

## Problem A. Inspection

Input file: standard input  
Output file: standard output  
Time limit: 2 seconds  
Memory limit: 64 mebibytes

Due to an inspection in an Imperial Army, it was decided to upgrade the droid army. Emperor Palpatine ordered to throw away two droids with the lowest serial number. Find them!

### Input

First line contains an integer  $N$  — number of droids ( $2 \leq N \leq 100\,000$ ), second line contains  $N$  integers, not exceeding  $2 \cdot 10^9$  in absolute value — droids' serial numbers.

### Output

Output two integers, first one should be the minimum serial number, second one — the second minimum serial number.

### Examples

standard input	standard output
5 49 100 23 -100 157	-100 23
3 1 2419 1	1 1

## Problem B. Sorting

Input file: *standard input*  
Output file: *standard output*  
Time limit: 2 seconds  
Memory limit: 64 mebibytes

Sort the given array of integers. **Don't use the standard sorting algorithm, code your own.**

### Input

First line contains one integer  $N$  ( $1 \leq N \leq 1000$ ), second line —  $N$  integers, not exceeding  $2 \cdot 10^9$  in absolute value.

### Output

Print given integers in non-decreasing order.

### Examples

standard input	standard output
5 9 2 7 1 2	1 2 2 7 9

## Problem C. Inversions

Input file: `standard input`  
Output file: `standard output`  
Time limit: 2 seconds  
Memory limit: 64 mebibytes

Write a program that for a given array  $A = \langle a_1, a_2, \dots, a_n \rangle$  finds the number of pairs of indices  $(i, j)$ , such that  $i < j$  and  $a_i > a_j$ .

### Input

The first line of input contains a single integer  $n$  ( $1 \leq n \leq 5100$ ), the number of elements in the array. The next line contains  $n$  pairwise distinct integers  $a_1, \dots, a_n$  ( $0 \leq a_i \leq 10^9$ ).

### Output

Print a single integer: the answer to the problem.

### Example

standard input	standard output
5 4 3 2 5 1	7



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## Problem D. Selection sort

Input file: *standard input*  
Output file: *standard output*  
Time limit: 1 second  
Memory limit: 256 mebibytes

Implement the selection sort, which, on each step, finds the minimum element in the remaining part of the array and puts it in the first position. Print the number of times the algorithm actually swapped two elements (don't count situations when the minimum is already in the first place).

### Input

First line contains  $n$  ( $1 \leq n \leq 1000$ ) — size of the array. Next line contains  $n$  distinct numbers from 1 to  $n$ , numbers are separated by spaces.

### Output

Output one number — the number of pairs that were swapped during sorting.

### Example

standard input	standard output
4 4 2 1 3	2



## Problem E. Insertion sort

Input file: `standard input`  
Output file: `standard output`  
Time limit: 1 second  
Memory limit: 256 mebibytes

Implement the insertion sort algorithm. Print the number of pairs of adjacent elements that were swapped during the sorting process.

### Input

First line contains  $n$  ( $1 \leq n \leq 1000$ ) — size of the array. Next line contains  $n$  distinct numbers from 1 to  $n$ , numbers are separated by spaces.

### Output

Output one number — the number of pairs that were swapped during sorting.

### Example

standard input	standard output
4 4 2 1 3	4

count

## Problem F. Archive creation

Input file: standard input  
Output file: standard output  
Time limit: 5 seconds  
Memory limit: 64 mebibytes

✓ sum < S

System administrator decided to make a backup of users' data. Unfortunately, hard drive size is less than sum of sizes of all archived files.

You know the sizes of all files. Write a program, that given information about users' data and hard drive size finds the maximum number of users, that can have their data backed up.

### Input

First line contains integers  $S$  — size of the hard drive ( $0 \leq S \leq 10^7$ ) and  $N$  — number of users ( $1 \leq N \leq 10^5$ ). Then  $N$  positive integers not exceeding 300 follow, size of data for each user.

### Output

Output the maximum number of users that can have their data backed up.

### Examples

standard input	standard output
100 2 200 50	1
100 3 50 30 50	2

$S$  long long  
 $N$  long long  
 $a[i] \leq S \leq N$   
~~sort~~ for  $i \leq N$ :  
 $a[i] \leq arr[i]$   
 sort + arr  
 count = 0;  
 sum = 0;  
 for  $i \leq N$   
 if sum < S.  
 count ++

300000

sort

100

25

## Problem G. Intricate sort

Input file: standard input  
Output file: standard output  
Time limit: 2 seconds  
Memory limit: 64 mebibytes

You are given a sequence of numbers. Sort these numbers in increasing order of their last digit. If last digits of two numbers are the same, sort them by their value.


### Input

First line contains  $N$ , the length of the sequence ( $1 \leq N \leq 100$ ). Next  $N$  lines contains numbers in sequence, each on its own line. Numbers are positive and do not exceed 32000.

### Output

Output a sequence of numbers, sorted according to the rule above.

