# VISVESVARAYA TECHNOLOGICAL UNIVERSITY

"JnanaSangama", Belgaum -590014, Karnataka.



#### LAB RECORD

#### **Bio Inspired Systems (23CS5BSBIS)**

Submitted by

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in partial fulfillment for the award of the degree of

BACHELOR OF ENGINEERING in COMPUTER SCIENCE AND ENGINEERING



B.M.S. COLLEGE OF ENGINEERING (Autonomous Institution under VTU) BENGALURU-560019 Sep-2024 to Jan-2025

#### **B.M.S.** College of Engineering,

**Bull Temple Road, Bangalore 560019** 

(Affiliated To Visvesvaraya Technological University, Belgaum)

#### **Department of Computer Science and Engineering**



#### **CERTIFICATE**

This is to certify that the Lab work entitled "Bio Inspired Systems (23CS5BSBIS)" carried out by **SWAPNIL SAHIL (1BM22CS300)**, who is bonafide student of **B.M.S. College of Engineering**. It is in partial fulfillment for the award of **Bachelor of Engineering in Computer Science and Engineering** of the Visvesvaraya Technological University, Belgaum. The Lab report has been approved as it satisfies the academic requirements of the above mentioned subject and the work prescribed for the said degree.

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Github Link:

https://github.com/Swapnilsahil/BIS-Lab

## Program 1:

Genetic Algorithm

|          | 100.01                                     | Date 03/10/34   |
|----------|--|-----------------|
|          | LAB-01                                     | Page            |
| #        | Genetic Algorithm for optimizat            | ton Problemg:   |
| ->       | Introduction:                              | *               |
|          | A genetic algorithm (GIA) is a             | tune of water   |
|          | tion and search algorithm                  | e inspired b    |
|          | the process of natural sele                | ection and      |
|          | genetics. It belongs to a                  | broader da      |
|          | of algorithms known as                     | evolutionary    |
| 1        | algorithma. GIAs are particu               | losly useful    |
|          | for solving complex problem                | s where         |
|          | traditional methods may                    | not be effect   |
| 14       | Key concepts:                              |                 |
|          | population : A set of cardida              | te solutions    |
|          | the problem:                               | 1000            |
| 2        | chromosome: A representation               | of a solutte    |
|          | often encoded o                            | s a string of   |
|          | or numbers.                                |                 |
| 3        | Fitness Function: A function tha           |                 |
|          | good a soluto                              | 7 4 20 5000     |
| 4        | selection ? The process of                 | choosing the    |
| 1        | fittest individe                           |                 |
| <u> </u> | d. Crossover : Combining part              | & of two man    |
|          | solutions to c                             | reale now offer |
| 6        | . Mutition : Randonly alter<br>solution to | ling parts of   |
|          | genetic dive                               | not maintai     |
|          | genera dive                                | A. A.           |
|          | ·  |                 |
|          |  |                 |

|           | Date   |
|-----------|--|
|           | Andicationa of C.A.                            |
|           | Applications of GAs                            |
|           | Optimization Problems:                         |
|           | GrAs are vaidely used to find optimal solute   |
| -         | in complex spaces, such as:                    |
|           | · Scheduling                                   |
|           | Resource allocation                            |
|           | · TSP (Traveling Salesman Proslem)             |
| . —       | 'Knapsack Problem.                             |
| 7         |  |
| 2         | Machine learning: GIAs can optimise hyperpose. |
|           | meters, select features, and improve           |
| * *       | model performance.                             |
| _         | ,  |
|           | Engineering Design: Used for optimizing design |
|           | parameters in fields like structual            |
|           | engineering, oelospace and                     |
| Fe (S. pr | automothe design.                              |
| 440       | - I  |
| 4.        | Financial Modeling: GAS help in optimizing     |
|           | investment postfolios & predicting             |
|           | market trends.                                 |
| *:        |  |
| 5.        | Grankolotics: Applied in path planning.        |
|           | control systems & robot design                 |
|           | Cordin system x nosti carina                   |
|           |  |
|           |  |
| -         | 7  |
|           |  |
|           | 3 1304 × 7 + 1 3 P                             |
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|           |  |
|           |  |
|           |  |
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|      | Date//   |
|------|--|
| 4    | Travelling Salesman problem (75P).   |
| ~    | Pseudo code  |
| • )  | 1 Bellab Come  |
| 14   | Function calculate-fitness (tour, distance-matrix):  |
|      | total distance: 0  |
|      | For i from 0 to length (tours - 1:   |
|      | to tal-distance += distance-matric [ tou   |
|      | [tour(s+1) med length (-   |
|      |  |
|      | Return total distance.   |
|      | Function tournament selection (population, fit is  |
|      | Stores, tournant &   |
|      | selected = Random sample (population, fitters.   |
|      | · tournaments size)  |
|      | selected: sort (selected by fitney score?  |
| e gr | Return relected TOJ  |
|      | Function order consider (parent: parent:):   |
|      | stre tength (parent)   |
|      | start and = Randomly 40 lock two indice  |
|      | cheld - Array of soils filled soith -1   |
|      | con segment from privatilistant? to  |
|      | child: Array of raise filled noith - 1 copy segment from parenti (start) to parent [end] into child[start] to an |
|      |  |
|      | current pos: (end+1) mod size '  Fox each city in parentz:  If city not in child:  child [current pos]: city     |
|      | Cox each city in parents:  |
|      | if city not in child:  |
|      | child [curent pox ] = city   |
|      | current pos = (current-pos 41)   |
|      | Return child   |
|      |  |
|      |  |

