

Swirl Flow Around a Rotating Disk

1) Important Info's: -

➔ *This example models a rotating disk in a tank.*

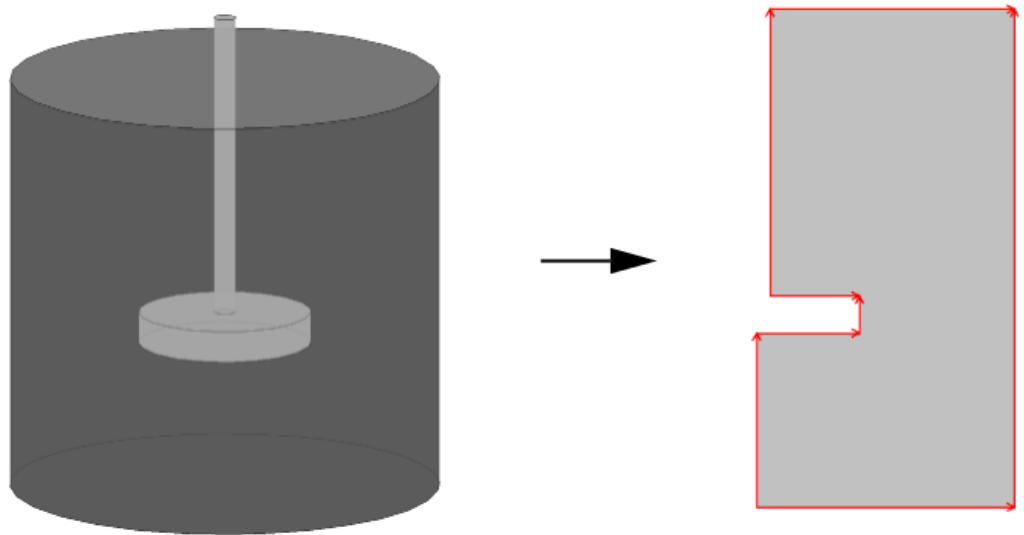


Figure 1: The original 3D geometry can be reduced to 2D because the geometry is rotationally symmetric.

➔ *the velocities in the angular direction differ from zero, so the model must include all three velocity components, even though the geometry is in 2D.*

2)Physics and Equations: -

➔ *The flow is described by the Navier-Stokes equations:*

$$\rho \frac{\partial \mathbf{u}}{\partial t} - \nabla \cdot \eta (\nabla \mathbf{u} + (\nabla \mathbf{u})^T) + \rho \mathbf{u} \cdot \nabla \mathbf{u} + \nabla p = \mathbf{F}$$

$$\nabla \cdot \mathbf{u} = 0$$

- u denotes the velocity (SI unit: m/s),
- ρ the density (SI unit: kg/m³),
- μ the dynamic viscosity (SI unit: Pa·s),
- p the pressure (SI unit: Pa).

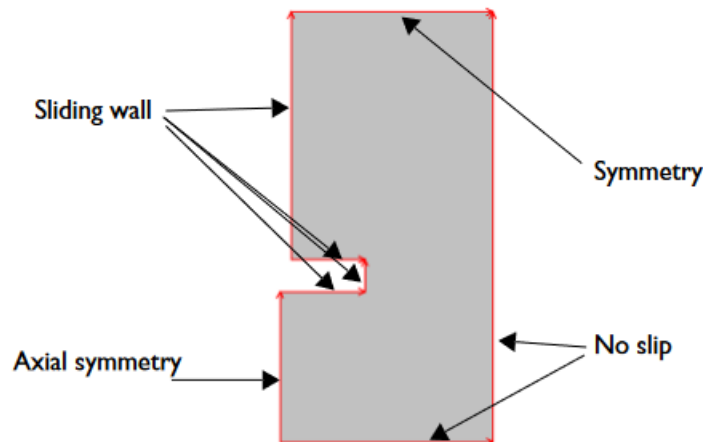
$$\rho \left(u \frac{\partial u}{\partial r} - \frac{v^2}{r} + w \frac{\partial u}{\partial z} \right) + \frac{\partial p}{\partial r} = \mu \left[\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial u}{\partial r} \right) - \frac{u}{r^2} + \frac{\partial^2 u}{\partial z^2} \right] + F_r$$

$$\rho \left(u \frac{\partial v}{\partial r} + \frac{uv}{r} + w \frac{\partial v}{\partial z} \right) = \mu \left[\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial v}{\partial r} \right) - \frac{v}{r^2} + \frac{\partial^2 v}{\partial z^2} \right] + F_\varphi$$

$$\rho \left(u \frac{\partial w}{\partial r} + w \frac{\partial w}{\partial z} \right) + \frac{\partial p}{\partial z} = \mu \left[\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial w}{\partial r} \right) + \frac{\partial^2 w}{\partial z^2} \right] + F_z$$

