

Learning Module 8: Yield and Yield Spread Measures for Floating Rate Instruments

Q.204 A Treasury Bill (T-Bill) with a par value of USD 1,000,000 and 200 days until maturity is selling for USD 990,000. Its bank discount yield is *closest to*:

- A. 0.54%
- B. 1.80%
- C. 1.82%.

The correct answer is **B**.

The following formula determines the bank discount yield;

$$PV = FV \times [1 - \frac{\text{Days}}{\text{Year}} \times DY]$$

Where; PV = Current selling price of the T-Bill. FV = Par value of the T-Bill. DY = Discount yield. Therefore;

$$990,000 = 1,000,000 \times [1 - \frac{200}{360} \times DY] \Rightarrow DY = 1.8\%$$

A is incorrect. Divides the number of days with days to maturity as follows:

$$1,000,000 \times [1 - \frac{360}{200} \times DY] = 990,000 \Rightarrow DY = 0.54\%$$

C is incorrect. It assumes a 365-day year:

$$990,000 = 1,000,000 \times [1 - \frac{200}{365} \times DY] \Rightarrow DY = 1.82\%$$

CFA Level I, Fixed Income, Learning Module 8: Yield and Yield Spread Measures for Floating-Rate Instruments, LOS (a): Calculate and interpret yield spread measures for floating-rate instruments.

Q.207 A Treasury bill with a face value of \$10,000 and 150 days until maturity is selling for \$9,650. The T-bill's money market yield is *closest to*;

- A. 8.40%
- B. 8.65%
- C. 8.70%

The correct answer is **A**.

The money market yield is calculated as:

$$DR = \frac{\text{Year}}{\text{Days}} \times \left(\frac{FV-PV}{FV} \right) = \frac{360}{150} \times \left(\frac{10,000-9650}{10,000} \right) = 8.40\%$$

B is incorrect. It assumes the 365-day year.

C is incorrect. It calculates the add-on rate instead of discount rate.

CFA Level I, Fixed Income, Learning Module 8: Yield and Yield Spread Measures for Floating-Rate Instruments, LOS (b): Calculate and interpret yield measures for money market instruments.

Q.212 A \$10,000 par value T-Bill is selling for \$9,850. There are 150 days until maturity. The bank discount yield is *closest to*:

- A. 3.60%
- B. 3.56%
- C. 3.65%

The correct answer is **A**.

$$PV = FV \times [1 - \frac{\text{Days}}{\text{Year}} \times DY]$$

So that:

$$9,850 = 10,000 \times [1 - \frac{150}{360} \times DY] \Rightarrow DY = 3.60\%$$

B is incorrect. It assumes annual compounding:

$$10000[1 - DY]^{\frac{150}{360}} = 9850 \Rightarrow DY = 3.56\%$$

C is incorrect. Assumes 365-day year:

$$9,850 = 10,000 \times [1 - \frac{150}{365} \times DY] \Rightarrow DY = 3.65\%$$

CFA Level I, Fixed Income, Learning Module 8: Yield and Yield Spread Measures for Floating-Rate Instruments, LOS (b): Calculate and interpret yield measures for money market instruments.

Q.853 The redemption yield is the rate of return based on certain assumptions. Which of the following is *least likely* an assumption for calculating the redemption yield?

- A. The investor holds the bond to maturity.
- B. The investor is able to reinvest coupon payments at a different yield.
- C. The issuer makes all of the coupon and principal payments in full on scheduled dates.

The correct answer is **B**.

Reinvestment of coupon payments at the exact yield is a characteristic of the internal rate of return. Hence, it is the least likely option.

A is incorrect. Bond maturity is critical in the calculation of the present value given a discount rate.

C is incorrect. The bond issuer always makes all of the coupon and principal payments in full and on scheduled dates.

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Q.863 A frequently used benchmark for floating-rate notes is the:

- A. LIBOR.
- B. I-spread.
- C. G-spread.

The correct answer is **A**.