|      | Date!  Page   |
|------|---|
|      | Function supp, mutation (treat, mutation rate)        |
|      | If randome! < mutation-rate:                          |
|      | idx1, idx2 = Randomly select to                       |
|      | indice from tour                                      |
|      | SWAP tows [idx1] & tows [idx]                         |
|      | Coites, population size, generations, multi-          |
|      | TOR.  |
|      | distance matrix = calculate: distance matrix (cities) |
| -    | population: Initialize random tours.                  |
|      | For generation from 1 to generations                  |
|      | THOM SCORES : C. / Patrical - Tithes                  |
| -    | 11 input  |
| _    | coords = np. random. rand (num-citres, 2) \$100       |
|      | City coordinates:                                     |
|      | city 0: (23.45, 67.89)                                |
|      | city " . [12-34, 45.67).                              |
|      | City 2 . (78,90, 12.34)                               |
| . ·  | city 3: (56.78, 90.12)                                |
| _    | city 4: (34.56, 23.45)                                |
|      | 0   |
|      | "output: ·  |
|      | Best Tour: [0,4,1,3,2]                                |
|      | Best Distance: 215.67                                 |
| -    | - B - C - C - C - C - C - C - C - C - C               |
| . 74 |   |
| -    |   |
|      |   |
|      |   |
|      |   |

```
import random
import numpy as np
import math
def generate cities(num cities):
  return [(random.randint(0, 100), random.randint(0, 100)) for in range(num cities)]
def compute distance matrix(cities):
  num cities = len(cities)
  distances = [[0] * num cities for in range(num cities)]
  for i in range(num cities):
    for j in range(num cities):
       if i != i:
          distances[i][j] = math.sqrt(
            (cities[i][0] - cities[j][0])**2 + (cities[i][1] - cities[j][1])**2
  return distances
class TSP:
  def init (self, distances):
    self.distances = distances
    self.num cities = len(distances)
  def fitness(self, route):
    total distance = sum(
       self.distances[route[i]][route[i + 1]] for i in range(len(route) - 1)
    total distance += self.distances[route[-1]][route[0]]
class GeneticAlgorithm:
  def init (self, tsp, population size=100, generations=500, mutation rate=0.1):
    self.tsp = tsp
    self.population size = population size
    self.generations = generations
    self.mutation rate = mutation rate
    self.population = self. initialize population()
```

```
def initialize population(self):
     return [random.sample(range(self.tsp.num_cities), self.tsp.num_cities) for _ in
range(self.population size)]
  def select parents(self):
     fitnesses = [self.tsp.fitness(route) for route in self.population]
     total fitness = sum(fitnesses)
     probabilities = [f / total fitness for f in fitnesses]
     return random.choices(self.population, probabilities, k=2)
  def crossover(self, parent1, parent2):
     size = len(parent1)
     start, end = sorted(random.sample(range(size), 2))
     child = [-1] * size
     child[start:end] = parent1[start:end]
     p2 idx = 0
     for i in range(size):
       if child[i] == -1:
          while parent2[p2 idx] in child:
            p2 idx += 1
          child[i] = parent2[p2 idx]
     return child
  def mutate(self, route):
     if random.random() < self.mutation rate:
       i, j = random.sample(range(len(route)), 2)
       route[i], route[i] = route[i], route[i]
  def evolve(self):
     for in range(self.generations):
       new population = []
       for in range(self.population size):
          parent1, parent2 = self. select parents()
```

```
child = self. crossover(parent1, parent2)
         self. mutate(child)
         new population.append(child)
       self.population = new population
  def get best solution(self):
    best route = min(self.population, key=lambda route: 1 / self.tsp.fitness(route))
    best distance = 1 / self.tsp.fitness(best route)
    return best route, best distance
if __name__ == "__main__":
  num cities = 5
  cities = generate cities(num cities)
  distances = compute distance matrix(cities)
  print("City Coordinates:")
  for i, city in enumerate(cities):
    print(f"City {i}: {city}")
  tsp = TSP(distances)
  ga = GeneticAlgorithm(tsp, population size=50, generations=100, mutation rate=0.2)
  ga.evolve()
  best route, best distance = ga.get best solution()
  print("\nBest route:", best route)
  print("Best distance:", best distance)
```

## Program 2:

Particle Swarm Optimization

|          | Dote 2 4, 10, 24   |
|----------|--|
| - 1      | LAB-02 Poge  |
| A        | Practicle Swarm Optimization for function Optimation:                                  |
|          | 01 216 1   |
|          | Realistics Commentation of   |
| zueb-i:  | Algorithm: Randomly initialize snown population of N particles XI (i=1,2               |
| 1 tep 2: | select hyperparameter values no, (1862   |
| step3    | For I ter in range (max iter):   |
|          | For i'm range (mox. iter):  For i'm range (N):  a. Compute new velocity of ith postèle |
|          | a. Compute new velocity of ith posticle  |
|          | snorm [i]. velocity  |
|          | was warm it. velocity +  |
|          | TIACIN (Swarmti7, best pos-  |
|          | swarmtil position)+  |
|          | *2 * C2 * (best_pos_c warm -   |
|          | a warm [i]. position   |
|          | 1 1 24   |
| 7        | be compute new position of ith particle  |
|          | using its new relocity swarming.   |
|          | using its new relocity swarmfit.  Swarm [i]. position + : Swarm Fit. velocit           |
|          |  |
|          | c. It position is not in range (minx, mas)   |
| -        | then clip it   |
| 1        | if swarmtill-position eminx:   |
| -        | Sworm [: I. position: minx   |
| -        | elif swarm (i] parter > maxx.  |
| +        | susarm [:1. position: maxx   |
| +        | d. update new best of this particle  |

