

## HomeWork 2

### 1. NFSA to Regular Expression

- a.  $(aa^?b)^+$
- b.  $a(b|ba)(aba^?)^*$

### 2. Bigram Probabilities:

#### a. No Smoothing

$$\begin{aligned} P(\text{standard}|\text{the}) &= 0.0008161044613710555 \\ P(\text{turbo}|\text{standard}) &= 0.2 \\ P(\text{engine}|\text{turbo}) &= 0 \\ P(\text{is}|\text{engine}) &= 0 \\ P(\text{hard}|\text{is}) &= 0 \\ P(\text{to}|\text{hard}) &= 0.75 \\ P(\text{work}|\text{to}) &= 0.004513217279174726 \\ P(\text{Input\_Sentence}) &= P(\text{standard}|\text{the}) * P(\text{turbo}|\text{standard}) * P(\text{engine}|\text{turbo}) \\ &\quad * P(\text{is}|\text{engine}) * P(\text{hard}|\text{is}) * P(\text{to}|\text{hard}) * P(\text{work}|\text{to}) \\ &= 0 \end{aligned}$$

#### b. Add-one Smoothing

$$\begin{aligned} P(\text{standard}|\text{The}) &= 0.0003546728143287817 \\ P(\text{turbo}|\text{standard}) &= 0.00039411455596426696 \\ P(\text{engine}|\text{turbo}) &= 0.0001315097317201473 \\ P(\text{is}|\text{engine}) &= 0.000131250820317627 \\ P(\text{hard}|\text{is}) &= 0.00012423903590508137 \\ P(\text{to}|\text{hard}) &= 0.0005259006047856955 \\ P(\text{work}|\text{to}) &= 0.0008740303725554463 \\ P(\text{Input\_Sentence}) &= P(\text{standard}|\text{the}) * P(\text{turbo}|\text{standard}) * P(\text{engine}|\text{turbo}) \\ &\quad * P(\text{is}|\text{engine}) * P(\text{hard}|\text{is}) * P(\text{to}|\text{hard}) * P(\text{work}|\text{to}) \\ &= 1.377839280853547\text{e-}25 \end{aligned}$$

#### c. Good-Turing Discounting based Smoothing

- a. Note: Please the set the Good Turing smoothed count  $C^*(c)=0$  if  $N_{(c+1)}=0$   
$$\begin{aligned} P(\text{standard}|\text{the}) &= 4.520905085529811\text{e-}05 \\ P(\text{turbo}|\text{standard}) &= 1.2824430746649818\text{e-}05 \end{aligned}$$

$$\begin{aligned}P(\text{engine}|\text{turbo}) &= 0.2483575627283251 \\P(\text{is}|\text{engine}) &= 0.2483575627283251 \\P(\text{hard}|\text{is}) &= 0.2483575627283251 \\P(\text{to}|\text{hard}) &= 4.520905085529811\text{e-}05 \\P(\text{work}|\text{to}) &= 0.00010794966406900566 \\P(\text{Input\_Sentence}) &= P(\text{standard}|\text{the}) * P(\text{turbo}|\text{standard}) * P(\text{engine}|\text{turbo}) \\&* P(\text{is}|\text{engine}) * P(\text{hard}|\text{is}) * P(\text{to}|\text{hard}) * P(\text{work}|\text{to}) \\&= 4.334533243595371\text{e-}20\end{aligned}$$

### 3. Transformation Based POS Tagging (40 points)

*The\_DT standard\_?? Turbo\_NN engine\_NN is\_VBZ hard\_JJ to\_TO work\_??*

A: Sol:

Most Probable tags:

Standard: NN

Work: VB

Top rules generated using Brill's transformation – based POS tagging algorithm are:

From	To	Condition	Score
VBP	VB	MD	54
NN	VB	MD	46
VBD	VDN	VBZ	38
VDN	VBD	PRP	35
VB	VBP	PRP	32
POS	VBZ	PRP	31
VB	VBP	NNS	30
VBP	VB	TO	28
NN	VB	TO	27
VDN	VBD	NNP	27
VBD	VDN	VB	22

After applying rules, final solution generated is standard\_NN, work\_VB

**Final Solution:**

**The\_DT standard\_NN Turbo\_NN engine\_NN is\_VBZ hard\_JJ to\_TO work\_VB**

B: Sol:

*The\_DT standard\_?? Turbo\_NN engine\_NN is\_VBZ hard\_JJ to\_TO work\_??*

Sol:

1. Standard: Word given tags: NN, JJ  
$$\text{NN} = P(\text{standard}/\text{NN}) * P(\text{NN}/\text{DT}) * P(\text{NN}/\text{NN}) = 0.0006305170239596469 * 0.5094639732781931 * 1 = \mathbf{0.0003212257082460234}$$
  
$$\text{JJ} = P(\text{standard}/\text{JJ}) * P(\text{JJ}/\text{DT}) * P(\text{NN}/\text{JJ}) = 0.000774593338497289 * 0.22808970892317482 * 0.5435063258455978 = 9.60249416421585\text{e-}05$$
2. Work: Word given Tags: VB, VBP, NN  
$$\text{VB} = P(\text{work}/\text{VB}) * P(\text{VB}/\text{TO}) = 0.0035035035035035035 * 0.63571889103804 = \mathbf{0.002227243361995135}$$
  
$$\text{VBP} = P(\text{work}/\text{VBP}) * P(\text{VBP}/\text{TO}) = 0.011400651465798045 * 0 = 0$$
  
$$\text{NN} = P(\text{work}/\text{NN}) * P(\text{NN}/\text{TO}) = 0.00234192037470726 * 0.03288201160541586 = 7.700705294008397\text{e-}05$$

**Final Solution:**

**The\_DT standard\_NN Turbo\_NN engine\_NN is\_VBZ hard\_JJ to\_TO work\_VB**