- u is the radial velocity, v the rotational velocity,
- w the axial velocity (SI unit: m/s).
- In the model we set the volumetric force components F_r , F_φ , and F_z to zero.

3)Boundary Conditions: -



➔ *The velocity components in the plane are zero, and that in the angular direction is equal to the angular velocity, ω , times the radius, r :*

$$u_w = r\omega;$$

➔ *At the boundaries representing the cylinder surface a no slip condition applies, stating that all velocity components equal zero:*

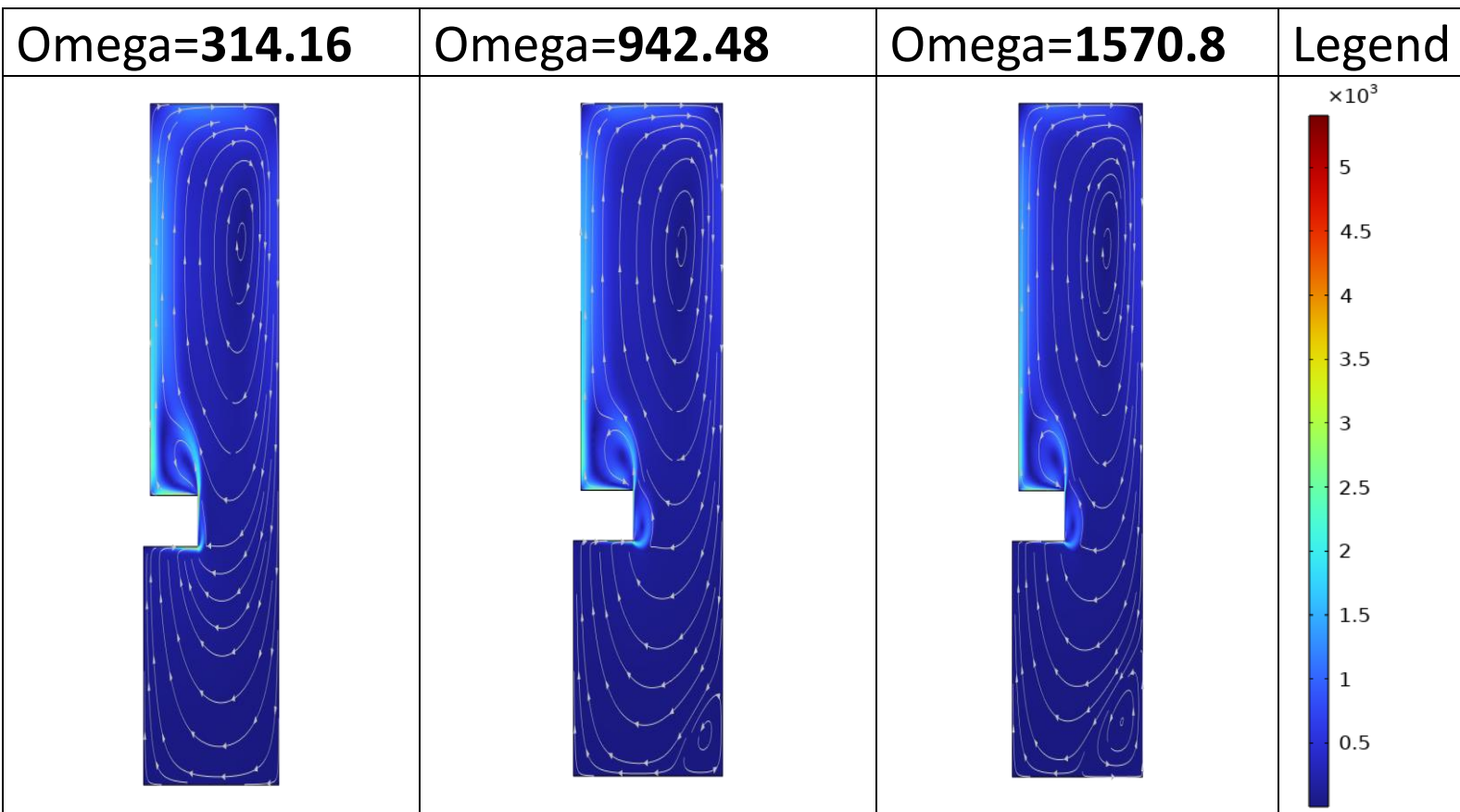
$$u = (0,0,0);$$

➔ *At the boundary corresponding to the rotation axis, use the axial symmetry boundary condition allowing flow in the tangential direction of the boundary but not in the normal direction.*