### Example

standard input	standard output
3	930 1280 382
1280	
382	
930	

size ~~elem~~: int  
elem: long long

→ compare by mod 10, if equal compare by value.

100

75

25

$a \% 10 < b \% 10$   
 $a < b$

$<$   $<=$

75  $< 25$



## Problem H. Digital root

Input file: standard input  
Output file: standard output  
Time limit: 2 seconds  
Memory limit: 64 mebibytes

A *digital root* of number  $n$  can be determined as follows: take sum of digits of  $n$ , then take sum of digits of that number and so on, until you get a 1-digit number, which will be a digital root.

Your task is to sort the given array in increasing order of their digital root. If digital roots of two number are the same, the lesser number should go before the larger one.

### Input

First line of input file contains elements of the array. Array length does not exceed 200, each number of positive and does not exceed  $10^9$ .

### Output

Output elements of the array, sorted by their digital root, in case of equality, by the value of the number.

### Examples

standard input	standard output
15 14 13 12 11 10 9 8 7	10 11 12 13 14 15 7 8 9
80 61 51 41 22 1	1 22 41 51 61 80

Size: int

elem: long long

compare by fn.

fn — while  $n \geq 10$

sum

while  $n \geq 1$

sum +=  $(n \% 10)$

$n = n / 10$

$\text{Ans} = \text{a} \setminus n \setminus 1$



## Problem I. Union of segments

Input file: standard input  
Output file: standard output  
Time limit: 1 second  
Memory limit: 64 mebibytes

Solving a problem from a math test, Vasya found the answer as a union of  $N$  segments  $[L_i, R_i]$  on a number line. But, some of these segments can intersect, which Vasya doesn't quite like. Your task is to represent Vasya's answer as a union of a minimum number of non-intersecting segments.

### Input

First line contains one integer  $N$  ( $1 \leq N \leq 50000$ ). Next  $N$  lines contains pairs of integers  $L_i$  and  $R_i$  ( $|L_i|, |R_i| \leq 50000$ ), describing segments.

### Output

In the first line, output a single integer  $M$  — the number of segments in the union. Next  $M$  lines should contain segments in the same format, as in the input file. Left endpoints of these segments must be in increasing order.

### Example

standard input	standard output
4	2
0 2	0 3
4 5	4 6
1 3	
5 6	

sort based on left and right

~~covered~~ ~~left~~ ~~is~~ ~~a[0][0]~~ covered = a[0][0] ans Vector append(a[a][a])

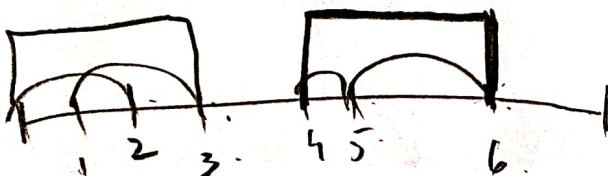
for (i = begin; i < end; i++)

if a[i][0] <= covered

if (i != begin)

ans Vector append(a[i-1])

covered = a[i-1][1]



## Problem J. Minimal cover

Input file: `standard input`  
Output file: `standard output`  
Time limit: 1 second  
Memory limit: 64 mebibytes

You are given some set of segments on a number line with integer endpoints  $[L_i, R_i]$ . Choose the minimum number of segments that cover  $[0, M]$  completely ( $M$  is natural number).

### Input

First line contains integer  $M$  ( $1 \leq M \leq 5000$ ). Next lines describe segments. Each line contains a pair of integers  $L_i$  and  $R_i$  ( $|L_i|, |R_i| \leq 50000$ ), the left and right endpoint of a segment. Input ends with a pair of zeros (doesn't count as a segment). Total number of segments is less than or equal to 100 000.

### Output

In the first line output the minimum number of segments, needed to cover  $[0, M]$  completely. Next, output segments that cover everything in the same format, as in input file (except for two zeros in the end). Output segments in order of increasing left endpoint.

If it's impossible to cover  $[0, M]$  using given segments  $[L_i, R_i]$  print "No solution".

### Examples

standard input	standard output
<pre>1 -1 0 -5 -3 2 5 0 0</pre>	No solution
<pre>1 -1 0 0 1 0 0</pre>	<pre>1 0 1</pre>

first insert  
may miss  
something

before print  
check covering

$[ ]$   $[ ]$

0 1

5  
-1 0  
0 2  
1 5  
2 3  
0 0

2

if



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### Examples

standard input	standard output
<pre> 1 1 0 -5 -3 2 5 0 0 </pre>	No solution
<pre> 1 -1 0 0 1 0 0 </pre>	<pre> 1 0 1 </pre>

sort based on left

~~filter~~ ~~left~~ ~~end~~

filter the ones  $\leq$  current L  
pick the highest  $[L_i, R_i]$

current L =  $\text{snd}$

If  $a[i] > \text{max}$

$\text{max} = a[i].\text{snd}$

current L = a.first

~~max = a.snd~~

current L =  $\text{RL}$

if  $L > \text{end}$

prev L = current L

then

break

filter  $\rightarrow$  init

init L = current L

No Solution