| DatePage                                 |
|--|
| and new best of swarm                    |
| - if swaIngergitive to scaling of dun    |
| variables. rm[i]. fitness swarm[i]       |
| best fitners!                            |
| swarm[i]. best fitners = swarm[i]. the   |
| swarm[i]. best pos - swarm[i]. position  |
|  |
| if cwarm[i]. fit new < best fitness worn |
| best-filmer - soum = sween(i). film      |
| best pos swarms coverm Til. position     |
| - End-for                                |
| Cond-for                                 |
| Slocks Colored Later A                   |
| Step4: Return best particle of Curam     |
| Program !                                |
| // input!                                |
| objective function: $m^2 + y^2$          |
| · dimension 9:2                          |
| · iterations: 100                        |
| · population gize: 50                    |
| · w : 0.7 (Inestia weight)               |
| · Contitue carameter / 1. 4              |
| 110/p 24                                 |
| man.                                     |
| 110/p                                    |
|  |
| Best position found: [4.0479, -2.23363]  |
| Best value found: 2.1374591              |
|  |
|  |
|  |
|  |

```
import random
import numpy as np
def objective function(position):
  """The function to be minimized."""
  x, y = position
  return x^{**}2 + y^{**}2
def pso(objective function, dimensions, iterations, population size, w=0.7, c1=1.4, c2=1.4):
  particles = []
  for in range(population size):
    position = np.random.uniform(-10, 10, dimensions)
    velocity = np.random.uniform(-1, 1, dimensions)
    particles.append({
       'position': position,
       'velocity': velocity,
       'best position': position.copy(),
       'best value': objective function(position)
     })
  global best position = particles[0]['best position'].copy()
  global best value = particles[0]['best value']
  for in range(iterations):
    for particle in particles:
       r1 = random.random()
       r2 = random.random()
       particle['velocity'] = (w * particle['velocity'] +
                       c1 * r1 * (particle['best position'] - particle['position']) +
                       c2 * r2 * (global best position - particle['position']))
       particle['position'] = particle['position'] + particle['velocity']
       particle['position'] = np.clip(particle['position'], -10, 10)
```

```
value = objective_function(particle['position'])

if value < particle['best_value']:
    particle['best_value'] = value
    particle['best_position'] = particle['position'].copy()

if value < global_best_value:
    global_best_value = value
    global_best_position = particle['position'].copy()

return global_best_position, global_best_value

dimensions = 2
iterations = 100
population_size = 50

best_position, best_value = pso(objective_function, dimensions, iterations, population_size)
print(f"Best position found: {best_position}")
print(f"Best value found: {best_value}")</pre>
```

## Program 3:

Ant Colony Optimization

|    | LAB-03 Page  |
|----|--|
| -£ |  |
|    | Ant colony Optimization for Traveling sales problem.                                 |
|    | (Austea)   |
| -> | Algorithm:   |
|    | initialize pheromone value Vi, je[1,n]:Tij >7  |
|    | repeat   |
|    | for each ant LECI, m ] do  |
|    | initalize selection set s > \$1, n}  |
|    | randomly choose starting city io € & for move to starting city i → io while 5 ± 0 do |
|    | move to steering city i - 10   |
|    | while 5 ± 0 do   |
|    | remove current city from selection   |
|    | set 5-5/913  |
|    | charge next city jin tour with   |
|    | probability Pij. Tij. Mij  |
|    | E cin. nin   |
|    | NES  |
|    | update solution rector stills > j  |
|    | more to new city i +j  |
|    | end while  |
|    | finalize solution vector stylibile   |
|    | end for  |
|    | for each solution Te, 1 = \$1, m3 do  calculate tourlength f(Ty) -> Ediry            |
|    | calculate tourlength prints 2017   |
|    | end for  |
|    |  |
|    | evaporate pheronone Zij + (1-p). Zij   |
|    | for all (i.j) do  evaporate pheronone zij -> (1.p).zij  end for                      |
|    |  |
|    |  |

|   |  |             | Date    |
|---|--|-------------|---------|
|   |  | · · · · · · | Page    |
| - |  |             |         |
|   | Steration 60: Ber                      | t rength:   | D 7.88  |
|   | Iteration 60: Ber<br>Iteration 70: Ber | t leigth:   | 77.88   |
|   | Iteration 80: Bes                      | t length.   | 38.46   |
|   | Iteration 80: Bes                      | t length:   | 88.EF   |
|   |  | 9           |         |
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|   | 3)                                     | 281         |         |
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|   |  | (90)        |         |

```
Code:
```

```
import numpy as np
import random
import matplotlib.pyplot as plt
# Define constants for the algorithm
NUM ANTS = 50
NUM CITIES = 20 # Now we have 20 cities
ALPHA = 1.0 \# Influence of pheromone
BETA = 2.0 # Influence of distance
RHO = 0.1 # Pheromone evaporation rate
            # Pheromone deposit constant
MAX ITER = 100 # Maximum number of iterations
# Predefined 20 cities (coordinates in 2D space)
def generate cities():
  cities = np.array([
    [5, 10], [11, 5], [14, 9], [12, 15], [8, 13], # Cities 0-4
    [10, 10], [13, 7], [16, 5], [14, 3], [18, 6], # Cities 5-9
    [4, 2], [7, 1], [8, 5], [6, 7], [4, 10], # Cities 10-14
    [15, 18], [12, 17], [3, 18], [17, 12], [19, 8] # Cities 15-19
  1)
  return cities
# Compute the distance matrix
def compute distance matrix(cities):
  num cities = len(cities)
  distance matrix = np.zeros((num cities, num cities))
  for i in range(num cities):
    for j in range(i + 1, num cities):
       dist = np.linalg.norm(cities[i] - cities[j])
       distance matrix[i, j] = dist
       distance matrix[j, i] = dist
  return distance matrix
# Initialize pheromone matrix
definitialize pheromone matrix(num cities):
```

```
pheromone matrix = np.ones((num cities, num cities)) # Pheromone starts as 1 for all
edges
  np.fill diagonal(pheromone matrix, 0) # No pheromone on the diagonal (self-loops)
  return pheromone matrix
# Calculate the total length of a tour
def calculate tour length(tour, dist matrix):
  length = 0
  for i in range(len(tour) - 1):
    length += dist matrix[tour[i], tour[i + 1]]
  length += dist matrix[tour[-1], tour[0]] # Returning to the start
  return length
# Ant solution construction (probabilistic decision on next city)
def construct solution(num cities, pheromone matrix, dist matrix):
  tour = [random.randint(0, num cities - 1)] # Start from a random city
  visited = set(tour)
  while len(tour) < num cities:
    current city = tour[-1]
    probabilities = []
    for next city in range(num cities):
       if next city not in visited:
          pheromone = pheromone matrix[current city, next city] ** ALPHA
         distance = (1.0 / dist matrix[current city, next city]) ** BETA
          probabilities.append(pheromone * distance)
       else:
          probabilities.append(0)
    total prob = sum(probabilities)
    probabilities = [p / total prob for p in probabilities]
    # Choose the next city based on the probabilities
    next city = np.random.choice(range(num cities), p=probabilities)
    tour.append(next city)
    visited.add(next city)
  return tour
```

```
# Update the pheromone matrix based on the solutions found by ants
def update pheromone(pheromone matrix, all tours, dist matrix, best tour):
  # Evaporate pheromone
  pheromone matrix *= (1 - RHO)
  # Add pheromone for all ants
  for tour in all tours:
    tour length = calculate tour length(tour, dist matrix)
    for i in range(len(tour) - 1):
       pheromone matrix[tour[i], tour[i + 1]] += Q / tour length
    pheromone matrix[tour[-1], tour[0]] += Q / calculate tour length(tour, dist matrix)
  # Add pheromone for the best tour
  best length = calculate tour length(best tour, dist matrix)
  for i in range(len(best tour) - 1):
    pheromone matrix[best tour[i], best tour[i + 1]] += Q / best length
  pheromone matrix[best tour[-1], best tour[0]] += Q / best length
# Main ACO algorithm for solving TSP
def ant colony optimization(num cities, dist matrix, pheromone matrix, max iter):
  best tour = None
  best tour length = float('inf')
  # Main loop
  for iteration in range(max iter):
    all tours = []
    # Step 1: All ants construct their solutions
    for in range(NUM ANTS):
       tour = construct solution(num cities, pheromone matrix, dist matrix)
       all tours.append(tour)
       tour length = calculate tour length(tour, dist matrix)
       # Step 2: Update the best tour if necessary
       if tour length < best tour length:
         best tour = tour
         best tour length = tour length
```

```
# Step 3: Update pheromone matrix
    update pheromone(pheromone matrix, all tours, dist matrix, best tour)
    # Optional: print progress every 10 iterations
    if iteration \% 10 == 0:
       print(f"Iteration {iteration}: Best tour length = {best tour length:.2f}")
  return best tour, best tour length
# Main Execution
if __name__ == "__main__":
  # Step 1: Generate predefined cities and distance matrix
  cities = generate cities()
  dist matrix = compute distance matrix(cities)
  # Step 2: Initialize pheromone matrix
  pheromone matrix = initialize pheromone matrix(NUM CITIES)
  # Step 3: Run ACO algorithm
  best tour, best tour length = ant colony optimization(NUM CITIES, dist matrix,
pheromone matrix, MAX ITER)
  # Step 4: Output the best tour and visualize it
  print(f"Best tour length: {best tour length:.2f}")
```

