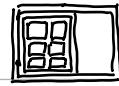


Sliding Window



○ Count Occurrences of Anagrams :

```

while (j < n)
    mp[s[j]] --; if (s[j] in anagram)
    if (j - i + 1 > lenAnagram)
        mp[s[i]] --; if (s[i] in anagram)
        i++;
    if (j - i + 1 == lenAnagram & mp all 0's) ans++;
    j++;

```

Instead of this
use counter.

○ Find all Anagrams (return indices)

○ Minimum Subarray Sum \geq Target :

```

while (j < n)
    s += nums[j]
    while (s >= Target)
        ans = min(ans, j - i + 1)
        s -= s[i]
        i++;
    j++;

```

○ Find First -ve element in window size k :

```

while (j < n)
    if (nums[j] < 0) v.push_back(j). instead of P
    if (j - i + 1 == k)
        if (v.size() <= p) ans.push(0) can use
        else ans.push(v[p])
        if (nums[i] < 0) p++;
        i++;
    j++;

```

Queue & remove front-

○ Minimum Window Substring Hard

```

while (i)
{
    // update jth counter
    while (counter == 0)
    {
        if (j - i + 1 < currMin) ....
        // update i th index // 
    }
    i++;
}

```

0 Contains Duplicate II

0 Count Subarrays with fixed Bounds Hard

nums: 6 3 5 2 1

$\min k = 1$ $\max k = 5$

ans = 2

subarray having $\min = \min k$
 $\max = \max k$.

6	1	2	3	4	5	6	7	8
1	7	2	5	3	1	4	3	9

calIdx	-1	-1	1 -	1	1	1	1	1	8
minIdx	-1	0	0	0	0	0	5	5	5

maxIdx	-1	-1	-1 0	-1	3	3	3	3	3
temp	$\frac{-1-(-1)}{=0}$	$\frac{-1-1=-2}{}$	-2	$\frac{0-1=-1}{}$	-1	$\frac{3-1=2}{}$	$\frac{3-1=2}{}$	$\frac{3-1=2}{}$	$\frac{3-8=-5}{}$

$[\min(\minIdx, \maxIdx) - \text{calIdx}]$

$\sim v$ means first valid
 boundary: 1
 is behind culprit: 7

means from
 last culprit to first

* again
 Invalid
 Boundary

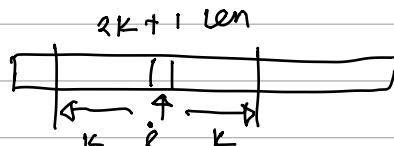
valid subarray & possible subarrays are there

2 5 3 1 and

5 3 1	\rightarrow	2 5 3 1 9
$2+2$	\rightarrow	3 3 1 9
		4 more
		\rightarrow
		2 5 3 1 4 3
		\rightarrow
		5 3 1 9 3

valid subarrays
 possible.

0 K radius Subarray Averages



0	1	2	3	4	5	6
· · · · · · ·	· · · · · · ·					

if ($j >= 2 \times k$)
 ans[j] = sumTill / (2k+1)

sum -= nums[i];

i++;

0 Maximum 1's after Deleting 1-Zero :-

```
while (cnt > 1)
{
    if (nums[i] == 0) cnt--;
    i++;
}
ans = max(ans, j-i)
```

2nd approach

```
lastSeen = -1
if (nums[j] == 0) {
    if (lastSeen != -1) {
        i = lastSeen + 1
        lastSeen = j
    } else lastSeen = j
}
ans = max(j-i)
```

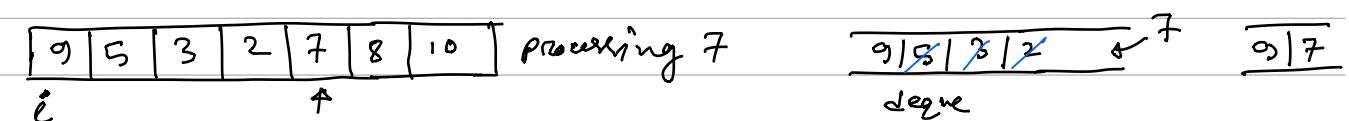
O Maximize Conversion in Exam :-

"TTFTFTFFF" maximum K no. of Flips are possible T \rightarrow F, F \rightarrow T

```

{ while (cntT, cntF (....)++)
    while (min(cntT, cntF) > K)
        cntT (....)--
        cntF (....)--
        i++
    ans = max(ans, j - i + 1)
    j++
}
  
