

Swapnil Daxini

Due: 30/11/2017

## CSC 226: Problem Set 4 Written Part

### Q1) Tragic Comedy and Network flows

We can reduce the ~~probl~~ problem to a Max-flow problem by doing the ~~ff~~ following.

For each comedian, draw a node  $c_i$ . Let the capacity of each edge be number of pairs of passengers  $(p_i, p_j)$ , such that  $c_i \in p_i, p_j$ . Create a directed graph with all the ~~pa~~ comedians and find the max-flow. If the max-flow is equal to ~~size~~  $k$ , then it is possible to evacuate everyone on board.

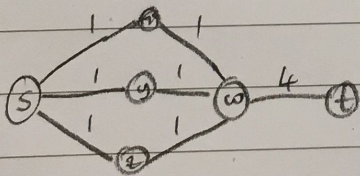


## Q2) Max-flow with Node Capacities

Ans In order to satisfy the node capacity constraint, we can create an additional graph  $G'$  which contains two vertices  $v_o$  and  $v_i$  for every vertex  $v$  in  $G$ . If we set the capacity of the edge  $(v_i, v_o)$  to be the capacity of edge vertex  $v$ , then we can run the Ford-Fulkerson algorithm. As an edge  $(u, v)$  in graph  $G$  does not have a capacity, we set the  $(u_o, v_i)$  in  $G'$  to be infinite. The flow through any vertex will not increase above capacity  $c_v$  as it has to pass through the edge  $(v_i, v_o)$ . Thus, using the Ford-Fulkerson algorithm will find a maximum  $s$ - $t$  flow.

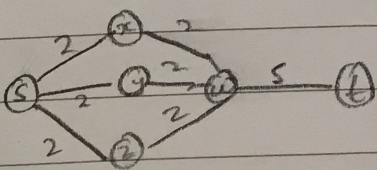
Q3) No they are not right. Consider the following counter example.

Let then initial graph be:



Then the minimum cut is  $A = \{s\}$ ,  $B = U - A$  which has the capacity 3.

Increasing the edges by 1 gives:



The previous min-cut now has a capacity of 6. However the cut  $A = \{s, x, y, z, w\}$ ,  $B = \{t\}$  has a



capacity of 5, thus is the min cut of the graph. Thus, the friend was WRONG

(Q4) Knuth-Morris-Pratt