Program 4:

Cuckoo Search Algorithm

|           | LAB-04                | Date! 4 , 11<br>Page |
|-----------|-----------------------|----------------------|
| * cuckeo  | search Algorithm      |                      |
| Algorith. | ν.:                   |                      |
| Initiali  | e population of n     | cuchoos .            |
| Evalua    | e fitness of such     | cukoo                |
| 11 Inpu   |                       |                      |
| 11 n=     | initial population se | 26                   |
|           | fraction of worse     |                      |
|           | and replaced          |                      |
| 11 Max    | iterations: the maxim | um no of ites        |
| 11 -f =   | the objective of a t  | o optimize ()        |
| 11 outp.  | d .                   |                      |
| 11 Tex    | best alution for      | -d·                  |
| Grenera   | e the initial popul   | lation of nh         |
|           | X: (1:1, 2, n)        | 7                    |
| while     | + < Max iterations:   |                      |
| Cre       | t a cucken randon     | fitness Fi           |
| js        | -choose a nest a      | mong n rounds        |
| ٠٠        | E: > E; :             |                      |
|           | Replace ; by the      | new courtien         |
|           | 1 3                   |                      |
| i-f d     | fraction (Pa) of      | warke notte          |
| also      | adoned and new        | once are buil        |
|           | keep the best o       | alutiona             |
|           | Rank the solution     | ns and And +         |
| Doct ac   | en tesulte and i      | 1                    |

|      | Page   |
|------|--|
| #    | Application Name: Traffic signal Optimization        |
|      | Inputs:  |
|      | dimensions (number of interactions): dim: 3          |
|      | bounds (Range of green light time): (10,10           |
|      | max iter ( the max" no. of iterations) : 100         |
|      | pa (probability of abandoning the ! 0.) worst nests) |
|      | Cambda ( The parameter of Cery flight: 1.2           |
|      | step size.   |
|      | ,  |
|      | 11 output:   |
|      | 11 output:<br>best solution: [90.5, 110.3, 75.8]     |
|      |  |
|      | best-fitnes: 325.5 (total waiting thm                |
|      |  |
|      | geo.   |
|      | 0/8 (64)   |
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Date \_\_/\_\_/\_\_

```
#cuckoo search(Traffic Signal Optimization)
import numpy as np
from scipy.special import gamma
def fitness function(x):
  waiting times = np.array([10 + (x[i] ** 2) / 100 \text{ for } i \text{ in range}(len(x))])
  total waiting time = np.sum(waiting times)
  return total waiting time
def levy flight(dim, beta=1.5):
  sigma u = np.power((gamma(1 + beta) * np.sin(np.pi * beta / 2) /
              gamma((1 + beta) / 2) * beta * (2 ** (beta - 1)), 1 / beta)
  u = np.random.normal(0, sigma u, dim)
  v = np.random.normal(0, 1, dim)
  step = u / np.power(np.abs(v), 1 / beta)
  return step
def cuckoo search(dim, bounds, num nests, max iter, p a=0.25, Lambda=1.5):
  nests = np.random.uniform(bounds[0], bounds[1], (num nests, dim))
  fitness = np.array([fitness function(nest) for nest in nests])
  best idx = np.argmin(fitness)
  best nest = nests[best idx]
  best fitness = fitness[best idx]
  for iter in range(max iter):
     new nests = np.copy(nests)
     for i in range(num nests):
       step = levy flight(dim, Lambda)
       new nests[i] = nests[i] + step
       new nests[i] = np.clip(new nests[i], bounds[0], bounds[1])
```

```
new fitness = np.array([fitness function(nest) for nest in new nests])
     for i in range(num nests):
       if new fitness[i] < fitness[i]:
         nests[i] = new nests[i]
         fitness[i] = new fitness[i]
     if np.random.rand() < p a:
       random idx = np.random.randint(num nests)
       nests[random_idx] = np.random.uniform(bounds[0], bounds[1], dim)
       fitness[random idx] = fitness function(nests[random idx])
     current best idx = np.argmin(fitness)
     current best fitness = fitness[current best idx]
     if current best fitness < best fitness:
       best fitness = current best fitness
       best nest = nests[current best idx]
  return best nest, best fitness
dim = 3
bounds = [10, 120]
num nests = 20
max iter = 100
best solution, best value = cuckoo search(dim, bounds, num nests, max iter)
print("\n--- Best Solution ---")
print("Green Light Timings (seconds):", best solution)
print("Best Fitness Value (Total Waiting Time):", best value)
```