The reason for its most frequent use is its nature (i.e., a composite interbank rate). Also, it is not a risk-free rate.

B is incorrect. I-spread is the difference between the yield on a bond and the swap rate.

C is incorrect. G-spread is the difference between the yield on treasury and corporate bonds of the same maturity.

CFA Level I, Fixed Income, Learning Module 8: Yield and Yield Spread Measures for Floating-Rate Instruments, LOS (b): Calculate and interpret yield measures for money market instruments.

Q.2515 Which type of debt instrument typically has a more stable market value?

- A. Fixed-rate debt instruments.
- B. Floating-rate debt instruments.
- C. Both fixed-rate debt and floating-rate debt instruments.

The correct answer is **B**.

Fixed-rate debt values are more volatile compared to those of floating-rate notes of similar maturities. Fixed-rate debts are sensitive to interest rate changes, leading to fluctuations in their market value. On the other hand, floating-rate notes adjust their coupon payments with the reference rate, making their values more stable.

A is incorrect. Fixed-rate debts are sensitive to interest rate changes, leading to fluctuations in their market value.

C is incorrect. Both fixed-rate and floating-rate debt instruments do not have equally stable values. Floating-rate debt instruments are more stable because their coupon payments adjust with interest rate changes.

CFA Level I, Fixed Income, Learning Module 8: Yield and Yield Spread Measures for Floating-Rate Instruments, LOS 8a: Calculate and interpret yield spread measures for floating-rate instruments.

Q.2516 If the discount margin is greater than the quoted margin, the floating rate note (FRN) will trade at:

- A. Par.
- B. A premium.
- C. A discount.

The correct answer is **C**.

If the discount margin is greater than the quoted margin, the FRN will trade at a discount.

A is incorrect. The FRN will trade at par if the discount margin equals the quoted margin.

B is incorrect. The FRN will trade at a premium if the discount margin is less than the quoted margin.

CFA Level I, Fixed Income, Learning Module 8: Yield and Yield Spread Measures for Floating-Rate Instruments, LOS (a): Calculate and interpret yield spread measures for floating-rate instruments.

Q.2517 A \$1,000 90-day T-bill is priced with an annualized discount of 1.2%. The annualized add-on yield based on a 365-day year is *closest to*:

- A. 1.22%
- B. 1.25%
- C. 1.50%

The correct answer is **A**.

We will first determine the current price of the treasury bill (PV).

$$PV = FV \times \left(1 - \frac{\text{Days}}{\text{Year}} \times DR\right)$$

Where

PV- Principal Amount (The price of the treasury bill).

FV = Face value of the treasury bond at maturity.

DR = Discount Rate.

Days = number of days between the settlement and maturity periods.

Year = number of days in a year.

$$PV = 1,000 \times \left(1 - \frac{90}{360} \times 0.012\right) = 997$$

Then we determine the AOR using the AOR formula. Note that we've been asked to use a 365-day year.

$$AOR = \frac{FV - PV}{PV} \times \frac{\text{Year}}{\text{Days}} = \frac{1,000 - 997}{997} \times \frac{365}{90} = 0.012203 \text{ or } 1.2203\%$$

CFA Level I, Fixed Income, Learning Module 8: Yield and Yield Spread Measures for Floating-Rate Instruments, LOS (a): Calculate and interpret yield spread measures for floating-rate instruments.

Q.2518 If a \$1 million negotiable Certificate of Deposit (CD) with 120 days to maturity is quoted with an add-on yield of 1.4% based on a 365-day year, then the payment at maturity for this CD is closest to:

- A. \$1,004,500
- B. \$1,004,603
- C. \$1,001,400

The correct answer is **B**.

We need to calculate the FV using the add-on-rate formulae.

$$PV = \frac{FV}{(1 + \frac{\text{Days}}{\text{Year}} \times AOR)}$$

Therefore,

$$FV = PV \times (1 + \frac{\text{Days}}{\text{Year}} \times AOR) = 1,000,000 \times (1 + \frac{120}{365} \times 0.014) = 1,004,602.74 \approx 1,004,603$$

A and C are incorrect. The correct answer is \$ 1,004,603 as shown in the calculation above.