```

O Sliding Window Maximum (Monotonic Deque) Hard



when i moves

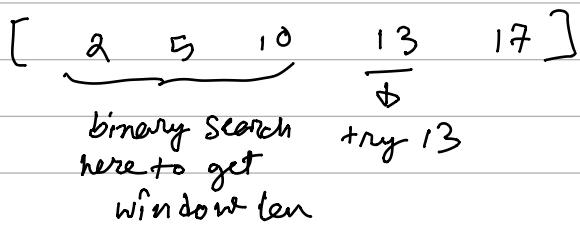
it will remove front of deque

O Frequency of the most Frequent Element :-

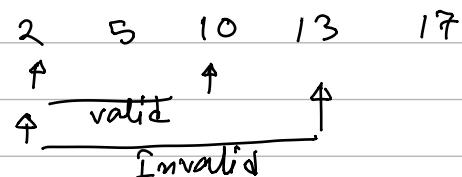
arr: [2, 5, 10, 13, 17] operations = 5.

arr[i] can be changed from $x \rightarrow x+k$ using k operation points
return freq of max element

\rightarrow since we can't decrement; max freq must be of some bigger no.



or, use sliding window for obtaining max window.



while ($j < n$)

$sm += nums[j]$

instead of
while; if can
also work.

if (while ($(j-i+1) * nums[j] - sm > k$)
 $sm -= nums[i]$
 $i++$)
 $ans = max(ans, j - i + 1)$

○ Count Complete Substrings :-

"igigee" count substring where no 2 consecutive characters are more different than 2

in an subarray all character must be present exactly K no. of time -

① separate $\rightarrow "a\underset{|}{a}d\underset{|}{d}e\underset{|}{e}x\underset{|}{x}x\underset{|}{x}"$ solve separately

count no. of subarray where all element occur exactly K no. of time

② need to write the sliding window code separately.

solver(str, start, end, k) \rightarrow return \uparrow they

method; count all subarray having 1 unique character

" " " " " " "

$\min(2^6, \text{no. of unique char available})$

take fixed window length = $K \times 1$ for 1 unique char

$K \times 2$ " 2 " "

$K \times 3$ " 3 " "

:

○ Binary Subarrays with Sum :-

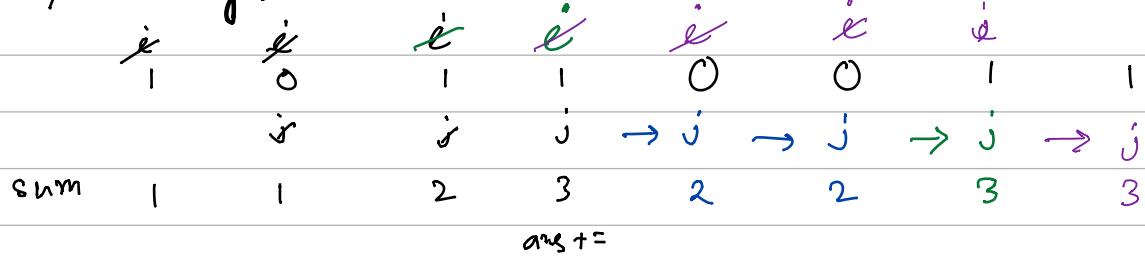
arrs [1, 0, 1, 1, 0, 0, 1, 1] target : 2