Program 5:

Grey Wolf Optimization

|               | Date 21 /11                                  |
|---------------|--|
|               | LAB-05                                       |
| 112.00        |  |
| 1             | Grey walf optimization:                      |
|               | 0  |
| •             | A'gan'thm                                    |
|               | Initialize population of wolves with ran     |
|               | paytren.                                     |
|               | initialize a , B , & position & their fitner |
|               |  |
|               | for each iteration from 1 to max             |
|               | for each wolf i in population                |
|               | if fitnew(i) > fitnew(a)                     |
|               | updake a position                            |
|               | else if fitness (i) & fitnes                 |
| -             | update a position                            |
| -             | else if fitnes (is > fitnes                  |
| -             | update & position                            |
| $\rightarrow$ |  |
| -             | for each wolfin population                   |
| -             | calculate a, B, & distan                     |
| -             | applace position of wolf u                   |
| -             | X:= x:+ A=D(a), A=)                          |
| +             | AN   |
| -             | • A  |
| +             | if position is outside bou                   |
| +             | Adjust position to                           |
| +             | neithin bounds                               |
| +             |  |
| -             | return best solution found ( a position      |
| +             | Citney)                                      |
|               | to be divers                                 |
| +             | B-1 2 nd best fitness                        |
| +             | B-1 2nd best fitner                          |
| -             | 8 -s tourd west fitness . v: = x:+A.         |

| _11 | Application: water distribution optimization                      |
|-----|---|
|     | Inpuls:   |
| ,   | Number of wolves: 30  |
|     | Maximum iterations: 100   |
|     | Number of nodes: 5  |
|     | Demand at each node: [50,40,30,60,80]                             |
|     | · Pipe costs : (1,2,1.5,3,2] · pump costs : [0.1,0.1,0.1,0.1,0.1] |
|     | · pump costs : [0.1, 0.1, 0.1, 0.1, 0.1]                          |
|     |   |
|     | 11 pertput:   |
|     | E.  |
|     | Best Pipe Stree: [0,703, 0.734, 0.586, 0.483, 1.89]               |
|     | Best Flow Rater: (0.884, 1.045, 1.117, 10.810, 1.385              |
|     |   |
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```
import numpy as np
import matplotlib.pyplot as plt
def objective function(pipe sizes, flow rates, demand, node pressure, pipe costs,
pump costs):
  pipe cost = np.sum(pipe sizes ** 2 * pipe costs)
  pump cost = np.sum(flow rates * pump costs)
  pressure penalty = 0
  for i in range(len(node pressure)):
    if node pressure[i] < 20:
       pressure penalty += (20 - node pressure[i]) ** 2
  demand penalty = 0
  for i in range(len(demand)):
    if flow rates[i] < demand[i]:
       demand penalty += (demand[i] - flow rates[i]) ** 2
  total cost = pipe cost + pump cost + pressure penalty + demand penalty
  return total cost
class GreyWolfOptimization:
  def init (self, num wolves, max iter, demand, pipe costs, pump costs,
num nodes):
    self.num wolves = num wolves
    self.max iter = max iter
    self.demand = demand
    self.pipe costs = pipe costs
    self.pump costs = pump costs
    self.num nodes = num nodes
    self.wolves = np.random.rand(self.num wolves, 2 * self.num nodes)
```

```
self.alpha = None
     self.beta = None
     self.delta = None
     self.alpha score = float('inf')
     self.beta score = float('inf')
     self.delta score = float('inf')
  def fitness(self, wolf):
     pipe sizes = wolf[:self.num nodes]
     flow rates = wolf[self.num nodes:]
     node pressure = np.random.rand(self.num nodes) * 50
     return objective function(pipe sizes, flow rates, self.demand, node pressure,
self.pipe costs, self.pump costs)
  def update positions(self):
     for i in range(self.num wolves):
       A = 2 * np.random.rand(1) - 1
       C = 2 * np.random.rand(1)
       D alpha = np.abs(C * self.alpha - self.wolves[i])
       X1 = self.alpha - A * D alpha
       A = 2 * np.random.rand(1) - 1
       C = 2 * np.random.rand(1)
       D_beta = np.abs(C * self.beta - self.wolves[i])
       X2 = self.beta - A * D beta
       A = 2 * np.random.rand(1) - 1
       C = 2 * np.random.rand(1)
       D_delta = np.abs(C * self.delta - self.wolves[i])
       X3 = self.delta - A * D delta
```