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Q.2677 A USD 1,000 face value T-bill is paying a Bank Discount Yield of 2.6%. The amount of the discount if the bill is maturing in 180 days is *closest to*:

- A. USD 13
- B. USD 26
- C. USD 52

The correct answer is **A**.

The bank discount yield is calculated as follows;

$$BDY = \frac{\text{Discount}}{\text{Face value}} \times \frac{360}{\text{Time to maturity}}$$

Therefore;

$$\text{Discount} = \frac{BDY \times \text{Face value} \times \text{Time to maturity}}{360} = \frac{0.026 \times 1,000 \times 180}{360} = \$13$$

B is incorrect. It assumes the following calculation;

$$\text{Discount} = \frac{2.6}{100} \times 1,000 = \$26$$

C is incorrect. It assumes the following calculations;

$$\text{Discount} = \$26 \times \frac{360}{180} = \$52$$

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Q.2679 Which of the following return measures ignore(s) the effect of compound interest in calculating the yield to maturity?

- I. Money Market Yield
- II. Bank Discount Yield
- III. Bond Equivalent Yield

- A. I only

B. I & II only

C. I, II & III

The correct answer is C.

The Bank Discount Yield (BDY), the Bond Equivalent Yield (BEY), and the Money Market Yield (MMY) all ignore the compounding effect, $(1 + i)^n$ where i is the interest rate and n the time, in the calculation of the YTM. For example, if the semiannual YTM is 3.75%, the bond equivalent yield is simply $3.75\% * 2 = 7.5\%$.

Note: Formula for:

$$\text{Money Market Yield} = \text{HPY} \times \frac{360}{t}$$

, where HPY is the Holding Period Yield and t the time to maturity. HPY is obtained using the formulae

$$\text{HPY} = \frac{P_1 - P_0 + D_1}{P_0}$$

, where P_0 is the beginning price, P_1 the ending price and D_1 the cash distributions.

$$\text{Bank Discount Yield} = r_{BD} = \frac{D}{F} \times \frac{360}{t}$$

, where D is the discount, F is the face value and t the time to maturity.

$$\text{Bond Equivalent Yield} = \frac{F - P}{P} \times \frac{365}{t}$$

, where F is the face value, P the purchase price and t the time to maturity of the bonds.

Bond equivalent yield, when given a semi-annual yield is simply $2 \times$ Semi annual Yield

CFA Level I, Fixed Income, Learning Module 8: Yield and Yield Spread Measures for Floating-Rate Instruments, LOS (b): Calculate and interpret yield measures for money market instruments.

Q.3416 A \$100 face-value T-Bill is currently trading for \$95.78. If the residual maturity of the T-Bill is 90 days, then its bank discount yield is *closest* to:

- A. 4.22%.
- B. 4.41%.
- C. 16.88%.

The correct answer is C.

$$\begin{aligned}\text{Bank Discount Yield(BDY)} &= \frac{(\text{Face value} - \text{Price})}{\text{Face value}} \times \frac{360}{\text{Days to maturity}} \\ &= \frac{(100 - 95.78)}{100} \times \frac{360}{90} = 0.1688 \text{ or } 16.88\%\end{aligned}$$

A is incorrect. It assumes the following calculation for BDY;

$$\text{BDY} = \frac{(100 - 95.78)}{100} \times 100\% = 4.22\%$$

B is incorrect. It assumes the following calculation for BDY;

$$\text{BDY} = \frac{(100 - 95.78)}{95.78} \times 100\% = 4.406\%$$

CFA Level I, Fixed Income, Learning Module 8: Yield and Yield Spread Measures for Floating-Rate Instruments, LOS (b): Calculate and interpret yield measures for money market instruments.

