## Faculty of Engineering & Technology First Semester B.E. (CBS) Examination APPLIED MATHEMATICS-I

## Paper-I

Time—Three Hours]

[Maximum Marks—80

## INSTRUCTIONS TO CANDIDATES

(1) Solve SIX questions as follows:

Que. No. - 1 OR Que. No. - 2

Que. No. - 3 OR Que. No. - 4

Que. No. - 5 OR Que. No. - 6

Que. No. - 7 OR Oue. No. - 8

Que. No. - 9 OR Que. No. - 10

Que. No. - 11 OR Que. No. - 12

- (2) Use of non-programmable calculator is permitted.
- 1. (a) If  $y = a \cos (\log x) + b \sin (\log x)$ show that  $x^2y_2 + xy_1 + y = 0$  and  $x^2y_{n+2} + (2n+1) xy_{n+1} + (n^2+1)y_n = 0.$ 
  - (b) Evaluate:

$$\lim_{x\to 0} \left( \frac{1}{\sin^2 x} - \frac{1}{x^2} \right)$$

$$\lim_{x\to 0} x \tan\left(\frac{\Pi}{2} - x\right)$$

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$$\theta = \frac{6}{100}$$

(b) Expand  $3x^3 - 2x^2 + x - 4$  in powers of (x-2). 5

Prove that

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(a) If  $u = \log [\tan x + \tan y + \tan z]$ ,

 $\sin 2x \frac{\partial u}{\partial x} + \sin 2y \frac{\partial u}{\partial y} + \sin 2z \frac{\partial u}{\partial z} = 2$ 

(b) If  $u = \sin^{-1} \left( \frac{x^2 + y^2}{\sqrt{x} + \sqrt{y}} \right)$ , then

find the value of  $x^2 \frac{\partial^2 u}{\partial x^2} + 2xy \frac{\partial^2 u}{\partial x \partial y} + y^2 \frac{\partial^2 u}{\partial y^2} = 7$ 

(c) Given  $u = \sin^{-1}x + \sin^{-1}y$ ,  $v = x\sqrt{1-y^2+y\sqrt{1-x^2}}$ . Are u, v functionally and

related? If so, find the relation between them. 6

**a** If  $u = \frac{yz}{x}, v = \frac{xz}{y}, w = \frac{xy}{z}$ 

Find  $\frac{\partial(x,y,z)}{\partial(u,v,w)}$ 

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(b) Expand  $x^2y + 2y - x^2 - 2$  in powers of (x - 1) and (y + 1) by Taylor's theorem.

Ĉ The temperature T at any point (x, y, z) in space is  $T = 400 \text{ xyz}^2$ . Find the highest temperature on the surface  $x^2 + y^2 + z^2 = 1$ .

Test the following system for consistency and solve

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x + y + z = 6

2x + y + 3z = 13

5x + 2y + z = 12

(b) Find the inverse of the following matrix by partitioning method:

OR

6. (a) Find the rank of the following matrix:

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(b) By adjoint method solve the system of equations:

$$x + y + z = 3$$
$$x + 2y + 3z = 4$$

$$x + 4y + 9z = 6$$

(a) Solve: 
$$(1 + x^2) \frac{dy}{dx} + y = e^{\tan^{-1}x}$$

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(a) Solve: 
$$(1+x^{-})\frac{dx}{dx} + y = e^{-x}$$
  
(b) Solve:  $\frac{dy}{dx} + xy = x^{3}y^{3}$ .

(c) Solve: 
$$\frac{dy}{dx} = -\frac{xy^2}{2 + x^2y}$$

8. (a) Solve 
$$p^3 - 4 \times yp + 8y^2 = 0$$
.

(b) Solve 
$$x^{2}(y - px) = yp^{2}$$

If E = 10 sin t volts and i = 0 when t = 0, find i as a function of t.

9. (a) Solve 
$$\frac{d^2y}{dx^2} - 2\frac{dy}{dx} + y = e^x \sin 2x$$

(b) Solve: 
$$\frac{d^2y}{dx^2} + y = \csc x$$
 by method of variation of

parameters.

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(c) Solve:  $x^2 \frac{d^2y}{dx^2} - 3x \frac{dy}{dx} + 5y = x \log x$ .

(a) Solve the simultaneous differential equation

$$\frac{dx}{dt} + 3x - 2y = 1$$

$$\frac{dy}{dt} - 2x + 3y = e^{t}$$

(b) Solve 
$$\frac{d^2y}{dx^2} = 3\sqrt{y}$$
, given that

$$y = 1$$
,  $\frac{dy}{dx} = 2$  when  $x = 0$ .

$$\frac{d^2x}{dt^2} + w_0^2x = F_0 \sin nt$$
, where W<sub>0</sub> and F<sub>0</sub> are

constants. If initially x = 0,  $\frac{dx}{dt} = 0$ , determine the

motion when w \* n.

(b) If 
$$2 \cos \theta = x + \frac{1}{x}$$
,  $2 \cos \phi = y + \frac{1}{y}$ 

prove that 
$$x^m y^n + \frac{1}{x^m y^n} = 2\cos(m\theta + n\phi)$$
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12. (a) Use De - Moivre's theorem to solve  $x^5 + 1 = 0$ .

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(b) If  $\cos (\theta + i\phi) = R (\cos \alpha + i \sin \alpha)$ 

prove that 
$$\phi = \frac{1}{2} \log \left[ \frac{\sin (\theta - \alpha)}{\sin (\theta + \alpha)} \right]$$

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