Таблицы

неопределенных интегралов

производных

$$1. \qquad \int 1 \cdot dx = x + C$$

$$\int 1 \cdot dx = x + C; \qquad (x)' = 1$$

2.
$$\int x^{\alpha} dx = \frac{x^{\alpha+1}}{\alpha+1} + C \quad (\alpha \neq -1);$$

$$(x^{\alpha})' = \alpha x^{\alpha - 1}$$

$$3. \qquad \int \frac{dx}{x} = \ln|x| + C;$$

$$(\ln x)' = \frac{1}{x}$$

4.
$$\int \sin x \cdot dx = -\cos x + C ;$$

$$(\sin x)' = \cos x$$

$$\int \cos x \cdot dx = \sin x + C \; ;$$

$$(\cos x)' = -\sin x$$

6.
$$\int \frac{dx}{\cos^2 x} = \operatorname{tg} x + C ;$$

$$(\mathsf{tg}x)' = \frac{1}{\cos^2 x}$$

7.
$$\int \frac{dx}{\sin^2 x} = -\operatorname{ctg} x + C;$$

$$(\operatorname{ctg} x)' = -\frac{1}{\sin^2 x}$$

8.
$$\int a^x dx = \frac{a^x}{\ln a} + C;$$

$$(a^x)' = a^x \cdot \ln a$$

$$9. \qquad \int e^x \, dx = e^x + C \; ;$$

$$(e^x)'=e^x$$

10.
$$\int \frac{dx}{1+x^2} = \begin{cases} \arctan x + C \\ -\arctan x + C \end{cases}$$

$$(\operatorname{arctg} x)' = \frac{1}{x^2 + 1}$$

11.
$$\int \frac{dx}{\sqrt{1-x^2}} = \begin{cases} \arcsin x + C \\ -\arccos x + C \end{cases}$$

$$(\operatorname{arcctg} x)' = -\frac{1}{x^2 + 1}$$

12.
$$\int \frac{dx}{a^2 + x^2} = \begin{cases} \frac{1}{a} \operatorname{arctg} \frac{x}{a} + C \\ \frac{1}{a} \operatorname{arcctg} \frac{x}{a} + C \\ -\frac{1}{a} \operatorname{arcctg} \frac{x}{a} + C \end{cases} \quad (a > 0);$$

$$(\arcsin x)' = \frac{1}{\sqrt{1 - x^2}}$$

13.
$$\int \frac{dx}{\sqrt{a^2 - x^2}} = \begin{cases} \arcsin \frac{x}{a} + C \\ -\arccos \frac{x}{a} + C \end{cases} \quad (a > 0); \quad (\arccos x)' = -\frac{1}{\sqrt{1 - x^2}}$$

$$(\arccos x)' = -\frac{1}{\sqrt{1 - x^2}}$$

14.
$$\int \frac{dx}{\sqrt{x^2 + a^2}} = \ln\left(x + \sqrt{x^2 \pm a^2}\right) + C \quad (a > 0); \qquad \left(\ln(x + \sqrt{x^2 \pm a^2})\right)' = \frac{1}{\sqrt{x^2 + a^2}}$$

$$\left(\ln(x + \sqrt{x^2 \pm a^2})\right)' = \frac{1}{\sqrt{x^2 \pm a^2}}$$

15.
$$\int \frac{dx}{x^2 - a^2} = \frac{1}{2a} \ln \left| \frac{x - a}{x + a} \right| + C \quad (a > 0);$$

16.
$$\int \operatorname{sh} x \cdot dx = \operatorname{ch} x + C;$$

$$(\operatorname{ch} x)' = \operatorname{sh} x$$

17.
$$\int \operatorname{ch} x \cdot dx = \operatorname{sh} x + C.$$

$$(\operatorname{sh} x)' = \operatorname{ch} x$$