Q.3417 A T-Bill is currently trading at a price of \$98.30 and has a residual maturity of 70 days. Assuming a face value of \$100, and 365-day year, the effective annual yield is *closest* to:

- A. 1.73%
- B. 8.74%.
- C. 9.35%.

The correct answer is C.

We need to calculate holding period yield:

$$\text{HPY} = \frac{(100 - 98.30)}{98.30} = 1.729\%$$

So that,

$$\text{Effective Annual Yield (EAY)} = (1 + \text{HPY})^{\frac{365}{t}} - 1 = (1 + 0.01729)^{\frac{365}{70}} - 1 = 0.0935 \text{ or } 9.350\%$$

A is incorrect. It relates to the value of HPY as calculated above.

B is incorrect. The figure relates to the value of Bank Discount Yield as calculated below;

$$\text{Bank Discount Yield (BDY)} = \frac{(\text{Face value} - \text{Price})}{\text{Face value}} \times \frac{360}{t} = \frac{(100 - 98.30)}{100} \times \frac{360}{70} = 0.08743 \text{ or } 8.743\%$$

CFA Level I, Fixed Income, Learning Module 8: Yield and Yield Spread Measures for Floating-Rate Instruments, LOS (b): Calculate and interpret yield measures for money market instruments.

Q.3418 A T-Bill is currently trading at \$97.35 and has a residual maturity of 70 days. Assuming a face value of \$100, the money market yield for this T-Bill is *closest* to:

- A. 2.72%
- B. 13.63%.
- C. 14%.

The correct answer is C.

Money market instruments are instruments that have a maturity of less than 1 year. Therefore, the return must be translated into 360 days since money market instruments have a year that is considered to be 360 days.

1. First, calculate the holding period yield:

$$HPY = \frac{(100 - 97.35)}{(97.35)} = 2.72\%$$

2. Then, translate the yield into a money market yield:

$$MMY = \frac{360}{70} \times 2.72 = 14\%$$

A is incorrect. It relates to the HPY rate as calculated above.

B is incorrect. It relates to the value of the Bank Discount Yield as follows;

$$BDY = \frac{(100 - 97.35)}{100} \times \frac{360}{70} = 0.13629 \text{ or } 13.629\%$$

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Q.3419 For a 360-day year, the bond equivalent yield of a 120-day banker's acceptance quoted at a discount rate of 3.75% is *closest* to:

- A. 1.266
- B. 3.75%
- C. 3.85%

The correct answer is C.

We need first to find the present value of the banker's acceptance calculated as:

$$PV = FV \times \left(1 - \frac{\text{Days}}{\text{Year}} \times DR\right)$$

Where

PV = present value or price of the money market instrument

FV = future value paid at maturity, or face value of the money market instrument

Days = number of days between settlement and maturity

Year = number of days in the year

DR = discount rate stated as an annual percentage rate

Thus, in this case we have:

$$PV = 100 \times \left(1 - \frac{120}{360} \times 0.0375\right) = 98.75$$

The bond equivalent rate is also called the add-on rate (AOR) which is given by (all variables are as defined above):

$$\left(\frac{365}{120}\right) \left(\frac{100 - PV}{PV}\right) = \left(\frac{365}{120}\right) \left(\frac{100 - 98.75}{98.75}\right) = 0.03850 \approx 3.85\%$$

Note: We are using a 360-day year for the PV and a 365-day year for the AOR.

A is incorrect. It indicates the HPY as follows;

$$HPY = \frac{(100 - 98.75)}{98.75} = 1.266\%$$

B is incorrect. It indicates the BDY as follows;

$$BDY = \frac{(100 - 98.75)}{100} \times \frac{360}{120} = 3.75\%$$

CFA Level I, Fixed Income, Learning Module 8: Yield and Yield Spread Measures for Floating-Rate Instruments, LOS (b): Calculate and interpret yield measures for money market instruments.