```
self.wolves[i] = (X1 + X2 + X3) / 3
  def optimize(self):
     for in range(self.max iter):
       for i in range(self.num wolves):
         fitness value = self.fitness(self.wolves[i])
         if fitness value < self.alpha score:
            self.alpha score = fitness value
            self.alpha = self.wolves[i]
          elif fitness value < self.beta score:
            self.beta score = fitness value
            self.beta = self.wolves[i]
          elif fitness value < self.delta score:
            self.delta score = fitness value
            self.delta = self.wolves[i]
       self.update positions()
     return self.alpha
num wolves = 30
max iter = 100
num nodes = 5
demand = np.array([50, 40, 30, 60, 80])
pipe costs = np.array([1, 2, 1.5, 3, 2])
pump costs = np.array([0.1, 0.1, 0.1, 0.1, 0.1])
gwo = GreyWolfOptimization(num wolves, max iter, demand, pipe costs, pump costs,
num nodes)
best solution = gwo.optimize()
best pipe sizes = best solution[:num nodes]
best flow rates = best solution[num_nodes:]
print("Best Pipe Sizes:", best pipe sizes)
print("Best Flow Rates:", best flow rates)
```

## Program:6

Parallel Cellular Algorithms and Programs

|   | LAB-06                                       |                 | Date 28 / 11 / 21 |
|---|--|-----------------|-------------------|
| * | Parallel Celular Alge                        | orithms and     | Program           |
| • | Paeudocodes:                                 |                 | 9                 |
|   | # constants                                  | 372             |                   |
|   | Giral width = N                              | м д             |                   |
|   | Gind Height : M                              |                 |                   |
|   | Max Generations - T                          |                 |                   |
|   | 981  |                 |                   |
|   | # Initialize grad (rand                      | lam O ox 1)     |                   |
|   | # Initialize grad (rand                      | (Gind-width     | , Gind Hoig       |
|   | 9  |                 | . 0               |
|   | I count i've neighbour                       |                 |                   |
|   | function count we Ne                         | ighbours ( grid | , 1, 1):          |
|   | live neighbour                               | S1-0            | - P               |
|   | for each neigh                               | Libour (n,y)    | f(1,1):           |
|   | if and                                       | [x][y]          | 10.               |
|   | ٠ ت ا  | e noigh bours   | 4= 1              |
|   | seturn live_r                                | ^ /             |                   |
|   |  | U               |                   |
|   | Apply Grame of life                          | rulal           |                   |
|   | function ApplyRules ( 9                      | nd iii          |                   |
|   | live neighbors = 8                           | butting Neight  | sors (qu'd,       |
|   | of gratistis=                                | -1/             | 3                 |
|   | return 1                                     | if live reigen  | word = 1 0        |
|   |  |                 | elso O            |
|   | else:  |                 |                   |
|   | return 1 of                                  | live neighbo    | rs=:3 else        |
|   |  | 0               |                   |
|   | tupdate and paralle                          | I undate for    | s all rell        |
| 0 | unction voolate and a                        | rids!           |                   |
|   | tupdate grid paralle<br>unction update and g | ex Grid (and)   |                   |
|   |  | 9               |                   |
|   |  |                 |                   |

|      |  |                                 |        |        |       |          |  |      |       | Date<br>Page |     |  |
|------|--|---------------------------------|--------|--------|-------|----------|--|------|-------|--------------|-----|--|
|      |  | 2.9                             |        | °n     | rang  | e (c     | , Gry  | id-  | heig  | nd):         |     |  |
|      |  | for i in range (0, ound width): |        |        |       |          |  |      |       |              |     |  |
|      | for i in range (0, orid-height):  for i in range (0, orid-height):  new grid (13[j]: Apply Rules (grid,i)) |                                 |        |        |       |          |  |      |       |              |     |  |
|      |  |                                 |        |        |       |          |  |      |       |              |     |  |
|      |  | re                              | two    | ne     | 2-9   | nd       |  |      |       |              |     |  |
|      |  |                                 | 100    |        |       | ,        |  |      |       |              |     |  |
| 14   | Tone   | oleme                           | n to t | 100    | lora  | me d     | of U   | le s | ules  | )            |     |  |
| **   | 117  | nput                            | !      |        |       |          | 1  | ]    |       |              |     |  |
|      | Gri  | d- 20                           | 4 dth  | :10    |       |          |  |      |       |              |     |  |
|      |  | d- He                           |        |        |       |          |  |      | ,     |              |     |  |
|      | No   | w - 9                           | enen   | ation: | 20    |          |  |      |       |              |     |  |
|      |  |                                 | 10.00  |        |       | 16       | <u>.                                    </u> |      | 20. 4 |              |     |  |
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|      | 0  | 0                               | 1      | 1      | 0     | 1 .      | 0  | ,    | 1     | 0            |     |  |
|      | 0  | 0                               | 1      | 0      | Ī     | 0        | 0  | 0    | 0     | 0            | 31  |  |
|      | - 1  | 0                               | 1      | 0      | 0     | 0        | 1  | 0    | 0     | 0            |     |  |
| 1    | 1  | 0                               | 0      | 0      | 0     | 0        | _!_  | 1    | 0     | 00           |     |  |
| -    | 1  | 0                               | 1      | 0      | 0     |          | 1  | 0    | 0     | 0            | 538 |  |
|      | 0  | 0                               | 1      | 0      | . 0   | 0        | 0  | 0    | 1     | 0            |     |  |
| )    | 1  | 0                               | 0      | 1      | 0     | 1        | 0  | 0    | O     | 0            |     |  |
| 1    | 0  |                                 | t      | 1      | 1     | 1        | 1  | 0    | 0     | 0            |     |  |
|      |  |                                 |        | A .    |       |          |  |      |       |              |     |  |
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| 1 19 | 124  | Al. an                          | a her  | ol     | alive |          |  | 39   |       |              | 6.3 |  |
| 2    | 0  | TALL.                           |        |        | ~~~   |          |  |      |       |              |     |  |
|      |  |                                 |        |        |       |          |  |      |       | 207          |     |  |
| -    |  |                                 |        |        |       |          |  |      |       |              |     |  |
|      |  |                                 |        |        |       |          |  |      |       | •            |     |  |

```
Code:
#Parallel Cellular Algorithm n programs
import random
import copy
GRID WIDTH = 10
GRID HEIGHT = 10
MAX GENERATIONS = 20
definitialize grid(width, height):
  return [[random.randint(0, 1) for in range(width)] for in range(height)]
def count live neighbors(grid, i, j):
  live neighbors = 0
  directions = [(-1, -1), (-1, 0), (-1, 1),
          (0, -1), (0, 1),
          (1, -1), (1, 0), (1, 1)
  for dx, dy in directions:
    x = (i + dx) \% len(grid)
    y = (j + dy) \% len(grid[0])
    live neighbors += grid[x][y]
  return live neighbors
def apply rules(grid, i, j):
  live neighbors = count live neighbors(grid, i, j)
  if grid[i][j] == 1:
    return 1 if live neighbors == 2 or live neighbors == 3 else 0
  else:
    return 1 if live neighbors == 3 else 0
def update grid(grid):
```