∅ PrefixSum (CumSum) + ~~Binary Search~~ HashTable

ip	1	0	1	1	0	0	1	1
cumSum	1	1	2	3	3	3	4	5
ans	0	0	cumSum - Target (+1)	+2	+2	+2	+1	+3
H.T.	0:1	0:1	0:1	0:1	0:1	0:1	0:1	0:1
	1:1	1:2	1:2	1:2	1:2	1:2	1:2	1:2
			0:1	0:1	0:1	0:1	0:1	0:1
			1:1	1:1	1:1	1:1	1:1	1:1
			2:1	2:1	2:1	2:1	2:1	2:1
			3:1	3:2	3:3	3:3	3:3	3:3

[0011
011
11]

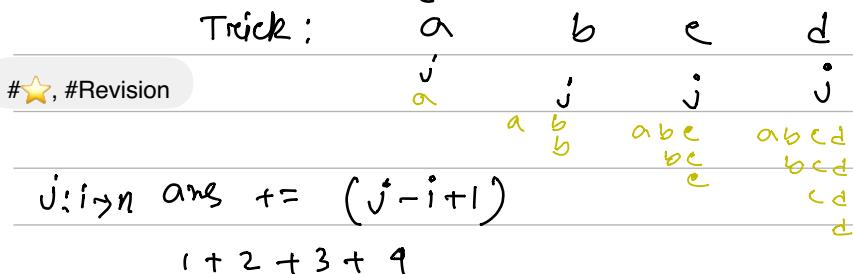
∅ Sliding Window



$$\begin{array}{ccccccc}
 & \text{2 accounting} & & \text{1 + count zero} & & & \\
 \text{for} & \{101\} & \leftarrow & = 1+1 & +1 & +1 & +1 + \text{count zero} \\
 \text{and } & \{011\} & & = 2 & \{110\} & \{1100\} & \{1001\} \\
 & & & & +3 & & \\
 & & & & \{0011\} & & \\
 & & & & \{011\} & & \\
 & & & & \{11\} & & \\
 & & & & & & \\
 \end{array}$$

○ Subarray product less than K

To count all subarrays $a, b, c, d, ab, bc, \dots, abcd$



next when i moves

valid subarray count
still holds.

i	a	b	c	d	e
j	b	be	bc	bcd	cd

$\begin{matrix} b \\ b \\ be \\ be \\ c \\ c \\ cd \\ cd \\ e \\ e \end{matrix}$ } valid from b to e
 $\begin{matrix} e \\ e \\ e \\ e \end{matrix}$ } count = 9
 ans += 9 ✓

> Similar Type

- Maximum size subarray sum equals K
- Subarray sum equals K.
- Count subarrays having equal vowel & consonants.
- Longest Substring containing vowels in even Count.
- Maximum no. of vowels in a substring of given length.

0 Length of longest Subarray with at most K frequency:

✓ good variable

✓ unordered_map

while → if ($mp[nums[j]] \geq k$)

good --j;

$mp[nums[j]]++$

if can $while(good != 0)$

also work here

since $j-i+1$ is not changing

after achieving maximum

$ans = max(ans, j-i+1)$

K=2						$g=0$	$g=1$	$g=1^*$
1	2	3	0	0	0			
1:1	1:1	1:1	1:2	1:2	1:2			
2:1	2:1	2:1	2:2	2:2	2:2			
3:1	3:1	3:1	3:2	3:2	3:2			

1:1 1:1 1:1 1:2 1:2 1:2 1:3 *

2:1 2:1 2:1 2:2 2:2 2:2 2:2

3:1 3:1 3:1 3:2 3:2 3:2 3:2

0 Count Subarrays where Element Appears atleast K times.

↳ element is max element here.

nums: [1, 3, 2, 3, 3] $K=2$

1	3	2	3	3
0	1	1	2	2
i	i	i	j	j

ans $+ (5-3) = 2$ $+ (5-3) = 2$ $+ (5-4) = 1$ $+ (5-4) = 1$

accounting for { 1 3 2 3 } { 3 2 3 } { 2 3 3 } { 3 3 }

while ($j < n$)

elementCount += 1:0 if $nums[j] == element$.

