

# GoE (Graph-of-Experts): Trainable Graphs for Hierarchical Multi-Scale Reasoning

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## Abstract.

- propose a Graph of Experts (GoE) architecture
- general framework for adaptive, compositional problem-solving
- each expert represents a specialized subnetwork
- edges between experts are learnable pathways encoding how info should flow
- gating policy learns which experts to invoke and how to traverse the expert graph
- gating enables dynamic routing, feedback, and recombination of partial results
- single pass -> structured reasoning
- blueprint for modern hierarchical intelligence
- efficient computation along graphs
- could coordinate reasoning across multi-modal domains
- need experiment results

## 1 Introduction

- hierarchical problems require systems that adapt across levels of abstraction
- vesuvius scrolls interesting because of diversity of challenges
- conventional deep networks such as UNets or transformers apply the same operations to every region, lacking mechanisms to dynamically compose specialized behaviors
- reframe modular neural routing as a learnable graph
- each node goes with an expert trained for distinct subtask
- in the vesuvius case, geometry reconstruction, fiber orientation, ink segmentation
- directed nodes encode transition policies governing how information propagates
- GoE learns structured pathways through the expert graph, discovering intermediate representations to solve complex, multi-scale problems
- unifies specialization and coordination
- gating mechanism dynamically selects experts and edge transitions
- allows for self-organization into meaningful workflows
- Add experiment info

## 2 Background

- Recent progress in adaptive architectures explores dividing neural computation into specialized components
- MoE paradigm trains multiple experts in a specific data regime, while a gating network selects which to activate per input
- Improves efficiency but remains flat due to one pass

- Google’s mixture of recursions introduces recursive expert calls, enabling dynamic reasoning chains, these are typically linear or sequential, optimized for symbolic or temporal reasoning tasks
- They lack explicit modeling of relationships between experts themselves, for instance, how information should transition between specialists handling distinct subproblems
- Each edge encodes transition policies
- Gating mechanism operates not as a simple router but as a graph traversal policy
- Trained to discover efficient and semantically meaningful pathways across experts
- Learns compositional workflows rather than isolated specializations
- Mention vesuvius relation

### 3 Model Architecture

Here we formalize GoE as a modular pipeline. We cleanly separate input stems, modality-specific adapters that transform raw data into tokens with positions/scale, from a task-agnostic encoder that adds local/global context and emits per-token content embeddings  $h$  (for experts) and routing features  $e$  (for the graph router). The GoE core then performs sparse traversal over a library of lightweight experts under a learned graph router, allocating computation by difficulty and recording path provenance. Task heads are pluggable and minimal (used only for supervision/inference), so stems and heads change with the domain while the GoE core is identical.

#### 3.1 Input Stem

Given a raw input  $x$ , the input stem should produce some sequence of tokens,  $T \in \mathbb{R}^{B \times N \times d}$ , as well as the auxiliary routing features for the graph router,  $A \in \mathbb{R}^{B \times N \times d_a}$ . The input stem is the only component of the system that is modality-specific, as it is the modality adapter for the problem.

#### 3.2 Encoder

The encoder provides global context for the auxiliary routing data with modality-specific methods. Given input from the input stem, the encoder produces multi-level feature maps,  $F^0, \dots, F^L$ , with  $F^L$  being the least dimensional feature map. This is executed by using repeatable G-Blocks with residuals. The encoder then installs a slight attention mechanism to ensure multi-modality multi-reasoning. It should be fused minimally via a content embedding. Routing features should also be extracted from the auxiliary routing features.

#### 3.3 Graph Router

Experts  $\{f_k\}_{k=1..M}$  are generally trainable neural circuits with parameter efficient adapters for modality hints.

#### 3.4 Experts -include training section

#### 3.5 Traversal

#### 3.6 Task Heads and Losses

##### Conflict of interests

The authors should declare here any potential conflicts of interests.

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**Availability of data and software code (optional and strongly suggested)**

Our software code is available at the following URL: XXX.

Our dataset is available at the following URL: XXX.

**References**