Q.3420 The money market yield of a T-Bill with a residual maturity of 90 days is 9.80%. Assuming a face value of \$100, the price of the T-Bill is *closest* to:

- A. \$96.61.
- B. \$98.61.
- C. \$97.61.

The correct answer is **C**.

$$\text{Money market yield} = \text{HPY} \times \left(\frac{360}{\text{Days to maturity}} \right)$$

where;

$$\begin{aligned}\text{HPY} &= \text{MMY} \times \frac{t}{360} = 9.8 \\ \Rightarrow \text{HPY} &= \frac{\text{Discount}}{\text{Price}} = \frac{\text{FV}}{\text{Price}} - 1\end{aligned}$$

Making the price the subject:

$$\text{Price} = \frac{\text{FV}}{1 + \text{HPY}} = \frac{100}{1 + 0.0245} = \$97.609$$

A and B are incorrect. The correct answer is \$97.61 as calculated above.

CFA Level I, Fixed Income, Learning Module 8: Yield and Yield Spread Measures for Floating-Rate Instruments, LOS (b): Calculate and interpret yield measures for money market instruments.

Q.3421 The bank discount yield of a T-Bill with a residual maturity of 110 days is equal to 2.30%. Assuming a face value of \$100, the price of the T-Bill is *closest* to:

- A. \$98.30.
- B. \$99.30.
- C. \$97.30.

The correct answer is **B**.

$$\begin{aligned}\text{Bank Discount Yield} &= \frac{\text{Discount}}{\text{FV}} \times \frac{360}{t} \\ \Rightarrow \text{Discount} &= \text{BDY} \times \frac{t}{360} \times \text{FV} = 2.30\% \times \frac{110}{360} \times 100 = 0.70 \\ \therefore \text{Price} &= \text{FV}-\text{Discount} = 100 - 0.70 = \$99.30\end{aligned}$$

A and C are incorrect. The correct answer is \$97.30 as calculated above.

CFA Level I, Fixed Income, Learning Module 8: Yield and Yield Spread Measures for Floating-Rate Instruments, LOS (b): Calculate and interpret yield measures for money market instruments.

Q.3422 A T-Bill with a residual maturity of 100 days has an effective annual yield of 4.45%. Assuming a face value of \$100, the price of the T-Bill is *closest* to:

- A. \$98.81.
- B. \$100.
- C. \$97.81.

The correct answer is **A**.

$$\text{Effective Annual Yield} = (1 + \text{HPY})^{\frac{365}{t}} - 1$$

Where

$$\text{HPY} = (1 + 4.45\%)^{\frac{100}{365}} - 1 = 1.20\%$$

So that:

$$\text{Price} = \frac{\text{FV}}{1 + \text{HPY}} = \frac{100}{1 + 0.012} = \$98.814$$

B is incorrect. This is the future value.

C is incorrect. The correct answer is \$98.814 as shown in the calculation above.

CFA Level I, Fixed Income, Learning Module 8: Yield and Yield Spread Measures for Floating-Rate Instruments, LOS (b): Calculate and interpret yield measures for money market instruments.

Q.3423 If a bond with a residual maturity of 4 months has a holding period return of 2.60%, then the semiannual bond equivalent yield is *closest* to:

- A. 7.99%.
- B. 7.85%.
- C. 8.00%.

The correct answer is **B**.

The bond equivalent yield is twice the semi-annual discount rate. The HPY is indicated for 4 months. The best method to solve this problem is converting the HPY into an annual rate:

Since 4 months * 3 = 12 months,

$$1 + \text{Annual rate} = (1 + \text{HPY})^3$$

$$\text{Annual rate} = (1 + 2.60\%)^3 - 1 = 8.00\%$$

Once we have the annual rate, we must convert the rate into a semi-annual rate.

$$1 + \text{Annual rate} = (1 + \text{Semi-annual rate})^2$$

$$\text{Semi-annual rate} = (1 + \text{Annual rate})^{0.5} - 1$$

$$= (1 + 8\%)^{0.5} - 1 = 3.92\%$$

$$\text{Bond equivalent yield} = 2 * 3.92\% = 7.85\%$$

A and C are incorrect. 8.00% is the annual rate.