while (elementCount == K)

ans += $n-j$ $\rightarrow j \rightarrow n-1 = n-1-j+1 = n-j$

elementCount -= 1:0 if $nums[i] == element$
i++

j++

» Approach 2 using Hash table

1	3	2	3	3	2
0	1	1	2	3	3

Table

1:1

3
4
5

ans : + 0 + 0 + 0 + 2 + 4 + 4

{ 1 3 2 3 } { 1 3 2 3 } { 1 3 2 3 } { 1 3 2 3 } { 1 3 2 3 }

Accounting for { 1 3 2 3 } { 1 3 2 3 } { 1 3 2 3 } { 1 3 2 3 } { 1 3 2 3 }

```

code : for (int i=0; i<n; i++) {
    if (numsc[i] == element) {
        elementCount++;
        mp[elementCount] = i;
    }
    if (elementCount >= k) ans += mp[elementCount - k + 1] + 1;
}

```

○ Subarrays with K Different Integers :-

Hard

Good subarray consisting exactly K unique integers

[1 2 3 1 1 2 3] → consist 3 integers.

It's difficult to find exactly K element.

j-i+1 gives all subarrays ending at j (In these subarrays there will be all subarrays where at max K unique elements possible i.e. subarrays having exactly K-1 unique elements, exactly K-2 unique elements ... etc.)

$$\text{ans} = f(k) - f(k-1)$$

⇒ at max K=2 elements,

	0	1	2	3	4	5
1	1:1	1:1	1:2	1:2	1:2+0	2:1
2		2:1	2:1	2:2	2:2+1	3:1
3				2:2	3:1	3:1
4					4:1	4:1

Table :

ans : +1 +2 +3 +4 +(j-i+1) = 2 + 2

j-i+1 {1} {1,2} {1,2,3} {1,2,1,2} {2,3} {3,4}

accounting for {2} {2,1} {2,1,3} {2,1,2} {1,2} {1,2,3} {2,3,4}

⇒ at max K=3 elements,

	0	1	2	3	4	5
1	1:1	1:1	1:2	1:2	1:2	1:2+0
2		2:1	2:1	2:2	2:2	2:2+1
3				2:2	3:1	3:1
4					4:1	4:1

Table :

ans : +1 +2 +3 +4 +5 +(5-3+1) = 3

j-i+1 {1} {1,2} {1,2,3} {1,2,1,2,3} {1,2,1,2,3} {2,3,4}

{1,2,3} {1,2,3} {1,2,3} {1,2,3} {1,2,3} {1,2,3}

exactly 3 elements : {1,2,1,2,3}, {2,1,2,3}, {1,2,3}, {2,3,4}

* using countOfDistinct instead of mp.size() is faster;

```

while( j < n )
    mp[nums[j]]++;
    while( mp.size() > k )
        mp[nums[i]]--;
        if( mp[nums[i]] == 0 ) mp.erase(nums[i]);
        i++;
    result += j - i + 1;
    j++;

```

Approach 2 one pass: $k=2$

firstⁱ

1

2

1

2

3

4

5

\hat{i}

\hat{i}

\hat{i}

\hat{i}

\hat{i}

Table: 1:1

1:1

1:2

1:1

1:1

2:1

2:1

2:1

2:2

3:1

3:1

$i \text{ at } 0$

$i \text{ at } 1$

$i \text{ at } 2$

$i \text{ at } 3$

$i \text{ at } 4$

ans:

$+1+(0)$

$+1+(1)$

$+1+(2)$

$+1+(3)$

$+1+(0)$

$\leftarrow = 1 + (\text{first } \hat{i} - i)$

$\{1, 2\}$

$\{2, 1\}$

$\{1, 2\}$

$\{2, 3\}$

$\{3, 4\}$

accounting for π

ans = 8 ✓

... 3 9 3 1 2 1 [2] \rightarrow Smallest window
 $\underbrace{\hspace{1cm}}$ $\begin{matrix} \text{or} \\ \text{2 distinct elements} \end{matrix}$
 whole window of those
 2 distinct elements.