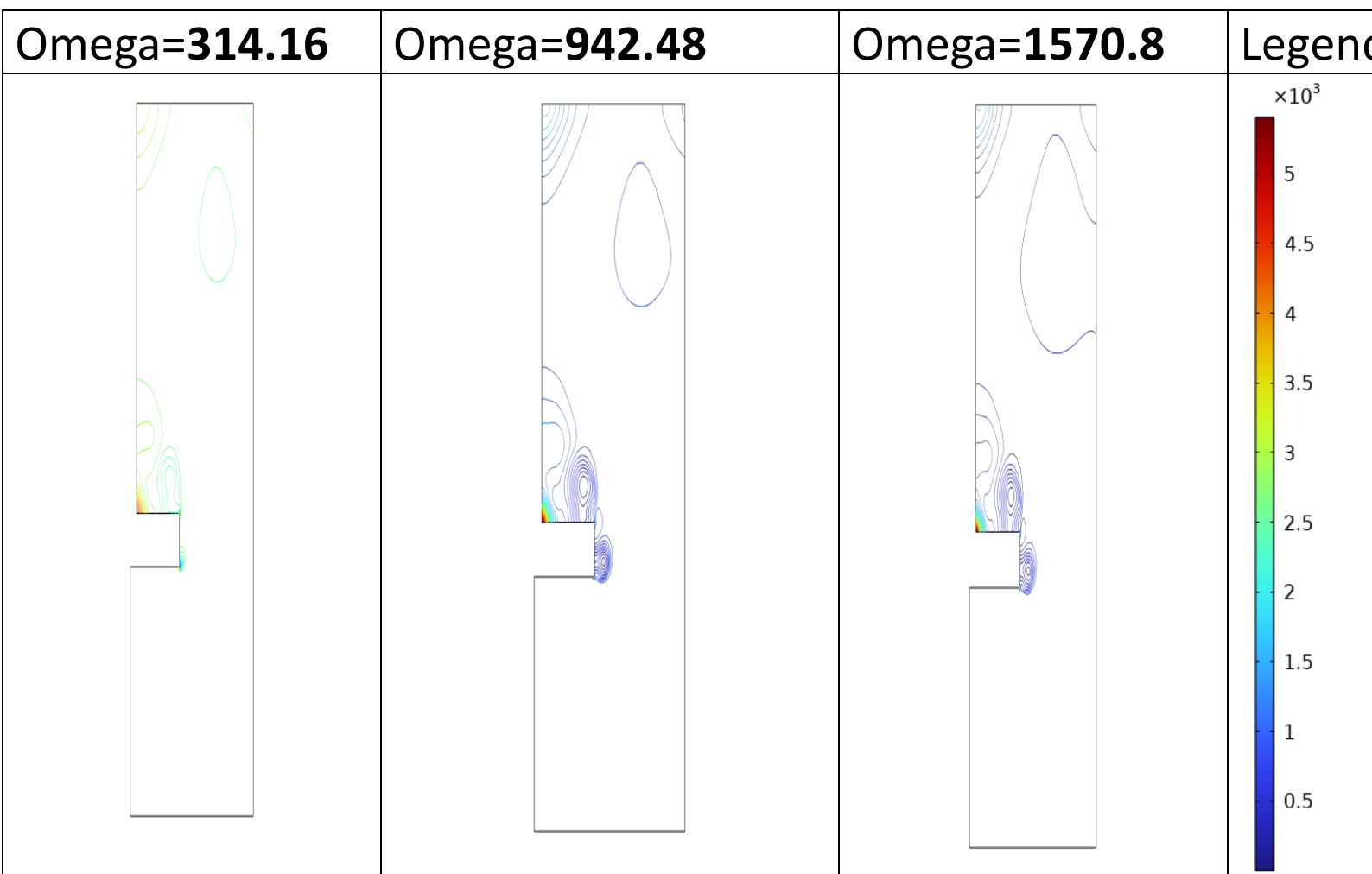
$$u=0; v=0;$$

4)Results: -

➔Velocity (Surface and Streamline) Plot: -

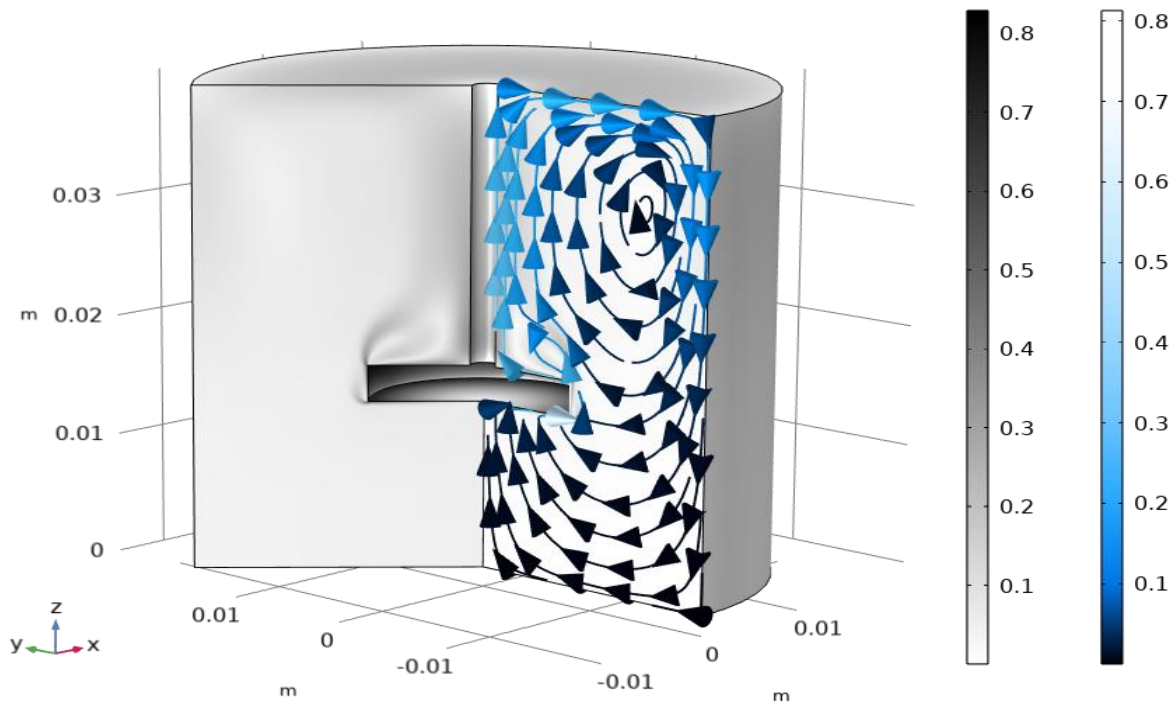


