

# Assignment 2 - EE1030

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## 1 E - SUBJECTIVE PROBLEMS

1. A curve 'C' passes through (2,0) and the slope at (x,y) as  $\frac{(x+1)^2+(y-3)}{x+1}$ . Find the equation of the curve. Find the area bounded by curve and x-axis in fourth quadrant. (2004 – 4Marks)
2. If length of tangent at any point on the curve  $y = f(x)$  intercepted between the point and the x-axis in fourth quadrant. (2005 – 4Marks)

## 2 F - MATCH THE FOLLOWING

- 1) Match the statements/expressions in **Column I** with the open intervals in **Column II**.

## 3 H - ASSERTION & REASON TYPE QUESTIONS

- 1) Let solution  $y = y(x)$  of the differential equation  $x\sqrt{x^2-1}dy - y\sqrt{y^2-1}dx = 0$  satisfy  $y(2) = \frac{2}{\sqrt{3}}$ .

**STATEMENT-1:**  $y(x) = \sec\left(\sec^{-1}x - \frac{\pi}{6}\right)$  and

**STATEMENT-2:**  $y(x)$  is given by  $\frac{1}{y} = \frac{2\sqrt{3}}{x} - \sqrt{1 - \frac{1}{x^2}}$  (2008)

- a) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is a correct explanation for STATEMENT-1
- b) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is **NOT** a correct explanation for STATEMENT-1
- c) STATEMENT-1 is True, STATEMENT-2 is False
- d) STATEMENT-2 is False, STATEMENT-2 is True

## 4 I - INTEGER VALUE CORRECT TYPE

- 1) Let  $y'(x) + y(x)g'(x) = g(x)$ ,  $g'(x), y(0) = 0$ ,  $x \in \mathbb{R}$ , where  $f'(x)$  denotes  $\frac{df(x)}{dx}$  and  $g(x)$  is a given non-constant differentiable function on  $\mathbb{R}$  with  $g(0) = g(2) = 0$ . Then the value of  $y(2)$  is (2011)
- 2) Let  $f : \mathbb{R} \rightarrow \mathbb{R}$  be a differentiable function with  $f(0) = 0$ . If  $y = f(x)$  satisfies the differential equation  $\frac{dy}{dx} = (2+5y)(5y-2)$ , then the value of  $\lim_{x \rightarrow -\infty} f(x)$  is. (JEEAdv.2018)
- 3) Let  $f : \mathbb{R} \rightarrow \mathbb{R}$  be a differentiable function with  $f(0) = 1$  and satisfying the differential equation  $f(x+y) = f(x)f'(y) + f'(y)f(x)$  for all  $x, y \in \mathbb{R}$  then, the value of  $\log_e(f(4))$  is. (JEEAdv.2018)

## 5 SECTION-B // JEE MAIN / AIEEE

- 1) The order and degree of the differential equation  $\left(1 + 3\frac{dy}{dx}\right)^{\frac{2}{3}} = 4\frac{d^3y}{dx^3}$  are [2002]

a)  $\left(1, \frac{2}{3}\right)$   
 b)  $(3, 1)$

c)  $(3, 3)$   
 d)  $(1, 2)$

2) The solution of the equation  $\frac{d^2y}{dx^2} = e^{-2x}$  [2002]

a)  $\frac{e^{-2x}}{4}$   
 b)  $\frac{e^{-2x}}{4} + cx + d$

c)  $\frac{1}{4}e^{-2x} + cx^2 + d$   
 d)  $\frac{1}{4}e^{-4x} + cx + d$

3) The degree and order of the differential equation of the family of all parabolas whose axis  $x$ -axis, are respectively. [2003]

a) 2, 3  
 b) 2, 1

c) 1, 2  
 d) 3, 2

4) The solution of the differential equation  $(1 + y^2) + (x - e^{\tan^{-1}y}) \frac{dy}{dx} = 0$ , is [2003]

a)  $xe^{2\tan^{-1}y} = e^{\tan^{-1}y} + k$   
 b)  $(x - 2) = ke^{2\tan^{-2}y}$

c)  $2xe^{\tan^{-1}y} = e^{2\tan^{-1}y} + k$   
 d)  $xe^{\tan^{-1}y} = \tan^{-2}y + k$

5) The differential equation for the family of circle  $x^2 + y^2 - 2ay = 0$ , where  $a$  is an arbitrary constant is [2004]

a)  $(x^2 + y^2)y'/prime = 2xy$   
 b)  $2(x^2 + y^2)y'/prime = xy$

c)  $(x^2 - y^2)y'/prime = 2xy$   
 d)  $2(x^2 - y^2)y'/prime = xy$

6) Solution of the differential equation  $ydx + (x + x^2y)dy = 0$  is [2004]

a)  $\log y = Cx$   
 b)  $-\frac{1}{xy} + \log y = C$

c)  $\frac{1}{xy} + \log y = C$   
 d)  $-\frac{1}{xy} = C$

7) The differential equation representing the family of curves  $y^2 = 2c(x + \sqrt{c})$ , where  $c > 0$ , is a parameter, is of order and degree as follows: [2005]

a) order 1, degree 2  
 b) order 1, degree 1

c) order 1, degree 3  
 d) order 2, degree 2

8) If  $x \frac{dy}{dx} = y(\log y - \log x + 1)$ , then the solution of the equation is [2005]

a)  $y \log\left(\frac{x}{y}\right) = cx$   
 b)  $y \log\left(\frac{y}{x}\right) = cy$

c)  $\log\left(\frac{y}{x}\right) = cx$   
 d)  $\log\left(\frac{x}{y}\right) = cy$