first $\hat{i} \hat{j}$
 3 3 9 3 1 2 1 3 3 4 3 1 2 1 2 1 2 1 \rightarrow
 possible: {3, 3, 4, 3} from first \hat{i} increases
 valid 3 3 9 3 1 2 1 2 1 2 1 2 1
 \leftarrow possible: {3, 1, 2, 1, 2, 1}

while (mp[nums[i]] > 1) {
 mp[nums[i]]--;
 i++; }

This will increment \hat{i} to smallest valid
 $i \leftrightarrow j$ window

first $\hat{i} \hat{j}$
 3 3 4 3 1 2 1 2 1 1 2 1 2 1
 possible: {3, 1, 2, 1, 2, 1, 2, 1}

```
while (j < n) {
    mp[nums[j]]++;
    while (mp.size() > k)
        mp[nums[i]]--;
        if 0 then erase
        i++;
        first_i = i;
    while (mp[nums[i]] > 1)
        mp[nums[i]]--;
        i++;
    if (mp.size() == k) ans += 1 + (i - first_i)
    j++;
}
```

○ Longest Contiguous Subarray with $\text{abs}(\max - \min) \leq \text{limit}$

approach  $\text{nums}[i:j]$

multiset < pair<int, int>> → storing $\{\text{nums}[j], j\}$

while (setMax → first - setMin → first) $\leq \text{limit}$)
 st.erase ({nums[i], i}); i++
 // update setMax, setMin.

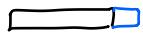
○ Find Subarray with Bitwise And closest to k

[a b c d ..] find min |k - AND(subarray)|

$x_1 x_2 x_3 x_4 x_5$

$\text{AND}(x_1, x_2, x_3, x_4) \leq \text{AND}(x_1, x_2, x_3, x_4, x_5)$ (Always)

so,

if ($k < \text{AND}$) $j++$ (expand) 

else if ($k > \text{AND}$) $i++$ (shrink) 

Now updating the AND without reiterating the array

1 1 0 0	a ₁
1 0 1 0	a ₂
<u>1 0 1 1</u>	a ₃
<u>1 0 0 0</u>	

remove a₁,

1 0 1 0	a ₂
<u>1 0 1 1</u>	a ₃
<u>2 0 1 0</u>	

0 1 2 3 4	31
<u>1 2 1 3 1</u>	

frequency of 1

0 1 2 3 4	31
<u>1 1 2 1 0 2 1</u>	

len(subarr) == freq of 1

means No 0 at 1st and 3rd bit

Count Substring that Satisfy K-Constraint - II

1 0 1 1 0 0 1 0 1 1 0 0 0 1

in the substring either $\text{count}[0] \leq K$ or $\text{count}[1] \leq K \}$ then valid.

also the query count # valid substring from $[\text{low}, \text{high}]$.

idea :

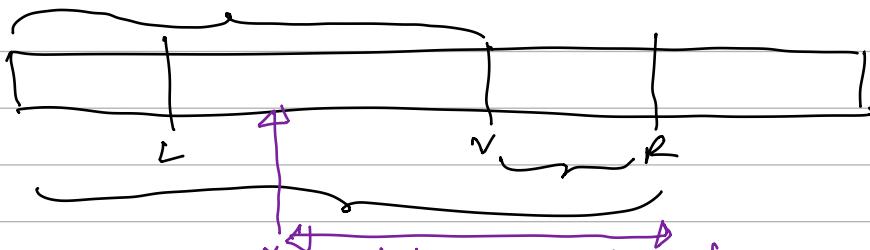


maximum valid window
from low towards high.

$$\text{len} = \text{valid rightmost} - \text{low} + 1$$

$$\text{result} = \text{len} \times (\text{len} + 1) / 2$$

result += remaining.



$$\text{Prefix Sum Till } [R] = 0 \text{ to } X + L_1 \times (L_1 + 1) / 2$$

$$-\text{Prefix Sum Till } [V] = 0 \text{ to } L + L \times (L + 1) / 2$$

$$V \rightarrow R$$