➔ Pressure Plots: -

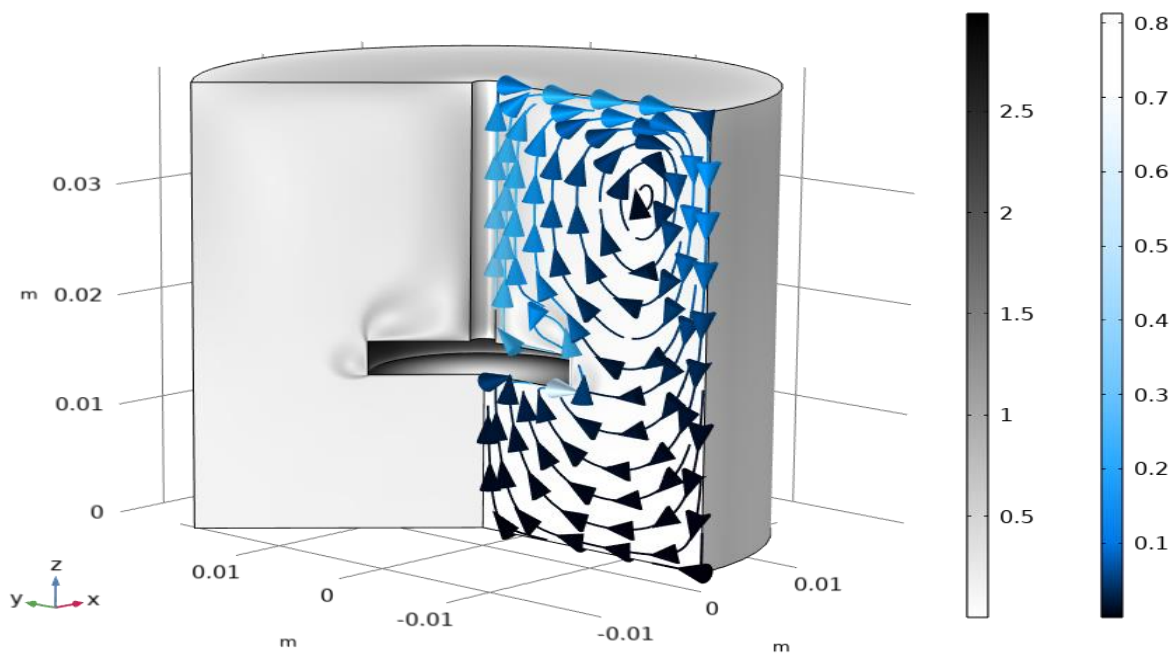


➔ Velocity 3D Plots: -

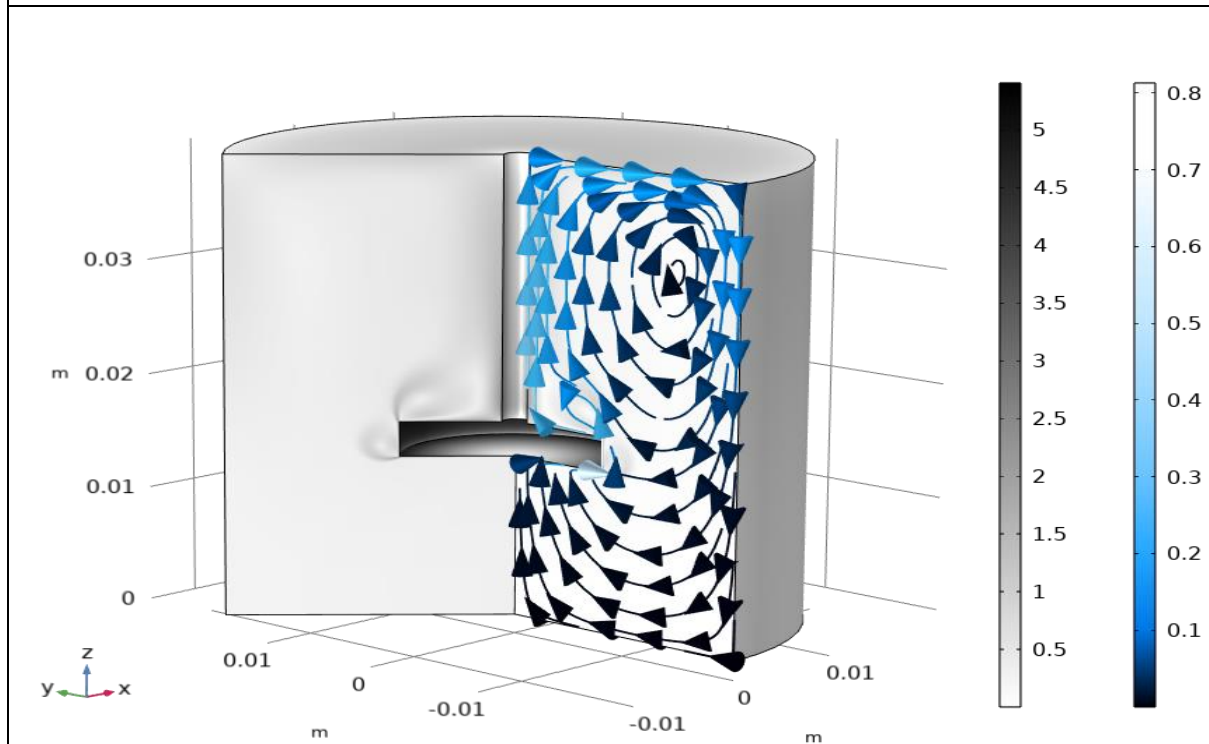