```
new grid = copy.deepcopy(grid)
  for i in range(len(grid)):
    for j in range(len(grid[0])):
       new grid[i][j] = apply rules(grid, i, j)
  return new grid
def display grid(grid):
  for row in grid:
    print(' '.join(str(cell) for cell in row))
  print("\n" + "="*20 + "\n")
def count alive cells(grid):
  return sum(sum(row) for row in grid)
def game of life(grid width, grid height, max generations):
  grid = initialize grid(grid width, grid height)
  print("Initial Grid:")
  display grid(grid)
  for generation in range(max generations):
    print(f''Generation {generation + 1}:")
    grid = update grid(grid)
    # display grid(grid)
    alive_cells = count_alive_cells(grid)
    print(f"Number of alive cells: {alive cells}")
if name == " main ":
  game of life(GRID WIDTH, GRID HEIGHT, MAX GENERATIONS)
```

**Program 7:** Optimization via Gene Expression Algorithm

|     | Date 19                                       |
|-----|---|
| -   | [A8-07  |
| *   | Gene Expression Algorithms (GIEA)             |
| ±1  | Algarithm:                                    |
| P.  | Define the Problem                            |
| _   | Define the optimization problem and o         |
|     |   |
|     | Example: fcx) - reininize or Moximize         |
| 2   | Initialize Parameters                         |
|     | Set Population Size                           |
| _   | Set Number of Grenes (length of Grenotte &    |
|     | Set Mutation Rate                             |
| _   | Set Crossover-Rate                            |
|     | get nox - Generations (Number of Eterations   |
| 3   | Initialize Population                         |
| -   | For each individual i in topulation - 520     |
|     | Generale a random genetic sequence (lo        |
|     | Store the genetic sequence in Popular         |
| Ce. | Evaluate Litness                              |
|     | For each individual i in Population:          |
|     | Translate the genetic requerce into a a       |
|     | (Grene Ex presuis                             |
|     | Compute fitnose using the objective fund      |
| -   | store the fitner value ofor Endividual        |
| 5:  | Iterate Until Stopping Criteria               |
|     | For generation in range (1, Max Goverations): |
|     | a selection:                                  |
|     | - Select individuals based on fitners         |
|     | Roulette whool or Tordinarat colortia         |
|     | - Store belocted individuale or noting. Por   |
| 500 |   |

| perform croccover to produce offepring Add offepring to New Population.  C. Mutation:  - For each individual in New Population for each gene in the genetic sequence with probability nutation. Pate:  Randomly after the genetical intro variation.  Translate the genetic sequence into a solution  compute the fitness using the objectic fit.  e. Replacement:  |   | - For each part of individuals in Meeting. 120 |
|---|---|--|
| - For each pair of individual in Mean Population  c Mutation!  - For each individual in New Population  for each gene in the genetic sequence into a variate  - For each individual in New Population.  Randomly after the gene into a variate  d. Gene Expection  - For each individual in New Population:  Translate the genetic sequence into a solution  compute the fitness using the objectic fit.  e. Replacement:  - Deplace the old population with New Population  f. Trade Best Solution  - Update the heat solution found so for based on fitness   |   | - For each part of individuals in Meeting. 120 |
| perform eroscover to produce perform eroscover to produce offspring to New Population and offspring to New Population.  - For each individual in New Population Port oach gene in the genetic sequence with probability neutation. Part Population.  - For each individual in New Population.  - For each individual in New Population.  - For each individual in New Population.  - Translate the genetic sequence into a solution compute the fitness using the objection fit.  - Replacement:  - Replacement:  - Populate the old population with New Population.  - Update the heat solution found so for based on fitness. |   | with protability croscover Rate                |
| perform croccover to produce offspring and offspring to New Population.  C Mutation:  - For each individual in New Population.  For each pere in the genetic sequence into a variate the genetic sequence into a solution  - For each individual in New Population.  Translate the genetic sequence into a solution  compute the fitness using the objective fit.  • Replacement:  - Replacement:  - Paplace the old population with New Population.  Track Best Salution  - Update the best solution found so for based on fitness   |   |  |
| offspring Add offspring to New Population:  - For each individual in New Population  For each gene in the genetic sequence into production and the personal acts the genetic sequence into a constant the genetic sequence into a solution  compute the fitness using the objectic fit experients of the Replacement:  - Replacement:  - Replacement:  - Populate the old population with New Population  f. Track Best Solution  - Update the best solution found so for based on fitness  |   | perform croccover to produce                   |
| c. Mutation!  - For each individual in New Population for each gene in the genetic sequence in the genetic sequence in the percentage of the probability neutration. Participantly after the genetiation.  - For each individual in New Population.  - For each individual in New Population.  - Translate the genetic sequence into a solution  compute the fitness using the objects fit e. Replacement:  - Replacement:  - Replacement:  - Paplace the old population with New Population.  - Update the best solution found so for based on fitness.  |   |  |
| - For each individual in New Population  For each gene in the genetic sequence in the probability nutation. Pate:  Randomly acted the geneticity nutation.  Variation  - For each individual in New Population.  Translate the genetic sequence into a solution  compute the fitness using the objectic fit.  e. Replacement:  - Replacement:  - Replacement old population with New Population.  Tracks Best Solution  - Update the best solution found so fer based on fitness.   |   | Add offspring to New Population                |
| For each gene in the genetic sequence in the probability relation. Pate:  Randomly after the genetiation  Valiation  Translate the genetic sequence into a solution  compute the fitness using the objector fit.  e. Replacement:  - Replacement:  - Deplace the old population with New Sopulation  f. Track Best Solution  - Update the best solution found so for based on fitness   |   | c Mutation!                                    |
| For each gene in the genetic sequence neith probability neutation. Pate:  Randomly after the genetiation  d. Gierre Expression  - For each individual in Now. Population:  Translate the genetic sequence into a solution  compute the fitness using the objector fit.  e. Replacement:  - Deplace the old population with New Sopulation  f. Trade Best Solution  - Update the best solution found so for based on fitness   |   | - For each individual in New-Population        |
| Randomly after the genelintro  Pardomly after the genelintro  variate  d. Gierre Expression  - For each individual in now-Population:  Translate the genetic sequence into a solution  compute the fitness using the objectic fits  e. Replacement:  - Poplace the old population with Now-Population  f. Trada Best Solution  - Update the best solution found so for based on fitness   |   | for each gene in the genetic sequen            |
| Randomly alter the gene lintro  variation  - For each individual in Non-Population:  Translate the genetic sequence into a  solution  compute the fitness using the objectic fit  e. Replacement:  - Paplace the old population with Non-Population  f. Trada Best Solution:  - Update the best solution found so for  based on fitness  6. Output the pest solution  |   | with probability ruletion, tate.               |
| d. Giero Expression '  - For each individual in New-Population:  Translate the genetic sequence into a solution  compute the fitness using the objectic fit e. Replacement:  - Replacement:  - Replacement:  - Deplace the old population with New-Population of Trade Best Solution '  - Update the best solution found so for based on fitness  6. Output the pest solution   | _ | Randomly after the genelintro.                 |
| - For each individual in Now-Population:  Translate the genetic sequence into a solution  compute the fitness using the objector fit e. Replacement:  - Replacement:  - Replacement old population with New-Population in the content of the population of the population of the population of the based on fitness.  6. Output the past solution   |   | vauati   |
| - For each individual in New-Population:  Translate the genetic sequence into a solution  compute the fitness using the objector fit e. Replacement:  - Replacement:  - Replacement:  - Peplace the old population with New-Population in the new Population of the population found so for based on fitness.   | 1 |  |
| compute the fitness using the objective fits  e. Replacement:  - Replacement:  - Replace the old population with New Population  f. Tracks Best Solution:  - Update the best solution found so for based on fitness  6. Output the pert solution  | 1 | d. Giero Expression                            |
| compute the fitness using the objective fits  e. Replacement:  - Replacement:  - Replace the old population with New Population  f. Tracks Best Solution:  - Update the best solution found so for based on fitness  6. Output the pert solution  | 1 | - For each individual in New-Population:       |
| compute the fitness using the objective fit  e. Replacement:  - Replacement:  - Replacement:  - Replace the old population with New Population  f. Track Best Solution:  - Update the best solution found so for  based on fitness  6. Output the pest solution   | + | Translate the genetic sequence into a          |
| e. Replacement:  - Replacement:  - Replace the old population with New Sopulation  f. Track Best Solution:  - Update the best solution found so for based on fitness  6. Output the pest solution   | 1 | solution                                       |
| - Replace the old population with New Population  f. Trade Best Solution:  - Update the best solution found so for based on fitness  6. Output the pest solution  | + | compute the fitness using the objectne fit     |
| - Replace the old population with New Espul  f. Trade Best Solution:  - Update the best solution found so for based on fitness  6. Output the pest solution   |   | e Replacement:                                 |
| - Update the best solution found so for<br>based on fitness<br>6. Output the pert solution  |   | - Replace the old population with New Popul    |
| 6. Output the pert solution   |   |  |
| 6. Output the pert solution   |   | - Update the best solution found so for        |
| 6. Output the pert solution - Return the best genetic sequence and its corresponding fitness value.   |   | based on fitness                               |
| - Return the best genetic sequence and its corresponding fitness value.   | 6 | · Output the pert solution                     |
| corresponding fitners value.  | • | Return the best genetic sequence and its       |
|   |   | corresponding fitnere value.                   |
|   |   |  |
|   |   |  |

Date / /

| 24     | Implementation ( Application - Minimizing quad   |
|--------|--|
|        | MInput   |
|        |  |
|        | function: n2-2n+10   |
|        | pop-624: 20  |
|        | generation = 100   |
|        | x. min, x_ max = -10,10  |
|        | crossover. rate =0.8   |
|        | · ·  |
|        | 11 Output:   |
|        | Best solution: x=1,00000, rinimum value: fc):  |
|        | 100  |
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# Code: import random # Objective function def objective function(x): return $x^{**}2 - 2^*x + 10$ # Initialize population definitialize population(pop size, x min, x max): return [random.uniform(x min, x max) for in range(pop size)] # Evaluate fitness def evaluate fitness(population): return [objective function(x) for x in population] # Selection: Tournament Selection def select parents(population, fitness, tournament size=3): selected = [] for in range(len(population)): competitors = random.sample(list(zip(population, fitness)), tournament size) winner = min(competitors, key=lambda x: x[1])selected.append(winner[0]) return selected # Crossover: Arithmetic crossover def crossover(parents, crossover rate=0.8): offspring = [] for i in range(0, len(parents), 2): p1, p2 = parents[i], parents[(i+1) % len(parents)]if random.random() < crossover rate: alpha = random.random() child1 = alpha \* p1 + (1 - alpha) \* p2child2 = alpha \* p2 + (1 - alpha) \* p1

```
else:
       child1, child2 = p1, p2
     offspring.extend([child1, child2])
  return offspring
# Mutation: Add small random noise
def mutate(offspring, mutation rate=0.1, mutation step=0.5):
  for i in range(len(offspring)):
     if random.random() < mutation rate:
       offspring[i] += random.uniform(-mutation step, mutation step)
  return offspring
# Gene Expression Algorithm
def gene expression algorithm(pop size, generations, x min, x max):
  population = initialize population(pop size, x min, x max)
  best solution = None
  best fitness = float("inf")
  for gen in range(generations):
     fitness = evaluate fitness(population)
     if min(fitness) < best fitness:
       best fitness = min(fitness)
       best solution = population[fitness.index(best fitness)]
     parents = select parents(population, fitness)
     offspring = crossover(parents)
     population = mutate(offspring)
  return best solution, best fitness
pop size = 20
generations = 100
x \min_{x} x \max = -10, 10
```

 $best_x$ ,  $best_fitness = gene_expression_algorithm(pop_size, generations, x_min, x_max)$  $print(f"Best solution: x = {best_x:.5f}, Minimum value: f(x) = {best_fitness:.5f}")$