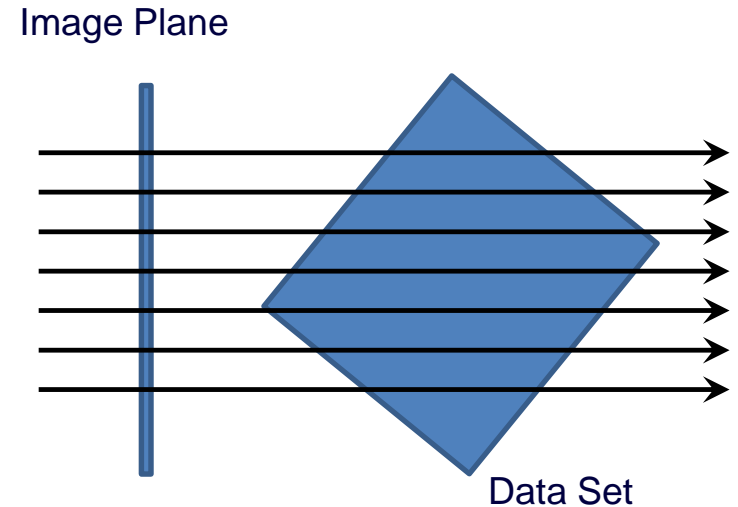


Image courtesy of: Engel et al.: „Real-Time Volume Graphics Tutorial“ – *Eurographics Workshop 2006*

# Orthographic vs. Perspective Projection

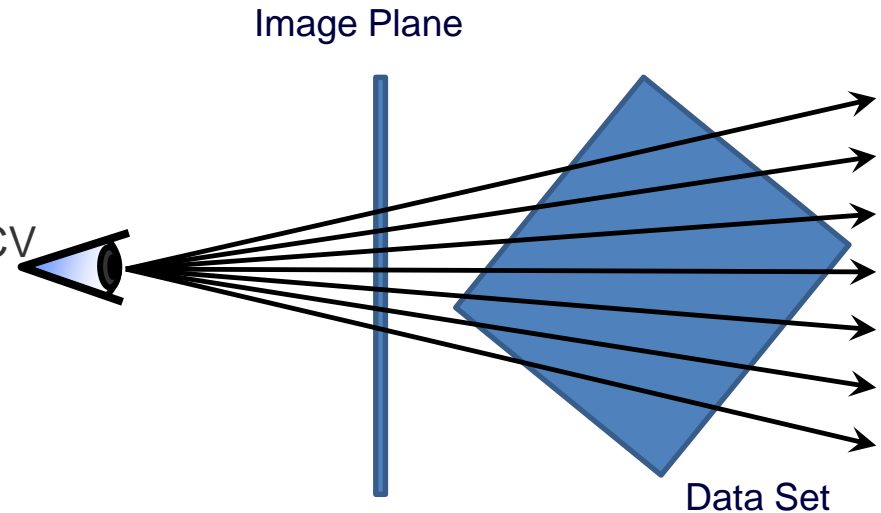
- Orthographic Projection

- Often used in engineering drawings
- Not a natural camera model



- Perspective Projection

- Fits the eye's natural imaging process better by modeling a pinhole camera
- More correct, usually used in CG, Vis, CV



# Compositing Modes

- The compositing mode (in conjunction with the transfer function) defines the look of the data
- Maximum Intensity Projection (MIP)
  - Simplest form, just use the maximum intensity along each ray
- Direct Volume Rendering (DVR)
  - Photo-realistic rendering, approximates physics of light transport
- Digitally Reconstructed Radiograph (DRR)
  - Simulate 2D X-Ray images from CT
- ...





# ASSIGNMENT 9

# Your Assignment

- Create a tool to visualize volume data
- → Use this to inspect and gain insight into the mystery data
- Functionality to implement:
  - Trilinear interpolation (~10 LOC)
  - Simple classification scheme (<10 LOC)
  - 2D MPR rendering (~30 LOC)
  - Simple Direct Volume Rendering with MIP classification scheme (~50 LOC)





# Optional Tasks

- Use advanced Transfer functions
  - You can use a transfer function editor from the internet if you like, as long as you give credit
- Use advanced Compositing schemes
  - DRR is simple to adapt from the simulation in part 1
  - DVR requires a front-to-back alpha blending
  - DVR without illumination might still look crappy
    - Use the volume gradient as a „surface normal“
    - Lambertian diffuse shading or Blinn, Phong, or Blinn-Phong shading
- Use parallelization
  - CPU-based Volume Rendering is slow
  - It scales with the display resolution
  - OpenMP, tbb and std::thread are nice ways to achieve parallelization





## FURTHER READING

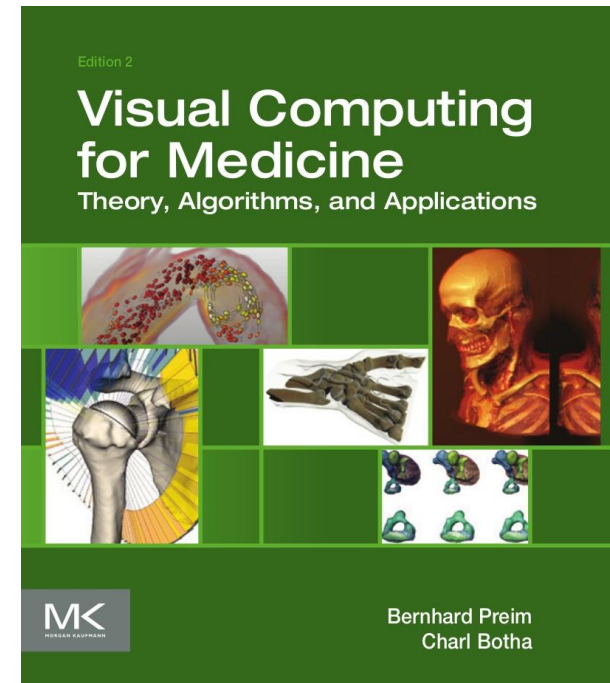
# Further Reading

Survey Book (goes far beyond this seminar):

- Excellent overview over almost the entire body of current literature on medical visualization  
→ <http://medvisbook.com>

More in-depth information on the different topics:

- English version of Prof. Preim's (University of Magdeburg) lecture slides on Medical Visualization are available at:  
→ <http://medvisbook.com/courses-and-tutorials/prof-preims-international-medvis-lectures/>



# Important!

Deadline is coming!

**February 1<sup>st</sup> 2017**

- Report to Tobias about your progress
- Make sure everything compiles on the VM/CI
- Make sure everybody did something





THANK YOU