CFA Level 1, Fixed Income, Learning Module 8: Yield and Yield Spread Measures for Floating-Rate Instruments, LOS (b): Calculate and interpret yield measures for money market instruments.

Q.3424 If a bond with a residual maturity of 3 months has a bond equivalent yield of 9.20%, then the holding period yield of the bond is *closest* to:

- A. 9.41%.
- B. 2.0%.
- C. 2.3%.

The correct answer is C.

Step I - Find the semi-annual yield:

$$\text{Semi-annual yield} = \text{BEY}/2 = 9.20\%/2 = 4.60\%$$

Step II - Compute the annual yield from the semi-annual yield:

$$\text{Annual yield} = (1 + \text{Semi-annual yield})^2 - 1$$

$$= (1 + 4.60\%)^2 - 1 = 9.41\%$$

Step III - Compute the holding period yield:

$$1 + \text{Annual yield} = (1 + \text{HPY})^{(12/\text{Residual maturity})}$$

$$1 + 9.41\% = (1 + \text{HPY})^{(12/3)}$$

$$1 + \text{HPY} = (1 + 9.41\%)^{(3/12)}$$

$$1 + \text{HPY} = 1.023$$

$$\text{HPY} = 1.023 - 1 = 0.023 = 2.3\%$$

A and B are incorrect. The correct answer is 2.3% as calculated above.

CFA Level 1, Fixed Income, Learning Module 8: Yield and Yield Spread Measures for Floating-Rate Instruments, LOS (b): Calculate and interpret yield measures for money market instruments.

Q.3745 A US pension fund pays a 180-day banker's acceptance (BA) with a quoted add-on rate of 5% for a 365-day year. The BA has an initial principal of \$ 100 million. The redemption value of the BA is *closest* to:

- A. \$102.47 million.
- B. \$102.50 million.
- C. \$106.75 million.

The correct answer is **A**.

The pricing formula for the money market instruments quoted on add-on rates is given by:

$$PV = \frac{FV}{(1 + \frac{\text{Days}}{\text{Year}} \times \text{AOR})}$$

Where

PV = Principal amount (the price of the money mar)

FV = redemption value of the money market instrument at maturity (including the interest)

Days = number the days between the settlement and maturity periods

Year = number of days in a year

AOR = add-on rate (usually stated as an annual percentage rate)

So in our case,

$$\begin{aligned} \$100 \text{ million} &= \frac{FV}{(1 + \frac{180}{365} \times 0.05)} \\ &\Rightarrow FV = \$100 \times 1.024658 = \$102.47 \text{ million} \end{aligned}$$

CFA Level 1, Fixed Income, Learning Module 8: Yield and Yield Spread Measures for Floating-Rate Instruments, LOS (b): Calculate and interpret yield measures for money market instruments.

Q.3746 A Canadian pension fund pays a 120-day banker's acceptance (BA) with a quoted add-on rate of 4.5% for a 365-day year. The BA has a redemption value of CAD 10.68 million and is priced at CAD 10.4 million. The applicable add-on rate is *closest* to:

- A. 8.08%.
- B. 8.19%.
- C. 7.05%.

The correct answer is **B**.

The add-on rate can be calculated as:

$$AOR = \left(\frac{\text{Year}}{\text{Days}} \right) \times \left(\frac{FV-PV}{PV} \right)$$

PV = principal amount (the price of the money mar)

FV = redemption value of the money market instrument at maturity (including the interest)

Days = number the days between the settlement and maturity periods

Year = number of days in a year

AOR = add-on rate (usually stated as an annual percentage rate)

So in our case,

$$AOR = \left(\frac{365}{120} \right) \times \left(\frac{10.68 - 10.4}{10.4} \right) = 8.19\%$$

A and C are incorrect. The correct answer is 8.19% as shown in the calculation above.

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