$\Omega = 314.16 \text{ rad/sec}$



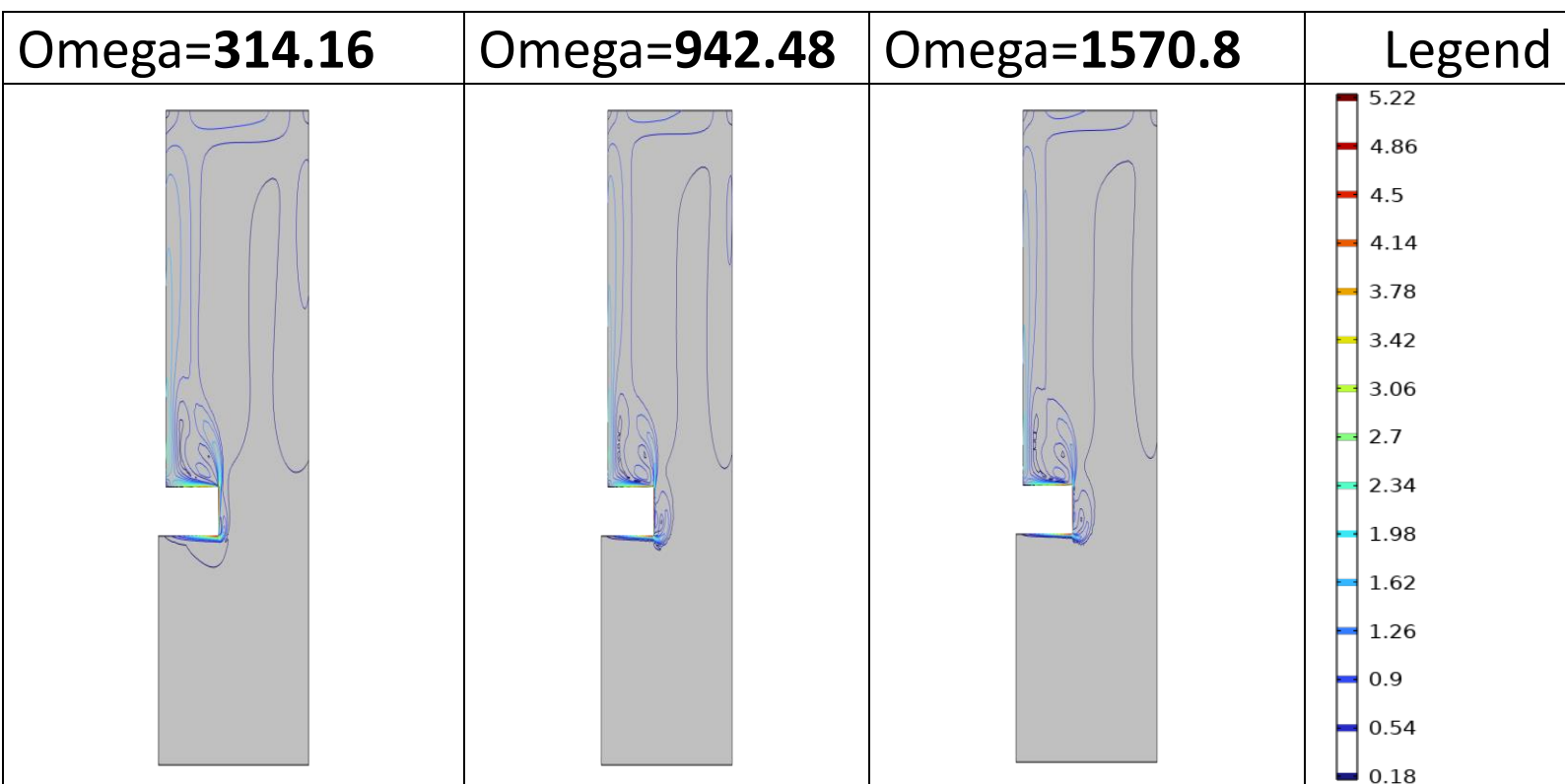
$\Omega = 942.48 \text{ rad/sec}$



$\Omega = 1570.8 \text{ rad/sec}$



➔ Azimuthal Velocity (Surface & Contour) Plot: -



➔ Turbulent Velocity (Surface & Streamline) Plot:

