

Assignment 1 - EE1030

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I. E - SUBJECTIVE PROBLEMS

1. A curve 'C' passes through (2, 0) and the slope at (x, y) as $\frac{(x+1)^2+(y-3)}{x+1}$. Find the equation of the curve. Find the area bounded by curve and x-axis in fourth quadrant. (2004 - 4Marks)
2. If length of tangent at any point on the curve $y = f(x)$ intercepted between the point and the x-axis in fourth quadrant. (2005 - 4Marks)

II. F - MATCH THE FOLLOWING

- 1) Match the statements/expressions in **Column I** with the open intervals in **Column II**.

III. H - ASSERTION REASON TYPE QUESTIONS

- 1) Let solution $y = y(x)$ of the differential equation $x\sqrt{x^2-1}dy - y\sqrt{y^2-1}dx = 0$ satisfy $y(2) = \frac{2}{\sqrt{3}}$.

STATEMENT-1: $y(x) = \sec\left(\sec^{-1}x - \frac{\pi}{6}\right)$ and

STATEMENT-2: $y(x)$ is given by $\frac{1}{y} = \frac{2\sqrt{3}}{x} - \sqrt{1 - \frac{1}{x^2}}$ (2008)

- a) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is a correct explanation for STATEMENT-1
- b) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is **NOT** a correct explanation for STATEMENT-1
- c) STATEMENT-1 is True, STATEMENT-2 is False
- d) STATEMENT-2 is False, STATEMENT-2 is True

IV. I - INTEGER VALUE CORRECT TYPE

- 1) Let $y'(x) + y(x)g'(x) = g(x)$, $y(0) = 0$, $x \in \mathbb{R}$, where $f'(x)$ denotes $\frac{df(x)}{dx}$ and $g(x)$ is a given non-constant differentiable function on \mathbb{R} with $g(0) = g(2) = 0$. Then the value of $y(2)$ is (2011)
- 2) Let $f: \mathbb{R} \rightarrow \mathbb{R}$ be a differentiable function with $f(0) = 0$. If $y = f(x)$ satisfies the differential

equation $\frac{dy}{dx} = (2+5y)+(5y-2)$, then the value of $\lim_{x \rightarrow -\infty} f(x)$ is. (JEEAdv.2018)

- 3) Let $f: \mathbb{R} \rightarrow \mathbb{R}$ be a differentiable function with $f(0) = 1$ and satisfying the differential equation $f(x+y) = f(x)f'(y) + f'(y)f(x)$ for all $x, y \in \mathbb{R}$ then, the value of $\log_e(f(4))$ is. (JEEAdv.2018)

V. SECTION-B // JEE MAIN / AIEEE

- 1) The order and degree of the differential equation $\left(1 + 3\frac{dy}{dx}\right)^{\frac{2}{3}} = 4\frac{d^3y}{dx^3}$ are [2002]
 - a) $\left(1, \frac{2}{3}\right)$
 - b) $(3, 1)$
 - c) $(3, 3)$
 - d) $(1, 2)$
- 2) The solution of the equation $\frac{d^2y}{dx^2} = e^{-2x}$ [2002]
 - a) $\frac{e^{-2x}}{4}$
 - b) $\frac{e^{-2x}}{4} + cx + d$
 - c) $\frac{1}{4}e^{-2x} + cx^2 + d$
 - d) $\frac{1}{4}e^{-4x} + cx + d$
- 3) The degree and order of the differential equation of the family of all parabolas whose axis x-axis, are respectively. [2003]
 - a) 2, 3
 - b) 2, 1
 - c) 1, 2
 - d) 3, 2
- 4) The solution of the differential equation $(1+y^2) + (x - e^{\tan^{-1}y})\frac{dy}{dx} = 0$, is [2003]
 - a) $xe^{2\tan^{-1}y} = e^{\tan^{-1}y} + k$
 - b) $(x-2) = ke^{2\tan^{-2}y}$
 - c) $2xe^{\tan^{-1}y} = e^{2\tan^{-1}y} + k$
 - d) $xe^{\tan^{-1}y} = \tan^{-2}y + k$
- 5) The differential equation for the family of circle $x^2 + y^2 - 2ay = 0$, where a is an arbitrary constant is [2004]
 - a) $\frac{(x^2 + y^2)}{2xy}y'/prime = \frac{(x^2 - y^2)}{2xy}y'/prime =$
 - b) $2\frac{(x^2 + y^2)}{xy}y'/prime = \frac{2(x^2 - y^2)}{xy}y'/prime =$
- 6) Solution of the differential equation $ydx + (x + x^2y)dy = 0$ is [2004]
 - a)

$$\begin{array}{ll} \log y = Cx & \text{c) } \frac{1}{xy} + \log y = C \\ \text{b) } -\frac{1}{xy} + \log y = C & \text{d) } -\frac{1}{xy} = C \end{array}$$

- 7) The differential equation representing the family of curves $y^2 = 2c(x + \sqrt{c})$, where $c > 0$, is a parameter, is of order and degree as follows:
[2005]

$$\begin{array}{ll} \text{a) order 1, degree 2} & \text{c) order 1, degree 3} \\ \text{b) order 1, degree 1} & \text{d) order 2, degree 2} \end{array}$$

- 8) If $x \frac{dy}{dx} = y(\log y - \log x + 1)$, then the solution of the equation is
[2005]

$$\begin{array}{ll} \text{a) } y \log \left(\frac{x}{y} \right) = cx & \text{c) } \log \left(\frac{y}{x} \right) = cx \\ \text{b) } y \log \left(\frac{y}{x} \right) = cy & \text{d) } \log \left(\frac{x}{y} \right) = cy \end{array}$$